

MAT 1340

Writing Project #0, Spring 2024

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1. Simplify $5 - 2(3x - 5) + 7(2 - 3x)$

There is at least one error in these solutions.

$$5 - 2(3x - 5) + 7(2 - 3x)$$

$$= 5 - 6x + 10 + 14 - 21x$$

$$= \boxed{-27x + 29}$$

2. Multiply

a. $3(2x^2)(2x + 3)(6x - 2)$

$$3(2x^2)(2x+3)(6x-2)$$

$$= (6x^2)(12x^2 - 4x + 18x - 6)$$

$$= 6x^2(12x^2 + 14x - 6)$$

$$= \boxed{72x^4 + 84x^3 - 36x^2}$$

b. $(3x - 2)(2x^2 - 3x + 7)$

$$= 6x^3 - 9x^2 + 21x - 4x^2 + 6x - 14$$

$$= \boxed{6x^3 - 13x^2 + 27x - 14}$$

$$\begin{array}{r} 12 \\ -11 \\ \hline 1 \\ -12 \\ \hline -11 \\ 12 \\ \hline 1 \end{array}$$

$$\begin{array}{r} -132 \\ +49 \\ \hline -83 \end{array}$$

3. Evaluate $b^2 - 4ac$ if $a = 3, b = -7,$ and $c = 11$

$$b^2 - 4ac = 7^2 - 4(3)(11) = 49 - 132 = \boxed{-83}$$

I'll ding you for
 $-7^2 - 4(3)(11)$

This is fine!
 $(-7)^2 - 4(3)(11)$

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4. Write $\frac{2310}{660}$ in lowest terms.

$$\frac{2310}{660} = \frac{2 \cdot 3 \cdot 5 \cdot 7 \cdot 11}{2^2 \cdot 3 \cdot 5 \cdot 11} = \boxed{\frac{7}{2}}$$

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31

$$\begin{array}{r} 2 \overline{) 2310} \\ \underline{4620} \\ 3 \overline{) 1155} \\ \underline{3465} \\ 5 \overline{) 385} \\ \underline{770} \\ 7 \overline{) 110} \\ \underline{770} \\ 11 \end{array}$$

$$\begin{array}{r} 2 \overline{) 660} \\ \underline{330} \\ 2 \overline{) 330} \\ \underline{165} \\ 3 \overline{) 165} \\ \underline{55} \\ 5 \overline{) 55} \\ \underline{55} \\ 11 \end{array}$$

$$\frac{2310}{660} = 115$$

5. Simplify $\sqrt{37800}$ without using a calculator.

$$\begin{aligned} &= \sqrt{2^3 \cdot 3^3 \cdot 5^2 \cdot 7} \\ &= \sqrt{2^2 \cdot 2 \cdot 3^2 \cdot 3 \cdot 5^2 \cdot 7} \\ &= 2 \cdot 3 \cdot 5 \sqrt{2 \cdot 3 \cdot 7} \\ &= \boxed{30\sqrt{42}} \end{aligned}$$

$$\begin{array}{r} 2 \overline{) 37800} \\ \underline{75600} \\ 2 \overline{) 18900} \\ \underline{37800} \\ 2 \overline{) 9450} \\ \underline{18900} \\ 3 \overline{) 4925} \\ \underline{14775} \\ 3 \overline{) 1575} \\ \underline{525} \\ 3 \overline{) 525} \\ \underline{175} \\ 5 \overline{) 175} \\ \underline{35} \\ 5 \overline{) 35} \\ \underline{35} \\ 7 \end{array}$$

6. Factor, if possible:

a. $x^2 - 3x - 10$

$-10 = (-5)(2)$ and $-5 + 2 = -3$ ✓

$$\begin{aligned} &= x^2 - 5x + 2x - 10 \\ &= x(x-5) + 2(x-5) \\ &= \boxed{(x-5)(x+2)} \end{aligned}$$

6. Factor, if possible:

b. $9x^2 - 16 = 3^2x^2 - 4^2 = (3x)^2 - 4^2$

$$\begin{aligned} &= \boxed{(3x-4)(3x+4)} \\ &2^2 - b^2 = (2-a)(2+b) \end{aligned}$$

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7. Simplify. Assume all variables represent nonzero real numbers. Your final answer should contain only positive exponents.

$$a. (a^2b^{-3})(a^{-5}b^2) = a^{2-5} b^{-3+2} = a^{-3}b^{-1} = \boxed{\frac{1}{a^3b}}$$

$$b. (a^2b^{-3})^{-2}(a^{-5}b^2)^4$$

$$= (a^{\overbrace{2}^{-2}}b^{\overbrace{-3}^{-2}})^{-2}(a^{-5}b^2)^4$$

$$= (a^{2(-2)}b^{-3(-2)})(a^{-5(4)}b^{2(4)})$$

$$= (a^{-4}b^6)(a^{-20}b^8) = a^{-4-20}b^{6+8} = \boxed{\frac{b^{14}}{a^{24}}}$$

$$c. \frac{3^4x^5y^{-2}}{9x^{-3}y^{-7}} = \frac{3^4x^{5-(-3)}y^{-2-(-7)}}{3^2} = 3^{4-2}x^8y^{-2+7} = \boxed{3^2x^8y^5}$$

$$= 9x^8y^5 \text{ either one.}$$

$$d. \frac{(6x^2y^3)^{-2}}{(15x^{-2}y^{-5})^4} = \frac{6^{-2}x^{-4}y^{-6}}{15^4x^{-8}y^{-20}} = \frac{1}{6^2 \cdot 15^4} \cdot x^{-4+8}y^{-6+20}$$

$$= \boxed{\frac{x^4y^{14}}{1822500}}$$

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8. Consider the equation $ax^2 + bx + c = 0$. Write the discriminant.

Discriminant is $b^2 - 4ac$ = what goes under the radical in the quadratic formula.

$$B1 \quad ax^2 + bx + c = 0 \rightarrow \boxed{x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}}$$

$$B2 \quad 168x^2 + 326x - 165 = 0$$

$$(-165)(168) = -27720 = \text{Magic \#}$$

$$326 = 327 - 1 \quad -327 \quad \text{Higher!}$$

$$= 336 - 10 \quad -3360 \quad \text{Higher!}$$

$$= 426 - 100 \quad -42600 \quad \text{Lower!}$$

$$= 376 - 50 \quad -1880 \quad \text{Higher!}$$

$$= 401 - 75 \quad -30075 \quad \text{Lower!}$$

$$= 386 - 60 \quad -23160 \quad \text{HIGHER}$$

$$= 396 - 70 \quad -27720! \quad \text{MAGIC!}$$

$$\Rightarrow 168x^2 + 326x - 165 = 168x^2 + 396x - 70x - 165$$

$$168 = 2^3 \cdot 3 \cdot 7 \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{GCF} = 2^2 \cdot 3 = 12$$

$$396 = 2^2 \cdot 3^2 \cdot 11$$

$$165 = 3 \cdot 5 \cdot 11 \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{GCF} = 5$$

$$70 = 2 \cdot 5 \cdot 7$$

$$\Rightarrow 12(14x + 33) - 5(14x + 33) = \boxed{(14x + 33)(12x - 5)}$$

There's also the sledgehammer method using Quadratic Formula & reverse-engineering the factored form.

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$$B3 \quad x^3 - 64 = x^3 - 4^3 = \boxed{(x-4)(x^2 + 4x + 16)}$$

Difference of cubes

$$\begin{aligned}
 B4 \quad & 27x^6 + 125y^6z^9 \\
 &= 3^3(x^2)^3 + 5^3(y^2)^3(z^3)^3 \\
 &= (3x^2)^3 + (5y^2z^3)^3 \quad \text{Sum of Cubes} \\
 &= (3x^2 + 5y^2z^3)(3x^2)^2 - (3x^2)(5y^2z^3) + (5y^2z^3)^2 \\
 &= \boxed{(3x^2 + 5y^2z^3)(9x^4 - 15x^2y^2z^3 + 25y^4z^6)}
 \end{aligned}$$

$$B5 \quad 9x^2 + 16y^2 \quad \boxed{\text{DOES NOT FACTOR}^*} \quad \text{Sum of Squares}$$

$$\begin{aligned}
 B6 \quad & 9x^2 - 16y^2z^7 = \quad \text{DIFFERENCE OF SQUARES.} \\
 &= 3^2x^2 - 4^2y^2(z^7)^2 \\
 &= (3x)^2 - (4yz^7)^2 \\
 &= (3x - 4yz^7)(3x + 4yz^7)
 \end{aligned}$$

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$B7 \quad x^2 - 4x + 1 = 0$
SLEDGEHAMMER
FIND ZEROS
REVERSE-ENGINEER

$$x^2 - 4x = -1$$

$$x^2 - 4x + 2^2 = -1 + 4$$

$$(x-2)^2 = 3$$

$$x-2 = \pm\sqrt{3}$$

$$x = 2 \pm \sqrt{3}$$

$$\rightarrow x^2 - 4x + 1 = (x - (2 + \sqrt{3}))(x - (2 - \sqrt{3}))$$

*B5 you can make #5 factor by force!

$$9x^2 + 16y^2 = 9x^2 - (-16y^2)$$

$$= 9x^2 - (i^2 \cdot 16y^2)$$

$$= 3^2x^2 - 4^2y^2i^2$$

$$= (3x)^2 - (4iy)^2$$

$$= (3x - 4iy)(3x + 4iy) \quad |$$

But you need complex #s to do it!