

121 S1.7 #s 1-17, 19, 22, 23, 26, 27, 34, 35, 38, 39, 41, 45, 47, 50, 53,  
56, 60, 62, 63, 67, 74, 77, 79, 81, 84, 91, 93

#5 7-14 write an SET for the interval or an interval for the inequality (which I turn into a set)

⑦  $(-\infty, 12) = \{x \mid x < 12\}$     ⑪  $\{x \mid x \geq -8\} = [-8, \infty)$

⑧  $(-\infty, -3] = \{x \mid x \leq -3\}$       ⑫  $\{x \mid x < 54\} = (-\infty, 54)$

(9)  $[-7, \infty) = \{x \mid x \geq -7\}$       (13)  $\{x \mid x < \frac{\pi}{2}\} = (-\infty, \frac{\pi}{2})$

(10)  $(1.2, \infty) = \{x \mid x > 1.2\}$       (14)  $\{x \mid x \geq \sqrt{3}\} = [\sqrt{3}, \infty)$

Book confuses a condition on a set with the set itself. Intervals are COLLECTIONS OR SETS, not just a condition/requirement for membership.

$[-\infty, -3]$   $\neq x \leq -3$   $\therefore$  incorrect. To use an equals sign, two both must be sets.

$(-\infty, -3] = \{x \mid x \leq -3\}$  = The set of all  $x$ , where  $x$  is less than or equal to negative 3.

#5 15-26 Write the solution set using interval notation and graph it.

15  $3x - 6 < 9$

$3x < 15$

$$x < \frac{5}{3} = 5$$

$$\{x \mid x < 5\} = (-\infty, 5) = \leftarrow \overleftrightarrow{\hspace{1cm}} \underset{5}{|}$$

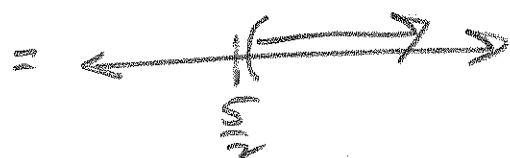
12) 51.7

(16)  $2x + 1 < 6$

$2x < 5$

$x < \frac{5}{2}$

$\{x \mid x < \frac{5}{2}\} = (\frac{5}{2}, \infty)$

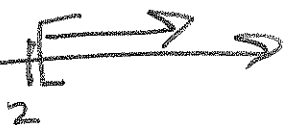


(17)  $7 - 5x \leq -3$

$-5x \leq -10$

$x \geq \frac{-10}{-5} = 2$

$\{x \mid x \geq 2\} = [2, \infty)$



The number line graphs are the usual, but the set notation and interval notation are how we typically represent these sets of numbers. You might use a number line to see it, but I don't ask for such graphs on tests.

(19)  $\frac{1}{2}x - 4 < \frac{1}{3}x + 5$

$LCD = 2 \cdot 3 = 6$

$\frac{3}{3} \cdot \frac{x}{2} - \frac{4}{1} \cdot \frac{6}{6} < \frac{2}{2} \cdot \frac{x}{3} + \frac{5}{1} \cdot \frac{6}{6}$

$\frac{3x - 24}{LCD} < \frac{2x + 30}{LCD}$

$3x - 24 < 2x + 30$

$x < 54$

Right Now the LCD is all constants. When we stick variables in the denominator, we won't be able to throw away the LCD.

$\{x \mid x < 54\} = (-\infty, 54)$



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(22)  $\frac{5-x}{3} \leq -2$

$5-x \leq -6$

$-x \leq -11$

$x \geq 11$

$\{x | x \geq 11\} = [11, \infty)$



(23)  $-\frac{2x-3}{-5} \geq 0$

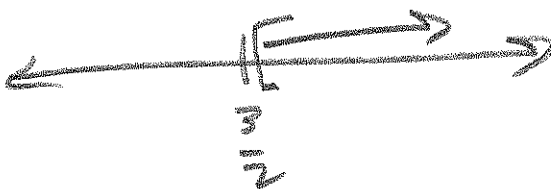
$-5\left(\frac{2x-3}{-5}\right) \leq -5(0)$  optional step.

$2x-3 \leq 0$

$2x \leq 3$

$x \leq \frac{3}{2}$

$\{x | x \leq \frac{3}{2}\} = \left[\frac{3}{2}, \infty\right)$



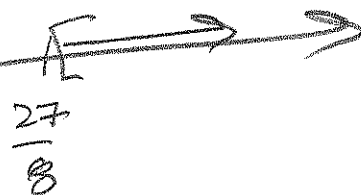
(26)  $-5x \leq 3(x-9)$

$-5x \leq 3x-27$

$-8x \leq -27$

$x \geq \frac{-27}{-8} = \frac{27}{8}$

$\{x | x \geq \frac{27}{8}\} = \left[\frac{27}{8}, \infty\right)$



What's wrong with this?

(1)  $\frac{5-x}{3} \leq -2$

(2)  $5-x \leq -6$

FALSE (3)  $\frac{-x \leq -11}{-1} \frac{-11}{-1}$

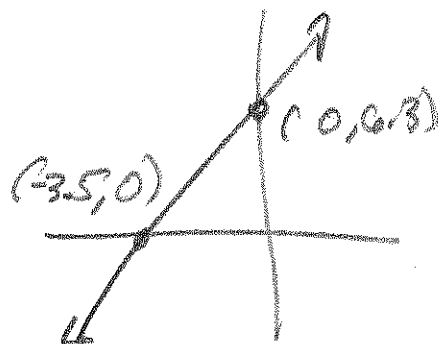
FALSE (4)  $x \geq 11$

What's wrong is that #3 doesn't follow from #2, and #4 doesn't follow from #3! Two lies in a search for truth?!

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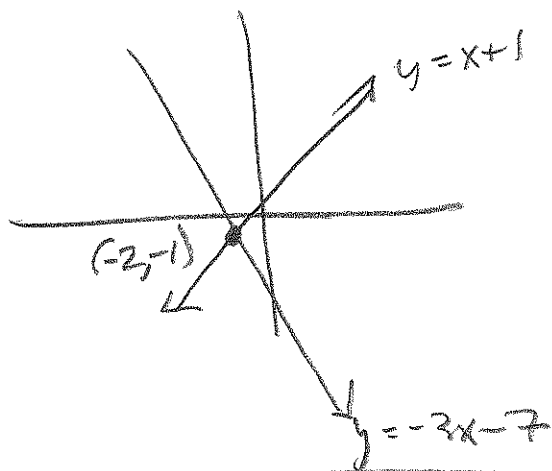
#527-38 Solve each inequality by reading the graph.

(27)  $1.8x + 6.3 < 0$



$$\{x \mid x < -3.5\} = (-\infty, -3.5)$$

(34)  $x + 1 > -3x - 7$



Looking for where

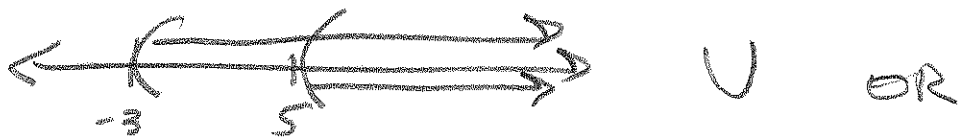
$y = x + 1$  is above  $y = -3x - 7$

$$\{x \mid x > -2\} = (-2, \infty)$$

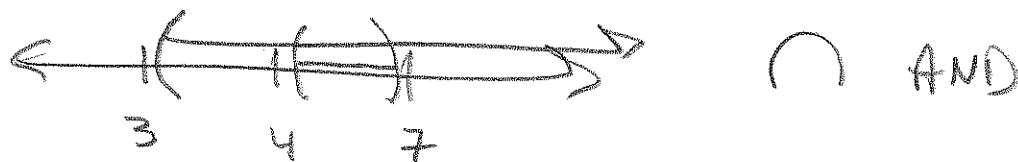
#181.7

#35-44 Write as a single interval

(35)  $(-3, \infty) \cup (5, \infty) = (-3, \infty)$



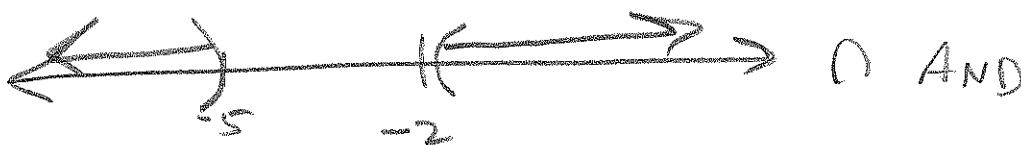
(38)  $(4, 7) \cap (3, \infty) = (4, 7)$



(39)  $(-\infty, -2) \cap (-5, \infty) = (-5, -2)$



(41)  $(-\infty, -5) \cap (-2, \infty) = \emptyset$



No number  
that's both  
less than -5  
and greater than -2

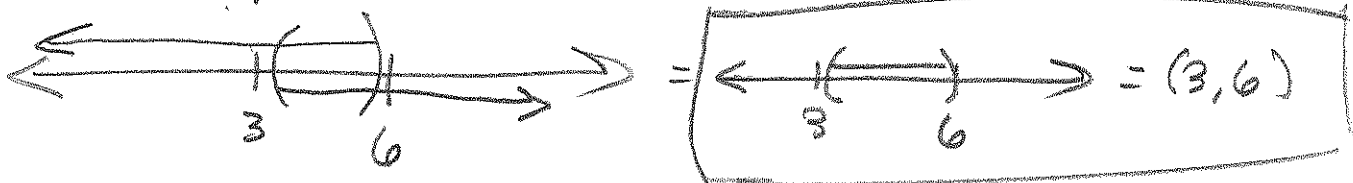
#45-58 Solve the compound inequalities. Answers in interval notation and graph.

INTERVALS REPORT  
GRAPH TO FIGURE OUT INTERVALS

(45)  $5 > 8 - x$  and  $1 + 5x < 4$

$-3 > -x$  and  $-5x < 3$

$3 < x$  AND  $x < 6$



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(47)  $\frac{2x-5}{-2} < 2$  and  $\frac{2x+1}{3} > 0$

$2x-5 > -4$

$2x > 1$

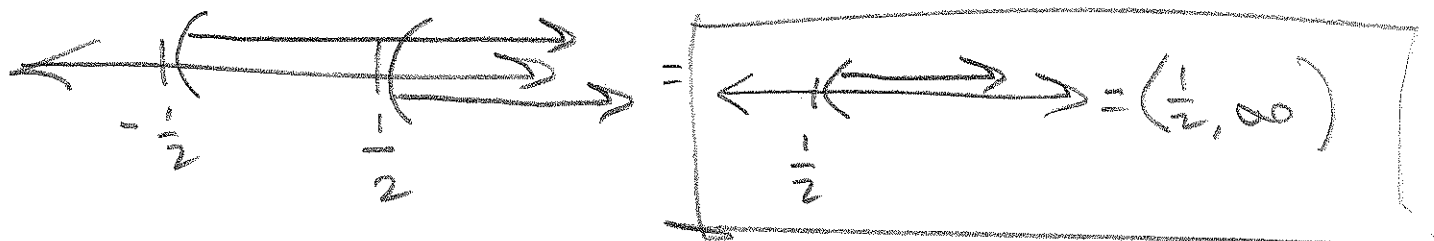
$x > \frac{1}{2}$

AND

$2x+1 > 0$

$2x > -1$

$x > -\frac{1}{2}$



(50)  $5+x > 3-x$  OR  $2x-3 > x$

$2x > -2$

$x > -1$

OR

$x > 3$



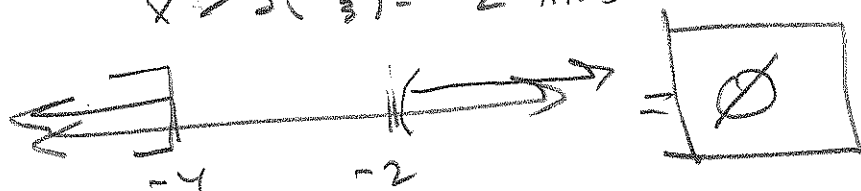
(53)  $1 - \frac{3}{2}x < 4$  and  $\frac{1}{4}x - 2 \leq -3$

$-\frac{3}{2}x < 3$

$\frac{1}{4}x \leq -1$

$x > 3(-\frac{2}{3}) = -2$  AND

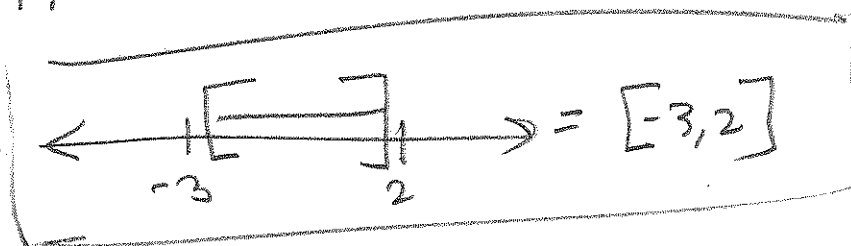
$x \leq -1(\frac{4}{1}) = -4$



(56)  $-3 \leq 4x + 9 \leq 17$

$-12 \leq 4x \leq 8$

$-3 \leq x \leq 2$



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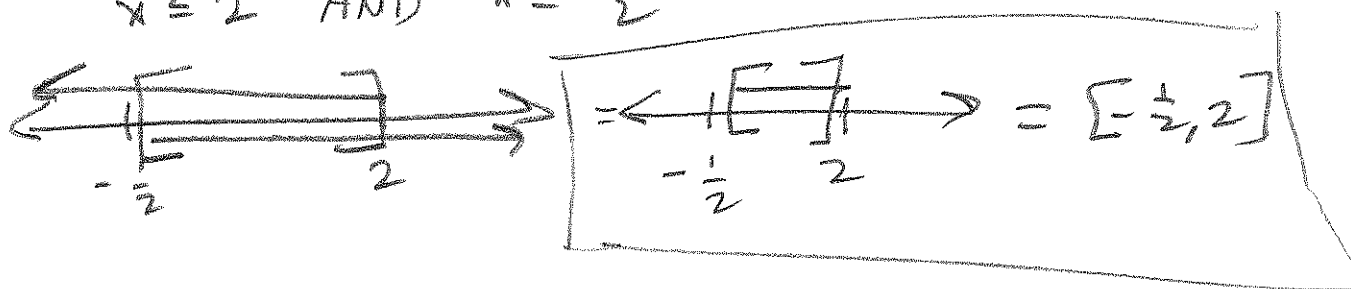
#559-76 Solve each absolute value inequality.  
Write solution set w/ interval & graph!

(60)  $|4x-3| \leq 5$

$$4x-3 \leq 5 \text{ AND } 4x-3 \geq -5$$

$$4x \leq 8 \quad 4x \geq -2$$

$$x \leq 2 \text{ AND } x \geq -\frac{1}{2}$$



(62) Note  $|6-x| = |-1(x-6)| = |-1||x-6| = 1|x-6| = |x-6|$

$$|6-x| < 6$$

$$|x-6| < 6$$

$$6-x < 6 \text{ and } 6-x > -6$$

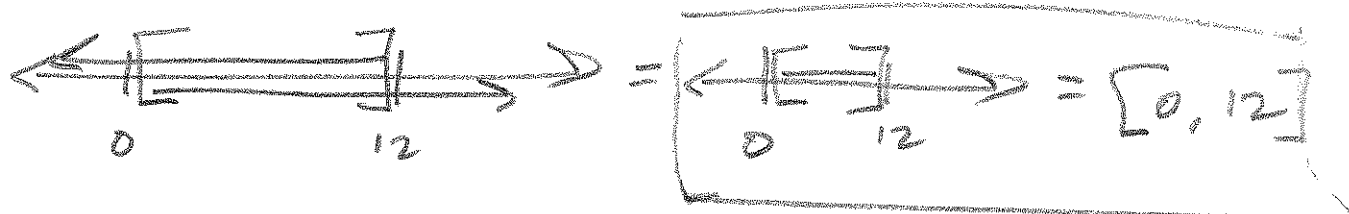
$$x-6 < 6 \text{ AND } x-6 > -6$$

$$-x < 0 \quad -x > -12$$

$$x < 12 \text{ AND } x > 0$$

$$x > 0 \text{ AND } x < 12$$

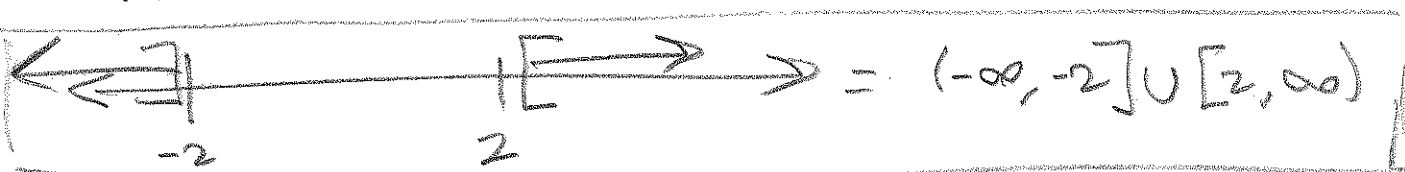
See? Same!



(63)  $|x-1| \geq 1$

$$x-1 \geq 1 \text{ OR } x-1 \leq -1$$

$$x \geq 2 \text{ OR } x \leq -2$$



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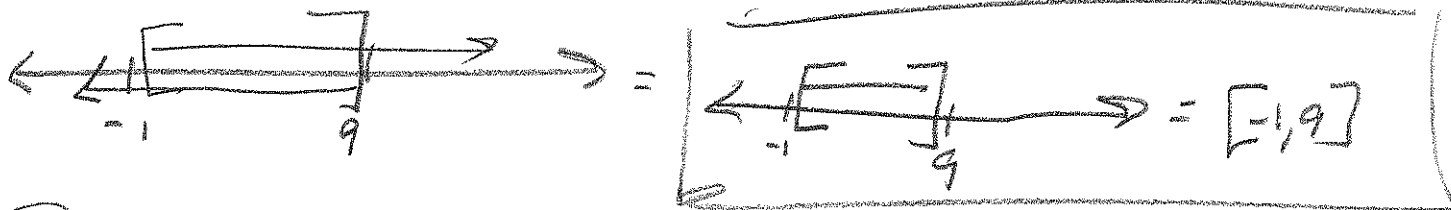
(67)  $5 \geq |4-x|$

$|4-x| \leq 5$  like  $|x|$  on left

$|x-4| \leq 5$  easier

$x-4 \leq 5$  and  $x-4 \geq -5$

$x \leq 9$  and  $x \geq -1$



(74)  $3|x-1| + 2 < 8$

$3|x-1| < 6$

$|x-1| < 2$

$x-1 < 2$  AND  $x-1 > -2$

$x < 3$  AND  $x > -1$



#S 77-84 Write an inequality of the form

$|x-a| < k$  or  $|x-a| > k$

(77)  $(-5, 5)$  Mid:  $\frac{-5+5}{2} = 0$

$|x-0| < 5$  Radius:  $\frac{5-(-5)}{2} = \frac{10}{2} = 5$

or just  $|x| < 5$



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(79)  $(-\infty, -3) \cup (3, \infty)$

MID:  $\frac{-3+3}{2} = 0$

$|x-0| > 3$

Radius:  $\frac{3-(-3)}{2} = \frac{6}{2} = 3$

or  $|x| > 3$

(81)  $(4, 8)$

MID:  $\frac{4+8}{2} = 6$

$|x-6| < 2$

Radius =  $\frac{8-4}{2} = 2$

(84)  $(-\infty, -1) \cup (5, \infty)$

MID:  $\frac{5+(-1)}{2} = 2$

$|x-2| > 3$

Radius:  $\frac{5-(-1)}{2} = 3$

#S 91-96 For what values of  $x$  is each of the following expressions a real number?

(91)  $\sqrt{x-2}$

Need  $x-2 \geq 0$

$\{x | x \geq 2\}$

(93)  $\frac{1}{\sqrt{2-x}}$

Need  $2-x \geq 0$  }  $2-x > 0$

and  $\sqrt{2-x} \neq 0$  }  $-x > -2$

$\{x | x < 2\}$