200 Points Comprehensive

NO GRAPHING CALCULATORS!!!

Problems out of order: 10 points off; Writing too faint: 10 points off; No margin in top left corner: 10 points off.

- 1. Solve the equation $x^2 + 3x 28 = 0$ in three different ways:
 - a. (10 pts) Factoring
 - b. (10 pts) Completing the Square
 - c. (10 pts) Quadratic Formula
- Solve the absolute value inequalities. Give your answers in set-build and interval notation.
 - a. (10 pts) |-5x-8| > 4
 - b. (10 pts) $|-5x-8| \le 4$
- 3. Let $f(x) = \sqrt{x+16}$ and $g(x) = x^2 4x 21$.
 - a. (10 pts) What is the domain of f? Give your answer in set-builder and interval notation.
 - b. (10 pts) What is the domain of g? Give your answer in set-builder and interval notation.
 - c. (5 pts) Determine $\left(\frac{f}{g}\right)(x)\left(\text{Just}\frac{f}{g},\text{for short}\right)$. Do not simplify your answer.
- **B1** (5 pts) What is the domain of $\frac{f}{g}$?
 - d. (10 pts) Determine $(f \circ g)(x)$ (Just $f \circ g$, for short). Simplify your answer.
 - e. (5. pts) What is the domain of $f \circ g$?
- 4. (10 pts) Solve $(x+3)^{15}(x-1)^4(x-5) \le 0$. Give your answer in interval notation.
- 5. (10 pts) What is the domain of $f(x) = \sqrt{(x+3)^{15}(x-1)^4(x-5)}$?
- **B 2** (5 pts) What is the domain of $g(x) = \log_{17}((x+3)^{15}(x-1)^4(x-5))$?
- 6. (10 pts) What is the domain of $g(x) = \sqrt{\frac{(x+3)^{15}(x-1)^4}{(x-5)}}$
- 7. (10 pts) Use synthetic division to find P(2), for $P(x) = 2x^5 5x^4 2x^2 + 6x 13$
- 8. (10 pts) Determine a, r, and n for the finite geometric sequence $\frac{5}{2}$, 5,10, ..., 640. Use a, r, and n to determine the *exact* value of the sum $\sum_{k=1}^{n} a \cdot r^{k-1} = a \left(\frac{1-r^{n}}{1-r} \right)$. For full credit, a fraction in lowest terms is required.

9. (10 pts) Find the sum of the infinite geometric series $\sum_{k=1}^{\infty} 2 \cdot \left(\frac{3}{7}\right)^{k-1}$

FinanceFormulas:

Finance Formulas:
$$A = P\left(1 + \frac{r}{m}\right)^{mi} = P(1+i)^{n} \qquad FV = R\left(\frac{\left(1 + \frac{r}{m}\right)^{mi} - 1}{\left(\frac{r}{m}\right)}\right) = R\left(\frac{(1+i)^{n} - 1}{i}\right)$$

- 10. (10 pts) What is the future value, in 10 years, of \$5,000 deposited at 5% annual percentage rate, compounded weekly? (Recall, there are 52 weeks in a year.).
- Answer ONE of the following:
 - a. (10 pts) If your monthly loan payments are \$958.00, and the loan is for 15 years, how much did you borrow in the first place, if you're paying 4.5% annual percentage rate, compounded monthly?
 - to the nearest year will it take for 100 grams of Niobium-94 to decay to 13 grams, if its half-life is 20,300 years?
- 12. Let $g(x) = -2 \cdot \sqrt{-5x + 40} + 7$.
 - a. (20 pts) Start with the graph of $f(x) = \sqrt{x}$, and proceed to the graph of g(x) with 4 more graphs, demonstrating each of the 4 basic transformations. So, 5 graphs, in all, counting the graph of f(x) as the first. Label the 3 points, (0,0), (1,1), and (4,2) in the graph of f(x), and track where they end up after each transformation. Each transformation leaves one coordinate fixed and changes one in a very particular way. Your job is to understand which coordinate, and how it's affected by the transformation.
 - b. (5 pts) Find the x-intercept of the graph of g(x), above. Report it as an ordered pair, A, in your answer, and label it as A on the final graph from part a. For full credit, use fractions in lowest terms for the coordinates.
 - c. (5 pts) Find the y-intercept of the graph of g(x), above. Report it as an ordered pair, B, in your answer, and label it as B on the final graph from part a. For full credit, use a radical expression, in lowest terms.

Bonus Answer up to 20 points' worth.

B3 (5 pts) Let
$$f(x) = -\ln(5x+4) - 9$$
. Find $f^{-1}(x)$.

B4 (5 pts) Use the Binomial Theorem (Pascal's Triangle!) to expand $(2x-3y)^5$.

$$x + y + z = 4$$

y - z = 4**B** 5 (10 pts) Solve the system of linear equations:

- -3x + 2y 7z = 7
- B6 (5 pts) John can finish a job in 10 hours that it takes Bill only 7 hours to finish. Suppose Bill shows up and starts working 3 hours before John shows up, and then they work together until the job is done. How many hours does each of the two end up working? For full credit, I expect a fraction, in lowest terms for each person's time. $3x + 5y \le 30$

$$5x - 2y \le 10$$

B 7 (5 pts) Sketch the following system of inequalities:

$$x \ge 0$$