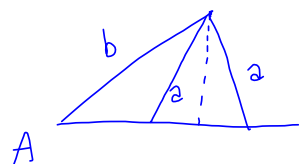


Law of Sines.

Look for 2-solution triangles.



Law of cosines SAS

Area of obtuse triangle

3.3 Vectors. Magnitude, Sum, Linear Combos!
 ↓ Resultant
 $\vec{u} + \vec{v}$
 $2\vec{u} - \vec{v}$

4.1 Complex #s $z = 3 + 2i$, $w = 7 - 5i$

$$\begin{aligned} & zw \\ & z+w \\ & z+\bar{z} \\ & z\bar{z} \end{aligned}$$

4.2 Let $P(x) = 13x^5 - 5x^4 + 7x^2 - 11x + 1$
 Use synthetic division to find $P(3)$

$$\begin{array}{r|rrrrrr} 3 & 13 & -5 & 0 & 7 & -11 & 1 \\ & & 39 & 102 & 306 & 939 & 2784 \\ \hline & 13 & 34 & 102 & 313 & 928 & 2785 = P(3) \\ & & & & & 3 & 3 \\ & & & & & 93 & 92184 \end{array}$$

Remainder
Theorem

This work says

$$P(x) = (x-3)(13x^4 + 34x^3 + 102x^2 + 313x + 928) + 2785$$

Find all zeros of, given $x=5$ is a zero.

$$P(x) = 4x^3 - 32x^2 + 73x - 65$$

$$\begin{array}{r|rrrr} 5 & 4 & -32 & 73 & -65 \\ & & 20 & -60 & 65 \\ \hline & 4 & -12 & 13 & 0 \end{array}$$

This says $P(x) = (x-5)(4x^2 - 12x + 13)$
 ↓ Depressed Polynomial.

$$4x^2 - 12x + 13 = 0$$

$$a=4, b=-12, c=13$$

$$b^2 - 4ac = (-12)^2 - 4(4)(13)$$

$$= 144 - 208$$

$$= -64 \rightarrow \sqrt{-64} = i\sqrt{64} = 8i$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{12 \pm 8i}{2(4)} = \frac{\cancel{4}(3 \pm 2i)}{\cancel{2}(4)} = \frac{3 \pm 2i}{2}$$

$$5, \frac{3 \pm 2i}{2}$$

Split $P(x)$ into linear factors:

$$P(x) = 4(x-5)\left(x - \left(\frac{3+2i}{2}\right)\right)\left(x - \left(\frac{3-2i}{2}\right)\right)$$

$$4x^3 \dots$$

Show that

$$x^2 - x - 6 = 0$$

$$(x-3)(x+2)$$

$$x \in \{-2, 3\}$$

$$(x-(-2))(x-3)$$

$$(2x+1)(3x-5)$$

$$= 6x^2 - 7x - 5$$

$$x \in \left\{-\frac{1}{2}, \frac{5}{3}\right\}$$

$$6\left(x - \left(-\frac{1}{2}\right)\right)\left(x - \frac{5}{3}\right)$$

$$3 \cdot 2\left(x + \frac{1}{2}\right)\left(x - \frac{5}{3}\right)$$

$$\widehat{2}\left(x + \frac{1}{2}\right)\widehat{3}\left(x - \frac{5}{3}\right)$$

$$(2x+1)(3x-5)$$

Show that $2+i$ is a root of

$$f(x) = 4x^3 - 19x^2 + 32x - 15$$

We divide $f(x)$ by $x - (2+i)$

$$\begin{array}{r} 2+i \overline{) 4 - 19 + 32 - 15} \\ \underline{4 - 11 + 4i + 6 - 3i + 0} \\ \phantom{4 - 11 + 4i + 6 - 3i + 0} - 15 \neq 2 \end{array}$$

$$(2+i)(-11+4i)$$

$$= -22 + 8i - 11i + 4i^2$$

$$= -22 - 3i - 4$$

$$= -26 - 3i$$

$$(2+i)(6-3i) = 12 - 6i + 6i - 3i^2$$

$$= 12 + 3 = 15 \neq 1$$

Write $\frac{1}{2+3i}$ in standard form

$$\frac{5+7i}{2+3i}$$

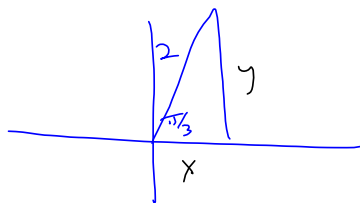
$$= \left(\frac{1}{2+3i} \right) \left(\frac{2-3i}{2-3i} \right) = \frac{2-3i}{2^2+3^2} = \frac{2}{13} - \frac{3}{13}i$$

Convert to trig form

$$1 + \sqrt{3}i$$

$$2 \left(\cos\left(\frac{\pi}{3}\right) + i \sin\left(\frac{\pi}{3}\right) \right)$$

convert to std form



$$\frac{y}{2} = \sin\frac{\pi}{3}$$

$$y = 2 \sin\frac{\pi}{3}$$

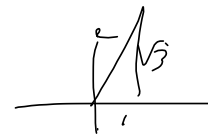
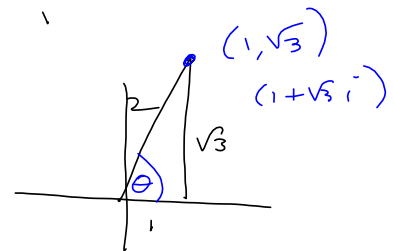
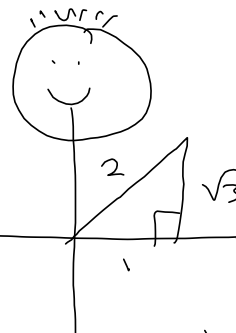
$$= 2 \cdot \frac{\sqrt{3}}{2} = \sqrt{3}$$

$$\frac{x}{2} = \cos\frac{\pi}{3}$$

$$x = 2 \cos\frac{\pi}{3}$$

$$= 2 \cdot \frac{1}{2} = 1$$

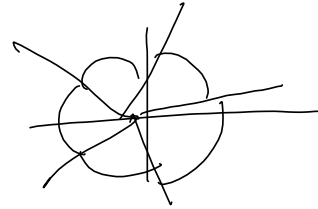
$$1 + \sqrt{3}i$$



$$z = r(\cos \theta + i \sin \theta)$$

$$z^n = r^n (\cos(n\theta) + i \sin(n\theta))$$

Find all solutions to



$$z^5 = 32$$

$$z^5 = 32 \left(\cos \frac{\pi}{3} + i \sin \frac{\pi}{3} \right)$$

$$\sqrt[5]{z^5} = \sqrt[5]{32}$$

$$\sqrt[5]{z^5} = z = \sqrt[5]{32} \left(\cos\left(\frac{\pi}{5}\right) + i \sin\left(\frac{\pi}{5}\right) \right)$$

$z = 2$ = principal 5th root.

$$\frac{2\pi}{5}$$

$$z = 2 \left(\cos\left(\frac{7\pi}{15}\right) + i \sin\left(\frac{7\pi}{15}\right) \right)$$

$$\frac{\pi}{15} + \frac{2\pi}{5} = \frac{7\pi}{15}$$

$$2 \left(\cos\left(\frac{7\pi}{15}\right) + i \sin\left(\frac{7\pi}{15}\right) \right) \left(\cos\frac{2\pi}{5} + i \sin\frac{2\pi}{5} \right)$$

$$2 \left(\cos\left(\frac{13\pi}{15}\right) + i \sin\left(\frac{13\pi}{15}\right) \right)$$

$$\frac{7\pi}{15} + \frac{6\pi}{15}$$