MAT 1340 70 points

2.7 – Combining Functions

2.8 – 1-to-1 Functions and their Inverses

Refer to 2.7 Notes and Videos and 2.8 Notes and Videos on harryzaims.com. When you finish WebAssign for 2.7, you're ready for #s 1 - 5. When you've finished WebAssign for 2.8, you're ready for the rest.

1. (5 pts) From the graphs of f and g in the figure, find the folloing:

a.
$$(f+g)(0)$$

- b. (f-g)(0)
- c. (fg)(0)
- d. $\left(\frac{f}{g}\right)(0)$
- e. $(f \circ g)(0) = f(g(0))$
- 2. (5 pts) If f(x) and g(x) are real functions, what is the domain of $f \circ g$? If you can, write it as a set in set-builder notation:

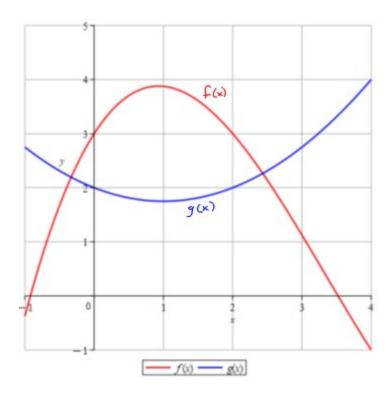
 $D(f \circ g) = \{x | x \text{ satisfies conditions}\}$. You need to supply the conditions on *x*.

3. Find the domain of each of the following:

a. (5 pts)
$$f(x) = \sqrt{x} + \sqrt{49 - x^2}$$

b. (5 pts)
$$f(x) = \frac{\sqrt{x}}{\sqrt{49 - x^2}}$$

- 4. Find f + g, fg, f/g, and $f \circ g$ for $f(x) = \sqrt{x}$ and $g(x) = x^2 3x + 2$, Find the domain of each.
 - a. (5 pts) f + g
 - b. (5 pts) fg
 - c. (5 pts) f/g



d. (5 pts) $f \circ g$

5. (5 pts) Let $f(x) = \sqrt{x}$, $g(x) = \frac{x}{x-4}$, and $h(x) = \sqrt[6]{x}$. Find $f \circ g \circ h$.

Bonus (5 pts) What is the domain of your answer to #5?

6. (5 pts) Define what is meant by "*f* is a function" and define what is meant by "*f* is a 1-to-1 function."

7. (5 pts) If
$$f(x) = \frac{14}{x}$$
, what's $f^{-1}(2)$?

- 8. $f(x) = x^2 + 10x 24$ has domain $D(f) = \{x \mid x \text{ is real}\} = (-\infty, \infty)$, because *f* is a polynomial. *f* is not 1-to-1, because $y_1 = f(-6) = f(-4) = y_2 = -48$, and the fact that $x_1 = -6 \neq -4 = x_2$. On WebAssign, Section 2.8 #19 restricts the domain to $D = \{x \mid x \ge -5\} = [-5, \infty)$. (Your version of 2.8 #19 may vary.)
 - a. (5 pts) Show how making $D = [-5, \infty)$ fixes the 1-to-1 problem for *f*, by sketching the graph of *f* on its restricted domain. Label the left endpoint of the graph. Say a few words about how it passes the visual test for being 1-to-1. What's the *range* of this restricted version of *f*?
 - b. (5 pts) Prove that f is not 1-to-1 algebraically. No, wait. I've already done that. I found two values of x that had the same f(x) by going one step to the right and left of the x-value of its vertex, which, since I can complete the square, I know is -b/2 = -10/2 = -5, just by looking at the +10x in the middle. In general, just solve the equation f(x) = c, for any c that will give you more than one solution. Typically, people will solve f(x) = 0, if they can, and it gives 2 solutions.
 - c. (5 pts) Find $f^{-1}(x)$. Sketch its graph. Label the lowest point on the graph. Then add a sketch of the line y = x to the graph. Finally, add the sketch of f that you did in **part a** to the graph.

Bonus (5 pts) It's just as valid to restrict the domain to $D = (-\infty, -5]$. That would yield a different $f^{-1}(x)$. What would it be? Support your answer.

Bonus (5 pts) Sketch the graph of f, restricted to the domain from the previous bonus question. Sketch the graph of *its* inverse. Label the endpoint of each of the graphs. Also find and label the *x*-and *y*-intercepts of both. State the domain and range of each.

9. Let
$$f(x) = \frac{x-1}{x+4}$$
.

- a. (5 pts) Find $f^{-1}(x)$.
- b. (5 pts) State the domain and range of both f and f^{-1} . There's a trick that allows you to just find 2 domains for this question.