

121 § 1.1 #71

$$f(x) = \frac{x-1}{x+2}, \quad g(x) = \frac{2x-1}{x-1}$$

\mathcal{D} = Domain.

Here, we're concerned with $\mathcal{D}(f+g)$ and it's the intersection of $\mathcal{D}(f)$ with $\mathcal{D}(g)$:

$$\begin{aligned} \mathcal{D}(f) &= \{x \mid x \neq -2\} \\ \mathcal{D}(g) &= \{x \mid x \neq 1\} \end{aligned} \left. \vphantom{\begin{aligned} \mathcal{D}(f) \\ \mathcal{D}(g) \end{aligned}} \right\} \begin{array}{l} \text{Both cases, we} \\ \text{can't let the} \\ \text{denominator be} \\ \text{zero!} \end{array}$$

$$\mathcal{D}(f) = (-\infty, -2) \cup (-2, \infty)$$

$$= \leftarrow \text{---} | \text{---} \rightarrow$$

-2

$$\mathcal{D}(g) = (-\infty, 1) \cup (1, \infty)$$

$$= \leftarrow \text{---} | \text{---} \rightarrow$$

1

$$\mathcal{D}(f) \cap \mathcal{D}(g) = \leftarrow \text{---} | \text{---} | \text{---} \rightarrow$$

-2 1

$$= (-\infty, -2) \cup (-2, 1) \cup (1, \infty)$$

$$= \{x \mid x \neq -2 \text{ and } x \neq 1\}$$

Hope this helps on the domain part.

You may need Chapter P for intersections.