

$$r=16, \quad \theta = 120^\circ = \frac{2\pi}{3} \text{ radians}$$

We find all 4<sup>th</sup> roots of  $z = re^{i\theta}$

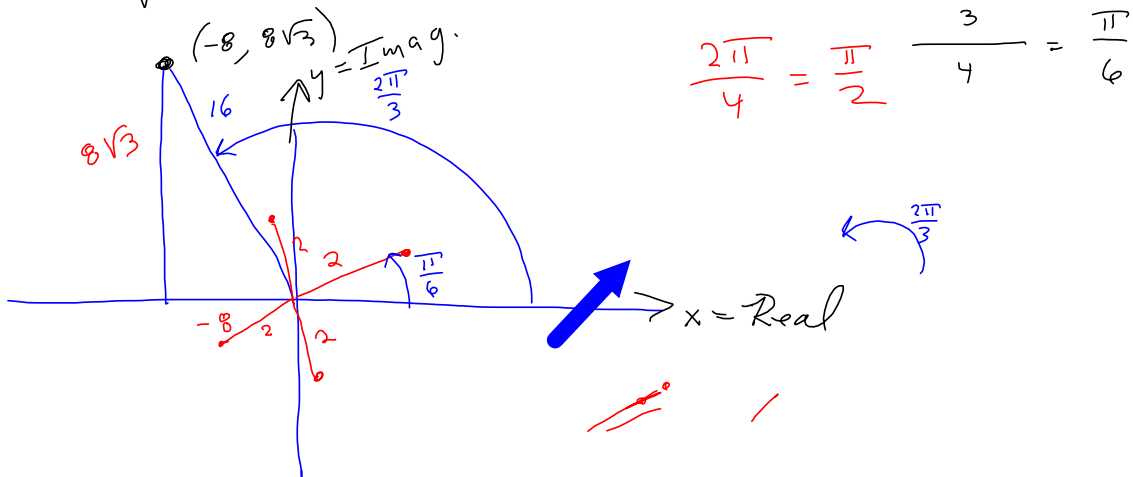
$$= r(\cos\theta + i\sin\theta)$$

We solve the equation

$$z^4 = 16(\cos(\frac{2\pi}{3}) + i\sin(\frac{2\pi}{3})) = 16(-\frac{1}{2} + i\frac{\sqrt{3}}{2})$$

One solution is immediate:  $= -8 + 8i\sqrt{3}$

$$\sqrt[4]{z^4} = \sqrt[4]{16} (\cos$$



$n^{\text{th}}$  roots of unity

$$x^n = 1$$

$$x^n - 1 = 0 \Rightarrow \text{cyclotomic polynomial}$$

$$(x-1)(x^{n-1} + x^{n-2} + \dots + x^2 + x + 1)$$

Always factors this way!

$$x^7 = 1$$

$$x^7 - 1 = 0$$

$x=1$  is a soln.

$$1 = 1 \left( \cos 0 + i \sin 0 \right) \quad 1$$

$$\text{So. } \cos\left(\frac{2\pi}{7}\right) + i \sin\left(\frac{2\pi}{7}\right) \quad 2$$

$$\cos\left(\frac{4\pi}{7}\right) + i \sin\left(\frac{4\pi}{7}\right) \quad 3$$

$$\cos\left(\frac{6\pi}{7}\right) + i \sin\left(\frac{6\pi}{7}\right) \quad 4$$

$$\cos\left(\frac{8\pi}{7}\right) + i \sin\left(\frac{8\pi}{7}\right) \quad 5$$

$$\cos\left(\frac{10\pi}{7}\right) + i \sin\left(\frac{10\pi}{7}\right) \quad 6$$

$$\cos\left(\frac{12\pi}{7}\right) + i \sin\left(\frac{12\pi}{7}\right) \quad 7$$

All the  
7<sup>th</sup> roots  
of unity!