

Find all points having an  $x$ -coordinate of 4, whose distance from the point  $(-2, -1)$  is 10.

Translation: We need to find all values of  $y$  such that the distance from  $(4, y)$  to  $(-2, -1)$  is 10.

The distance from  $(x_1, y_1) = (-2, -1)$  to  $(x_2, y_2) = (4, y)$  is given by

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \sqrt{(4 - (-2))^2 + (y - (-1))^2} = \sqrt{36 + (y + 1)^2}$$

We want this distance to be 10:

$$\sqrt{36 + (y + 1)^2} = 10$$

Now we have an equation, we see that we must solve for  $y$ . Because of the square inside, there, we expect 2 different answers for  $y$ .

Square both sides:

$$\left(\sqrt{36 + (y + 1)^2}\right)^2 = 10^2$$

$$36 + (y + 1)^2 = 100$$

Isolate the  $(y + 1)^2$ :  $(y + 1)^2 = 100 - 36 = 64$

Square Root Property:  $y + 1 = \pm\sqrt{64} = \pm 8$ , so that

$$y = -1 \pm 8$$

This gives  $y = 7$  or  $y = -9$ . So the final answer is the two points

$$(4, y) = (4, 7) \text{ or } (4, -9)$$

Let me know if this helps. I'm a bit handicapped by technology when I'm at home.