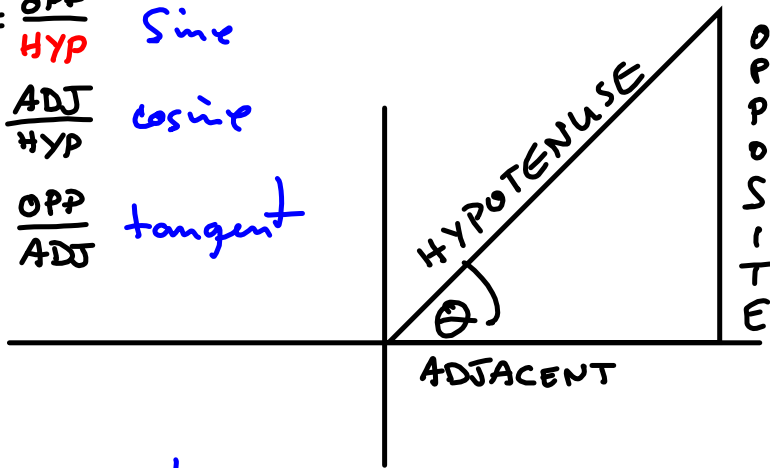


Pythagorus says:  
 $a^2 + b^2 = c^2$

SOHCAHTOA

$\sin \theta = \frac{\text{OPP}}{\text{HYP}}$  Sine  
 $\cos \theta = \frac{\text{ADJ}}{\text{HYP}}$  cosine  
 $\tan \theta = \frac{\text{OPP}}{\text{ADJ}}$  tangent



$\csc \theta = \frac{1}{\sin \theta}$  cosecant

$\sec \theta = \frac{1}{\cos \theta}$  secant

$\cot \theta = \frac{1}{\tan \theta}$  cotangent

Reciprocal Identities

$\sin \theta = \frac{\text{OPP}}{\text{HYP}}$

$\csc \theta = \frac{\text{HYP}}{\text{OPP}}$

$\cos \theta = \frac{\text{ADJ}}{\text{HYP}}$

$\sec \theta = \frac{\text{HYP}}{\text{ADJ}}$

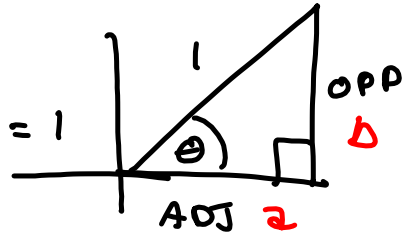
$\tan \theta = \frac{\text{OPP}}{\text{ADJ}}$

$\cot \theta = \frac{\text{ADJ}}{\text{OPP}}$

c

Pythagorean Identities.

Suppose the hypotenuse is  $c = 1$



$$\sin \theta = \frac{\text{OPP}}{1} = \text{OPP} = b$$

$$\cos \theta = \frac{\text{ADJ}}{1} = \text{ADJ} = a$$

$$a^2 + b^2 = c^2 = 1$$

$$(\sin \theta)^2 + (\cos \theta)^2 = 1$$

$$\textcircled{1} \sin^2 \theta + \cos^2 \theta = 1$$

Notation!

$$(\sin \theta)^2 = \sin^2 \theta$$

$$(\sin \theta)^3 = \sin^3 \theta$$

$$\frac{1}{\sin \theta} = (\sin \theta)^{-1} = \sin^{-1} \theta,$$

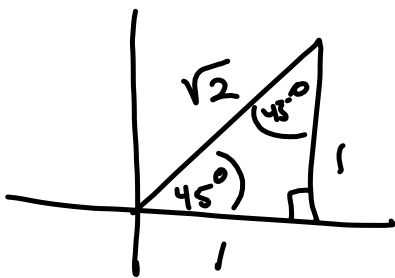
but SOMETIMES

$\sin^{-1} \theta$  means the inverse  
FUNCTION of sine.

$\sin^{-1}$  on calculator  
is NOT  $\frac{1}{\sin \theta}$

It means "Give me  
sine, I tell you  $\theta$ ."

who's the silly  
geese, Millie?



$$\sin \theta = \frac{1}{\sqrt{2}}$$

$\sin^{-1}$  Key

$$\sin^{-1} \left( \frac{1}{\sqrt{2}} \right)$$

Derivation of the others:



$$\begin{aligned} \tan^2 \theta + 1 &= \frac{\sin^2 \theta}{\cos^2 \theta} + 1 & \tan \theta &= \frac{b}{a} = \frac{b/c}{a/c} \\ &= \frac{\sin^2 \theta}{\cos^2 \theta} + \frac{1}{1} \cdot \frac{\cos^2 \theta}{\cos^2 \theta} & &= \frac{\sin^2 \theta + \cos^2 \theta}{\cos^2 \theta} = \frac{\sin^2 \theta}{\cos^2 \theta} \\ &= \frac{1}{\cos^2 \theta} = \left( \frac{1}{\cos \theta} \right)^2 = \sec^2 \theta \end{aligned}$$

Summarize:  $\textcircled{2} \tan^2 \theta + 1 = \sec^2 \theta$

$\textcircled{3} \cot^2 \theta + 1 = \csc^2 \theta$

$$\left( \frac{\sin \theta}{\cos \theta} \right)^2 = \frac{(\sin \theta)^2}{(\cos \theta)^2} = \frac{\sin^2 \theta}{\cos^2 \theta}$$

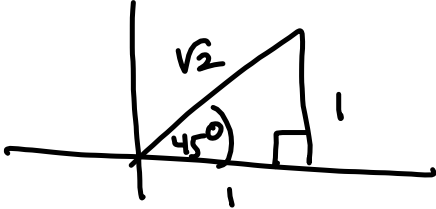
$$\sin^2 \theta = 1 - \cos^2 \theta$$

$$\cos^2 \theta = 1 - \sin^2 \theta$$

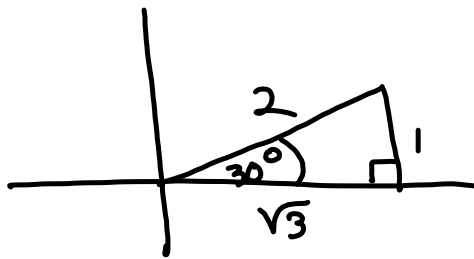
$$\csc^2 \theta - 1 = \cot^2 \theta$$

} Variations flowing from 1-3.

"1-1- $\sqrt{2}$ " 45-45 right triangle



"1-2- $\sqrt{3}$ " 30-60 (or 60-30)

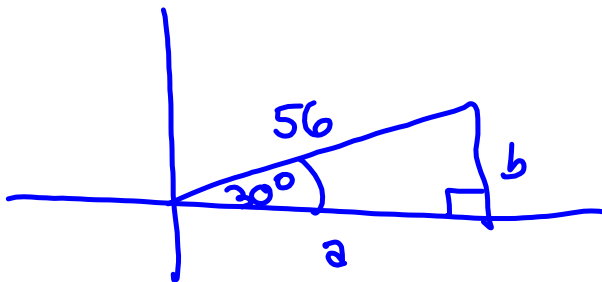
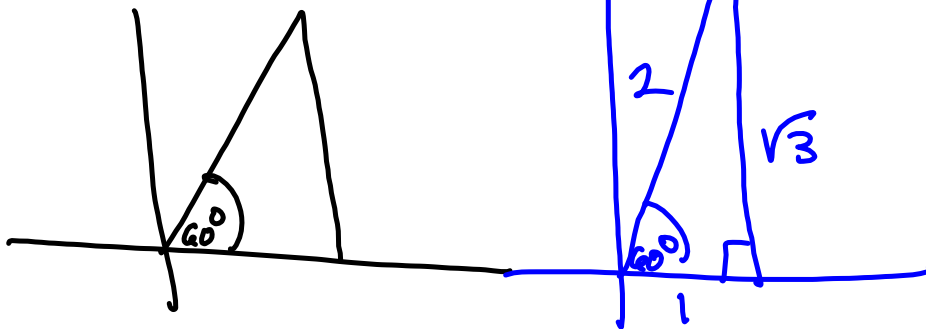


$$\sqrt{3} \approx 1.732$$

$$\sin 30^\circ = \frac{1}{2}$$

$$\cos 30^\circ = \frac{\sqrt{3}}{2}$$

$$\tan 30^\circ = \frac{1}{\sqrt{3}}$$



Find  $a$  &  $b$ .

$$\sin 30^\circ = \frac{b}{56} = \frac{1}{2}$$

$$\rightarrow b = 56 \cdot \frac{1}{2} = 28 = b$$

$$\cos 30^\circ = \frac{a}{56} = \frac{\sqrt{3}}{2}$$

$$\rightarrow a = 56 \cdot \frac{\sqrt{3}}{2} = 28\sqrt{3} = a$$

# Quadrantal Angles & Degenerate Triangles

