100 Points

Covers Chapter 4, plus 8.3

NO GRAPHING CALCULATORS!!!

1. (20 pts) Starting with  $f(x) = 3^x$ , sketch the graph of  $g(x) = 2 \cdot 5^{x+4} - 3$  in 4 steps (counting  $f(x) = 3^x$  as the first step). Use x = -1, x = 0, and x = 1 to find 3 points in the first graph, and show how these 3 points are moved around by each step in the transformation to g(x). Your final graph should also show the *y*-intercept and, for 5 bonus points, the *x*-intercept.

- 2. Let  $f(x) = \sqrt{2x+8}$  and  $g(x) = \frac{1}{x+2}$ .
  - a. (5 pts) What is the domain of f?

b. (5 pts) What is the domain of g?

- c. (5 pts) Determine (f+g)(x). (Sometimes just called "f+g" in the text.). Do not simplify.
- d. (5 pts) What is the domain of (f + g)(x)?

- e. (5 pts) Determine  $(f \circ g)(x)$  (Again, sometimes just called  $f \circ g$ )
- f. (5 pts) What is the domain of  $(f \circ g)(x)$ ? Hint: An interval of length ½.

3. (5 pts) What is the domain of  $\sqrt{\frac{(x+3)(x-2)^2}{(x-4)^3}}$ ?

4. (5 pts) Let  $f(x) = 5^{2x-5} - 3$ . Find  $f^{-1}(x)$ .

5. Find the geometric sums:

a. 
$$(10 \text{ pts})$$
  $1+3+9+27+.....+19683$ 

b. (5 pts) 
$$\sum_{n=1}^{\infty} 2 \cdot \left(\frac{2}{3}\right)^{n-1}$$

6. (5 pts) Solve  $\log_2(x-4) + \log_2(x+3) = 3$ .

- 7. Suppose the half-life of C-14 is 5900 years. (It isn't, quite, but just suppose...).
  - a. (10 pts) Derive the exponential decay model,  $A(t) = A_0 e^{kt}$ . The trick is to use the half-life to find the relative decay rate, k.

b. (5 pts) How old is a sample of charcoal from a prehistoric fire pit, if 43% of the C-14 has decayed (i.e., 35% is left.)? Round to the nearest year in your final answer.