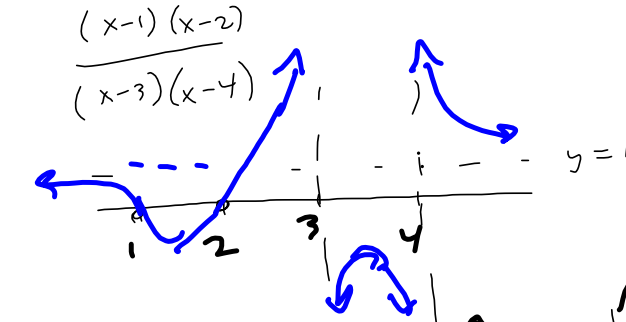
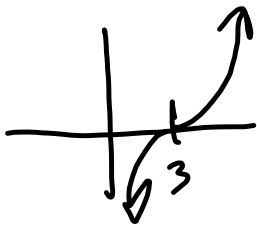


≠ 8ish

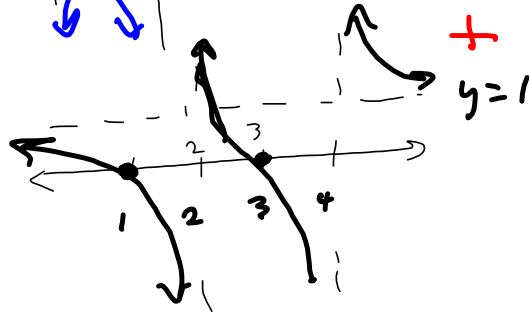
$\frac{x^2}{x^2} = 1 = y$

$x^2 = 4x + 3$   
 $x^2 - 4x + 3$

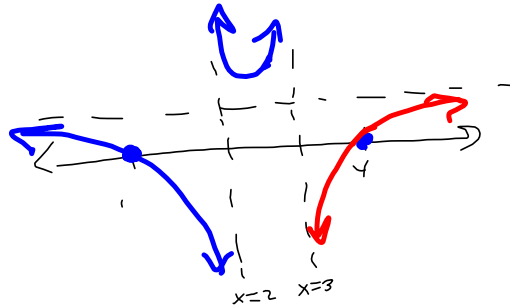
$(x-3)^3$



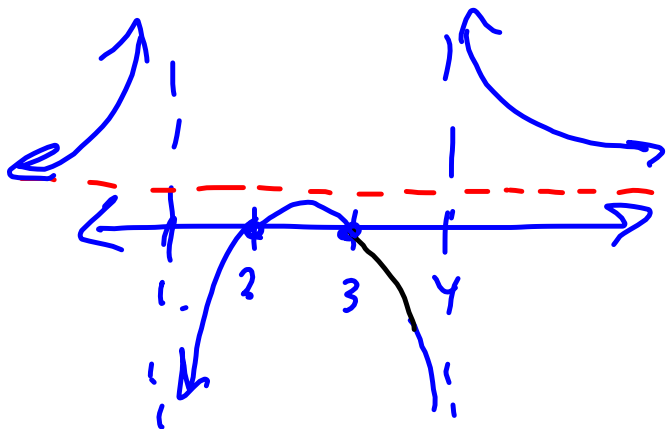
$\frac{(x-1)(x-3)}{(x-2)(x-4)}$



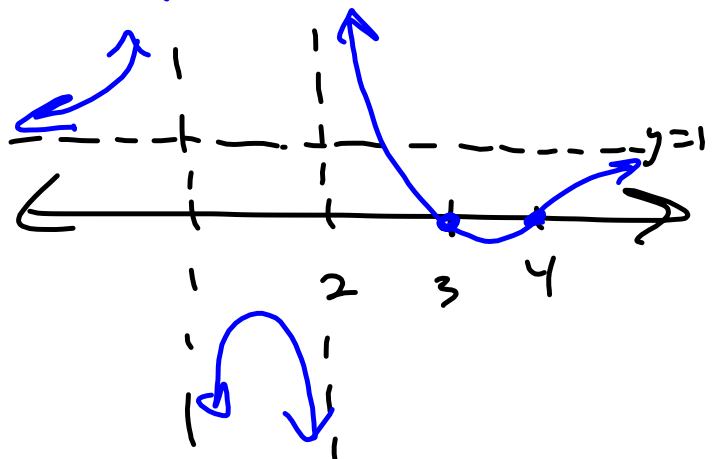
$\frac{(x-1)(x-4)}{(x-2)(x-3)}$



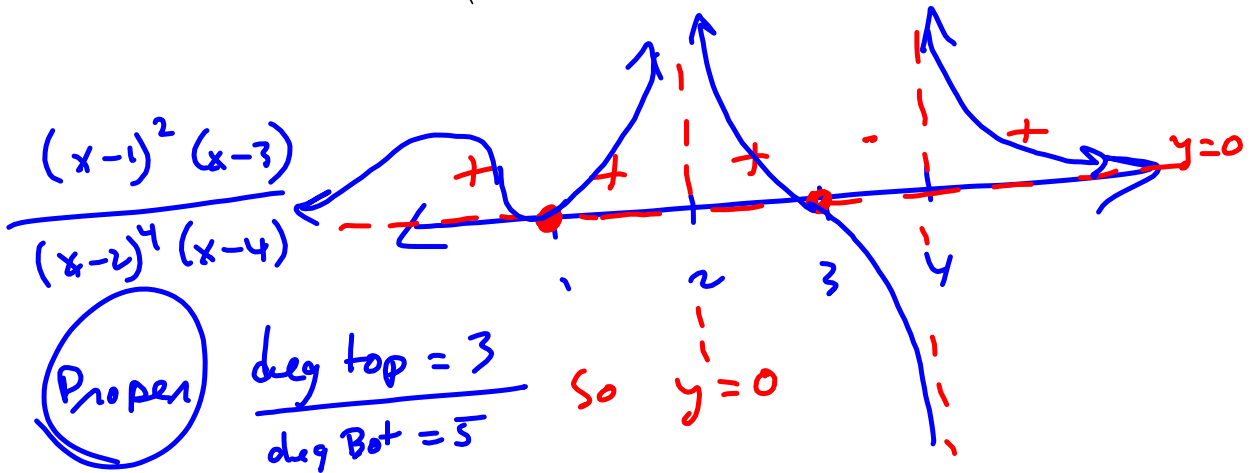
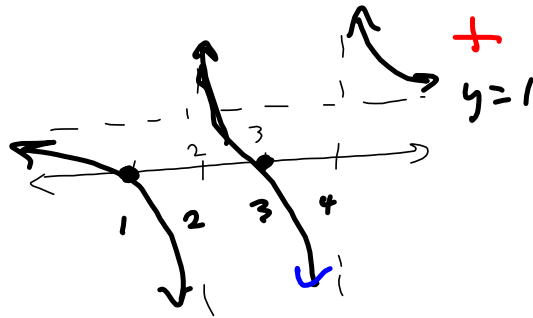
$\frac{(x-2)(x-3)}{(x-1)(x-4)}$



$\frac{(x-2)^3(x-4)}{(x-1)^5(x-3)^5}$



$$\frac{(x-1)(x-3)}{(x-2)(x-4)}$$



Proper

$$\frac{\text{deg top} = 3}{\text{deg Bot} = 5}$$

So  $y=0$



$$\frac{2x^3 - 5x^2 - 28x + 15}{x^2 - x - 20}$$

Obligue  
Slant asymptote

deg Top = 3

deg Bot = 2

$(2x - 1) \cdot (x + 3) \cdot (x - 5)$

$(x + 4) \cdot (x - 5)$

$y = 2x - 3$  is O.A.

$$\begin{array}{r} x^2 - x - 20 \quad \left( \begin{array}{l} 2x^3 - 5x^2 - 28x + 15 \\ - (2x^3 - 2x^2 - 40x) \end{array} \right) \\ \hline -3x^2 + 12x \end{array}$$

$$R(x) = \frac{(2x-1)(x+3)(x-5)}{(x+4)(x-5)}$$

$$D = \mathbb{R} \setminus \{-4, 5\}$$

$$R^*(x) = \frac{(2x-1)(x+3)}{(x+4)}$$

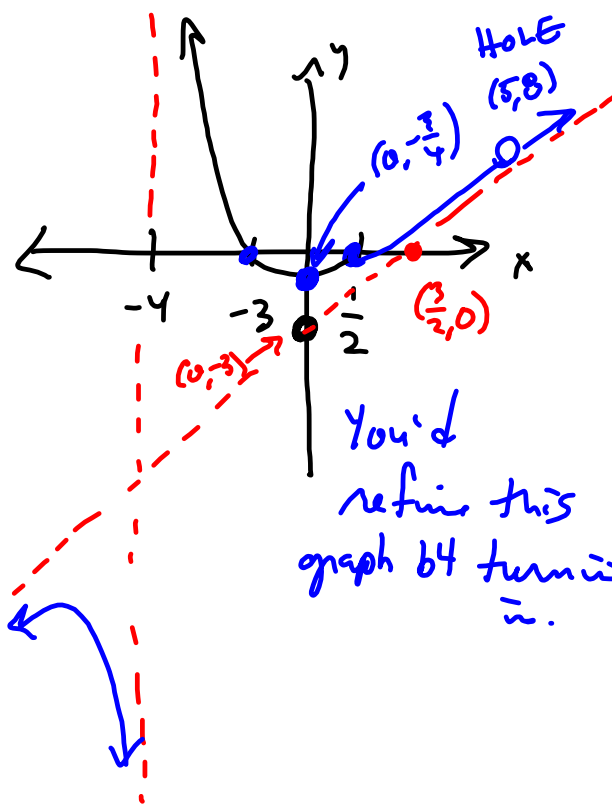
V.A.  $x = -4$

$x = 5$  → No  
 $x = 5$  is hole!

HOLE:  $\frac{(2(5)-1)(5+3)}{5+4}$

$$= \frac{(9)(8)}{9} = 8$$

HOLE (9) (5, 8)



You'd refine this graph by turning it ~.

$$y = 2x - 3 \quad (0, -3)$$

$$2x - 3 = 0$$

$$2x = 3$$

$$x = \frac{3}{2}$$

$$\left(\frac{3}{2}, 0\right)$$

Domain  $\sqrt{(x-5)(x+2)(x-3)^2(x-11)}$

$= \sqrt{\text{stuff}}$ . Need stuff  $\geq 0$  +

$\begin{array}{cccccccc} \text{N} & \text{Y} & \text{Y} & \text{Y} & \text{Y} & \text{N} & \text{Y} & \text{Y} \\ \hline & -2 & 3 & 5 & & 11 & & \\ & =0 & =0 & =0 & & =0 & & \end{array}$

$$D = [-2, 5] \cup [11, \infty)$$

$\sqrt{\frac{(x-5)(x-11)(x+2)}{(x-3)^2}}$  Find  $D$

$\begin{array}{cccccccc} \text{N} & \text{Y} & \text{Y} & \text{Y} & \text{Y} & \text{N} & \text{Y} & \text{Y} \\ \hline & -2 & 3 & 5 & & 11 & & \\ & =0 & \star & =0 & & =0 & & \end{array}$

$$D = [-2, 3) \cup (3, 5] \cup [11, \infty)$$