

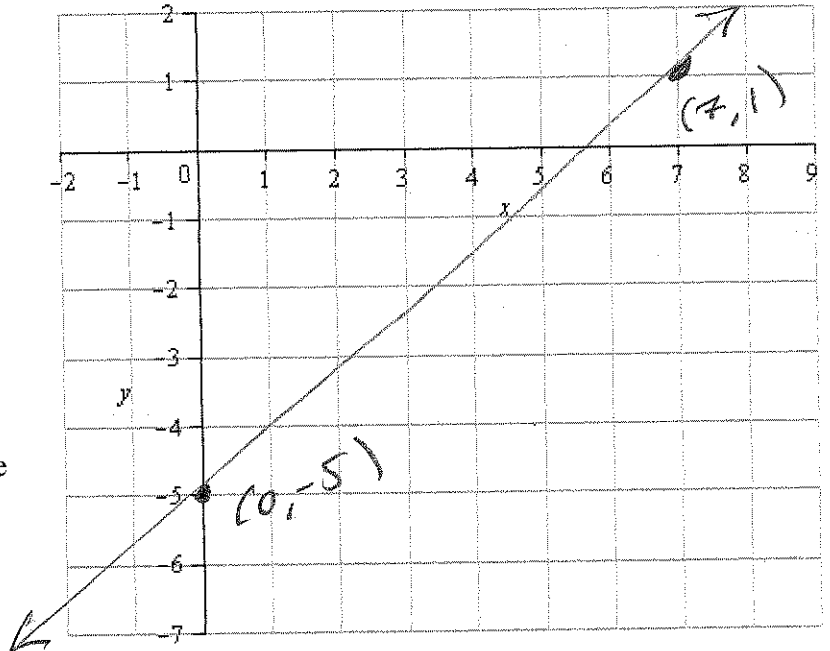
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1. Let $f(x) = \frac{6}{7}x - 5$

- a. (5 pts) Determine the slope and y-intercept of f .

$m = \frac{6}{7}, (0, b) = (0, -5)$

- b. (5 pts) Use the slope and y-intercept to graph f , in the space on the right:



- c. (5 pts) What's the average rate of change of f ?

$m = \frac{6}{7}$

2. Suppose y varies jointly as x and the square of z and inversely as the cube of w .

- a. (5 pts) Write an equation representing the relationship.

$y = \frac{k \times z^2}{w^3}$

$26 \frac{256}{64} = \frac{128}{32} = \frac{64}{16} = \frac{32}{8} = \frac{16}{4} = 4$

- b. (5 pts) Suppose $y = 24$ when $x = 2, z = 9$ and $w = 4$. What, then, is y when $x = 2, z = 3$ and $w = 4$?

$24 = \frac{k(2)(9)^2}{4^3}$
 $\frac{48}{(2)(81)} = k = \frac{256}{27}$

$y = \frac{256}{27} \left(\frac{(2)(3)^2}{4^3} \right) = \frac{4(2)}{3} = \frac{8}{3}$

3. (5 pts each) Compute the discriminant for each of the following quadratic and tell me the nature of solutions, specifically, how many distinct solutions there are and whether they're real or non-real. Do not solve the equations.

a. $3x^2 - 12x + 9 = 0$

$a = 3, b = -12, c = 9$

$b^2 - 4ac = (-12)^2 - 4(3)(9) = 144 - 108 = 36$

Two distinct, rational

b. $-5x^2 - 110x - 703 = 0$

$a = -5, b = -110, c = -703$

$b^2 - 4ac = (-110)^2 - 4(-5)(-703) = -1960$

Two nonreal solutions

4. Solve by any method, but *show all work!!!*

a. (10 pts) $84x^2 - 8x - 105 = 0$

$a = 84, b = -8, c = -105$

$b^2 - 4ac = (-8)^2 - 4(84)(-105) = 35344$

$\sqrt{b^2 - 4ac} = 188$

$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$= \frac{8 \pm 188}{2(84)} = \frac{4(2 \pm 47)}{2(84)} = \frac{2 \pm 47}{42}$

$x \in \left\{ -\frac{15}{14}, \frac{7}{6} \right\}$

Just hit 35344 with $\sqrt{\quad}$
 first thing
 2 | 35344
 2 | 17672
 2 | 8836
 2 | 4418
 47 | 2209
 47

ouch!
 tough to get w/o techs

$\frac{49}{42} = \frac{7}{6}$
 $\frac{-45}{42} = -\frac{15}{14}$

5. (5 pts) Solve $x^2 + 6x + 11 = 0$ by completing the square.

$x^2 + 6x = -11$

$x^2 + 6x + 3^2 = -11 + 9$

$(x+3)^2 = -2$

$x+3 = \pm i\sqrt{2}$

$x = -3 \pm i\sqrt{2}$

$\frac{-25}{12} - \frac{120}{12} = \frac{-145}{12}$

6. Complete the square and re-write each of the following in the form $f(x) = a(x-h)^2 + k$.

a. (5 pts) $f(x) = x^2 + 6x + 11$

$= x^2 + 6x + 3^2 - 9 + 11$

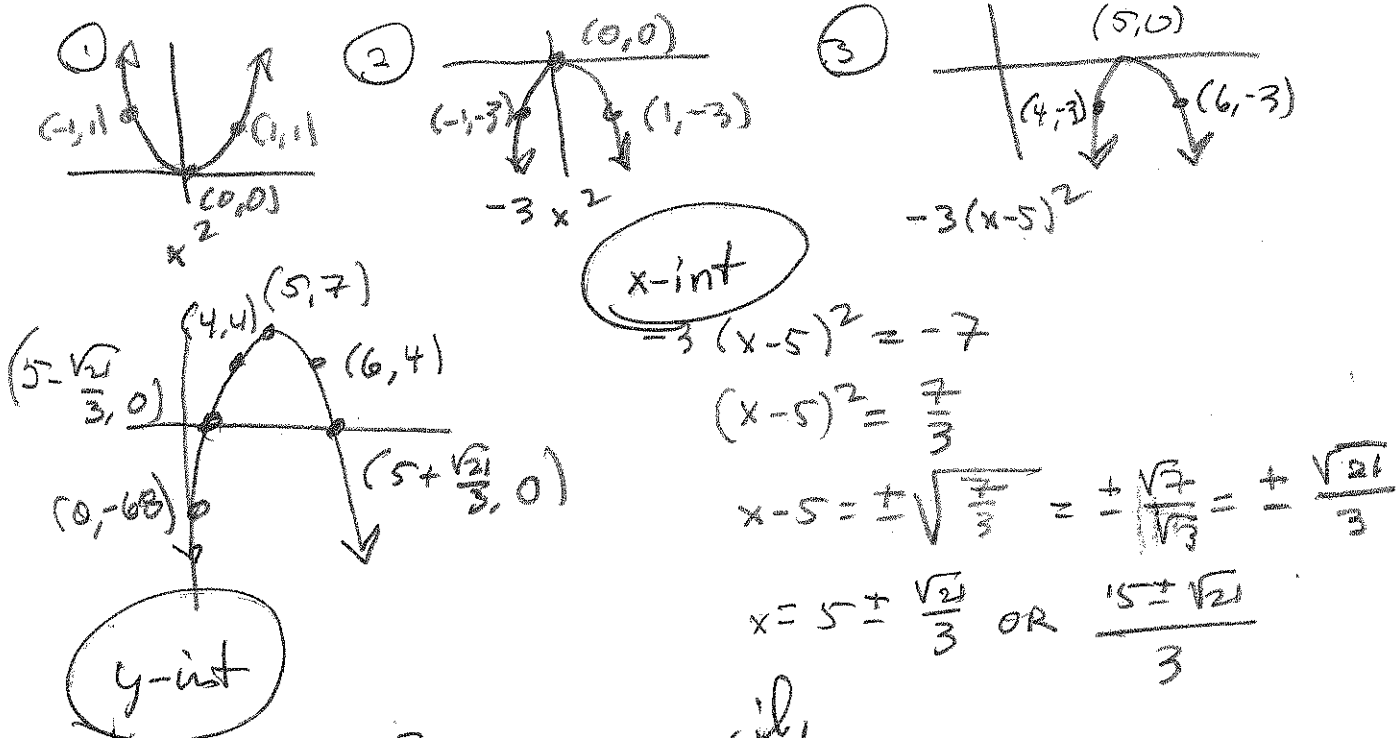
$= (x+3)^2 + 2$

b. (5 pts) $f(x) = 3x^2 - 5x - 10$

$= 3\left(x^2 - \frac{5}{3}x + \left(\frac{5}{6}\right)^2\right) - 3\left(\frac{25}{36}\right) - 10$

$= 3\left(x - \frac{5}{6}\right)^2 - \frac{145}{12}$

7. a. (10 pts) Sketch the graph of $f(x) = -3(x-5)^2 + 7$. I want to see it step-by-step, using techniques I gave you. Your first graph of the basic function should include the points $(-1,1)$, $(0,0)$, and $(1,1)$. Track where those points end up at each stage (each graph), as demonstrated in videos.



x-int

$$-3(x-5)^2 = -7$$

$$(x-5)^2 = \frac{7}{3}$$

$$x-5 = \pm \sqrt{\frac{7}{3}} = \pm \frac{\sqrt{7}}{\sqrt{3}} = \pm \frac{\sqrt{21}}{3}$$

$$x = 5 \pm \frac{\sqrt{21}}{3} \text{ OR } \frac{15 \pm \sqrt{21}}{3}$$

y-int

use pencil, Steve!

$$-3(0-5)^2 + 7$$

$$= -3(-5)^2 + 7$$

$$= -3(25) + 7 = -75 + 27 = -68$$

8. (5 pts) Based on your work on the previous, state the domain and range of $f(x)$.

$$D = \mathbb{R}, R = (-\infty, 7]$$

9. (5 pts) State intervals of increase and decrease for $f(x)$. Took it out.

Inc: $(5, \infty)$
 Dec: $(-\infty, 5)$

10. (5 pts) Find the x- and y-intercepts for $f(x)$. Indicate and label these points on the graph, above.

Decimal approximation: 1-point deduction. Simplified Radical Form For full credit.

11. (10 pts) Solve the inequality $x^2 + 14x - 9 \leq -x^2 + 5x - 4$. Give your final answer in set notation and interval notation.

$$2x^2 + 9x - 5 \leq 0$$

$$= (2x - 1)(x + 5) = 0$$

$$x = \frac{1}{2}, -5$$



want -

$$x \in \left[-5, \frac{1}{2} \right]$$

$$2\left(x^2 + \frac{9}{2}x\right) = 5$$

$$2\left(x^2 + \frac{9}{2}x + \left(\frac{9}{4}\right)^2\right) = 5 + 2\left(\frac{81}{16}\right)$$

$$2\left(x + \frac{9}{4}\right)^2 = 5 + 2\left(\frac{81}{16}\right)$$

$$\left(x + \frac{9}{4}\right)^2 = \frac{5}{2} + \frac{81}{16}$$

$$x + \frac{9}{4} = \pm \sqrt{\frac{121}{16}} = \pm \frac{11}{4}$$

$$x = \frac{-9 \pm 11}{4} \rightarrow \frac{1}{2}, -5$$



Bonus (5 pts) Solve $x^2 - 5x + 4 > 3 - x$. Give an exact final answer (simplified radical form), in set notation and interval notation.

$$x^2 - 4x + 1 > 0$$

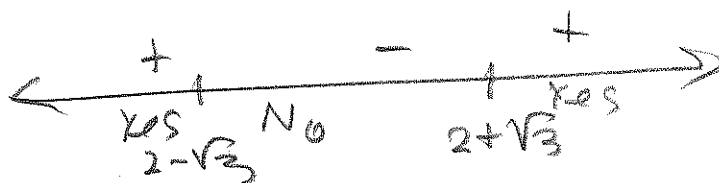
$$x^2 - 4x + 2^2 - 2^2 + 1 = 0$$

$$(x - 2)^2 - 3 = 0$$

$$(x - 2)^2 = 3$$

$$x - 2 = \pm \sqrt{3}$$

$$x = 2 \pm \sqrt{3}$$



$$x \in \left((-\infty, 2 - \sqrt{3}) \cup (2 + \sqrt{3}, \infty) \right)$$

12. Solve The absolute value inequalities. Give your answers in set-builder and interval notation.

a. (5 pts) $|4x + 7| \geq 1$

$$4x + 7 \geq 1 \text{ OR } 4x + 7 \leq -1$$

$$4x \geq -6 \text{ OR } 4x \leq -8$$

$$\left\{ x \mid x \geq -\frac{3}{2} \text{ OR } x \leq -2 \right\}$$

$$= (-\infty, -2] \cup \left[-\frac{3}{2}, \infty\right)$$

b. (5 pts) $|4x - 7| < 1$

$$4x - 7 < 1 \text{ and } 4x - 7 > -1$$

$$4x < 8 \text{ and } 4x > 6$$

$$\left\{ x \mid x < 2 \text{ and } x > \frac{3}{2} \right\}$$

$$= \left(\frac{3}{2}, 2\right)$$