

This Project is due Friday, April 27th. Neatness, Completeness and Margins count. Show all work.

Face-to-Face Students: This Writing Project is due by the end of class, Friday, April 27th.

Online Students: If you can do a quality scan to a single, multi-page PDF, you may submit your work by e-mail *in the Course Shell*. Use the E-Mail link in the Main Navbar, and attach it to a message to Harry Mills. I'm not accepting submissions to my steve.mills@aims.edu account.

Online Students may also drop their work by my office EDBH 134K. I'd be pleased to meet you, or just slide it under my door. If you *can't* scan to PDF or deliver in-person, then you may send it by regular U.S. Mail, to the following address:

Harry Mills
EDBH 134K
Aims Community College
5401 West 20th Street
Greeley, CO 80634

As long as it's postmarked by April 27th, I will accept it, even though I probably won't get it until the following week.

1. Solve the system of linear equations $\begin{cases} 3x - y = 6 \\ 2x + y = 8 \end{cases}$ in 3 ways:

- (10 pts) Find the general vicinity of the solution by graphing the system. This should at least give you a general idea. Don't worry about it being super-accurate. Just graph the two lines by the intercept method. Supply the exact answer after you work parts b and c, below. Resist the temptation to use tickmarks on the horizontal and vertical axes.
- (10 pts) Use the Substitution Method
- (10 pts) Use the Elimination Method.

2. (10 pts) Use Elimination to solve the independent system of linear equations:

$$\begin{cases} 3x + 7y - z = -6 \\ x + 2y = -1 \\ 4x + 10y - 3z = -11 \end{cases}$$

3. Solve the dependent system of linear equations:

$$\begin{cases} x + 3y - 2z = 12 \\ 3x + 11y - 5z = 34 \\ 2x + 8y - 3z = 22 \end{cases}$$

- (10 pts) Give the general solution. Be kind to your teacher and let z be free! That means, find an expression for x and y in terms of the variable z .
- (10 pts) Give the particular solutions corresponding to $z = 0$, $z = 1$ and $z = -1$.

4. **The Underlying Assumption:** *All* of the techniques we learn for solving systems of linear equations are based on the *assumption* that the systems *have* solutions. So when we arrive at a false (*absurd!*) statement after a few elimination steps, the only explanation is that there was no solution in the first place*. Our incorrect assumption* led to something absurd, like $0 = 10$ or $0 = -5$.

*... or you made a mechanical error and should check your work, just to make sure. Stay organized and always check your work.

Higher Learning: In higher mathematics, this is the most basic method of proving something is false: "Assume it's true and conclude something absurd (like ' $0 = 1$ ')." It's important that you realize what's happening when you arrive at those absurdities at the end of a perfectly logical and legal sequence of moves. That said, let me *finally* get to the question:

$$x + 3y - 2z = 12$$

(10 pts) **Your Task:** Show that the dependent system of linear equations $3x + 11y - 5z = 34$

$$2x + 8y - 3z = 23$$

has no solution. I expect to see the word "absurd" in your discussion.