

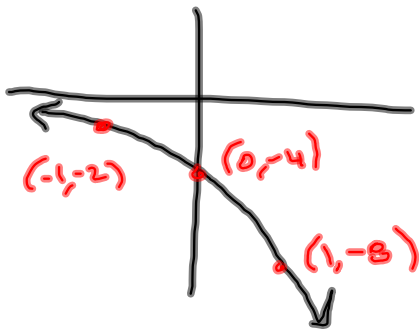
$f(x) = 2^x$

$g(x) = -4 \cdot 2^{x+1} + 5$

$$\begin{array}{l}
 2^x \rightarrow -4 \cdot 2^x \rightarrow -4 \cdot 2^{x+1} \rightarrow -4 \cdot 2^{x+1} + 5 \\
 (-1, \frac{1}{2}) \rightarrow (-1, -2) \rightarrow (-2, -2) \rightarrow (-2, 3) \\
 (0, 1) \rightarrow (0, -4) \rightarrow (-1, -4) \rightarrow (-1, 1) \\
 (1, 2) \rightarrow (1, -8) \rightarrow (0, -8) \rightarrow (0, -3)
 \end{array}$$

	-4 times y	left + 1	up 5
$f(x)$	$-4f(x)$	$-4f(x+1)$	$-4f(x+1) + 5$

Vertical Flip times 4



etc.

Friday: Kalista will run class Friday.

Group work $\left\{ \begin{array}{l} \text{word problems 5.1, 5.2, 6.1} \\ \text{Systems of nonlinear} \end{array} \right. \rightarrow \text{matrix.}$
equations (5.3)

TAKE YOUR TIME: Be systematic

\rightarrow Left to right
Top to bottom

- ① Eliminate x in E_2 & E_3 using E_1
- ② Eliminate y in E_3 using E_2 .

$$\begin{aligned} \#11 \ E1 \quad x + y + z &= 6 \\ E2 \quad 2x - 2y - z &= -5 \\ E3 \quad 3x + y - z &= 2 \end{aligned}$$

$$-2E1 + E2:$$

$$\begin{aligned} -2E1 \quad -2x - 2y - 2z &= -12 \\ E2 \quad 2x - 2y - z &= -5 \\ \hline & -4y - 3z = -17 \end{aligned}$$

New:

$$\begin{aligned} x + y + z &= 6 \\ -4y - 3z &= -17 \\ y + 2z &= 8 \end{aligned}$$

we like 1's

Improved

$$\begin{aligned} x + y + z &= 6 \\ y + 2z &= 8 \\ -4y - 3z &= -17 \end{aligned}$$

Row swap

NEW!

$$\begin{aligned} x + y + z &= 6 \\ y + 2z &= 8 \\ \boxed{z = 3} \end{aligned}$$

Back-substitute:

$$y + 2(3) = 8$$

$$y + 6 = 8$$

$$\boxed{y = 2}$$

Check

$$x + 2 + 3 = 6$$

$$x + 5 = 6$$

$$\boxed{x = 1}$$

A set containing a single ordered triple.

$$\{ \underline{(1, 2, 3)} \}$$

3-tuple

(1, 2, 3, 4) 4-tuple

(1, 2, 3, 4, 5) 5-tuple

(1, 2, 3, ..., m) m-tuple

ordered

m-tuple

#11 $x + y + z = 6$
 $2x - 2y - z = -5$
 $3x + y - z = 2$

SG.1 Take

has augmented coefficient matrix.

$$\begin{matrix} R1 \\ R2 \\ R3 \end{matrix} \left[\begin{array}{ccc|c} 1 & 1 & 1 & 6 \\ 2 & -2 & -1 & -5 \\ 3 & 1 & -1 & 2 \end{array} \right] \begin{matrix} R1 \\ -2R1+R2 \\ -3R1+R3 \end{matrix} \left[\begin{array}{ccc|c} 1 & 1 & 1 & 6 \\ 0 & -4 & -3 & -17 \\ 0 & 1 & 2 & 8 \end{array} \right]$$

Scratch:

$$\begin{array}{cccc|c} -2R1: & -2 & -2 & -2 & -12 \\ R2: & 2 & -2 & -1 & -5 \\ \hline & 0 & -4 & -3 & -17 \\ \\ -3R1 & -3 & -3 & -3 & -18 \\ R3 & 3 & 1 & -1 & 2 \\ \hline & 0 & -2 & -4 & -16 \end{array}$$

INDEPENDENT
CONSISTENT

$\div -2 \sim$ $\begin{matrix} 0 & 1 & 2 & 8 \end{matrix}$

$$R2 \leftrightarrow R3 \left[\begin{array}{ccc|c} 1 & 1 & 1 & 6 \\ 0 & 1 & 2 & 8 \\ 0 & -4 & -3 & -17 \end{array} \right] \begin{matrix} R1 \\ R2 \\ 4R2+R3 \end{matrix} \left[\begin{array}{ccc|c} 1 & 1 & 1 & 6 \\ 0 & 1 & 2 & 8 \\ 0 & 0 & 5 & 15 \end{array} \right]$$

etc. Compare to previous way

$$\begin{matrix} R1 \\ R2 \\ \frac{1}{5}R3 \end{matrix} \left[\begin{array}{ccc|c} 1 & 1 & 1 & 6 \\ 0 & 1 & 2 & 8 \\ 0 & 0 & 1 & 3 \end{array} \right]$$

etc.

Triangular on Left-hand side
"Row-echelon form."

DEPENDENT CONSISTENT as "triangular" as
 $2x - y + z = 7$
 $y + z = 5$ this one gets

This could happen with a system like

$$\begin{aligned} 2x - y + z &= 7 \\ y + z &= 5 \\ 3y + 3z &= 15 \end{aligned}$$

$-3E2 + E3$
 slab blah blah,
 gives me:

$$\begin{aligned} 2x - y + z &= 7 \\ y + z &= 5 \\ 0 &= 0 \end{aligned}$$

↘
 vacuous
 truth.

How to write up the solution?

CONVENTION:

Let z be free /
 x & y will depend
 on z .

$$y + z = 5$$

$y = -z + 5$

$$\begin{aligned} 2x - y + z &= 7 \\ 2x - (-z + 5) + z &= 7 \\ 2x + z - 5 + z &= 7 \\ 2x + 2z - 5 &= 7 \\ 2x + 2z &= 12 \\ x + z &= 6 \end{aligned}$$

$z = \text{Any real \#} !$

Solution Set:

$$\{ (-z + 6, -z + 5, z) \mid z \in \mathbb{R} \}$$

$x = -z + 6$

$$= \{ (x, y, z) \mid x = -z + 6, y = -z + 5, z \in \mathbb{R} \}$$

General
 Solution

Do NOT say "z is all reals"

"z is any real #" is OK.

For a particular solution, let $z =$ a particular value.

$z = 0 \Rightarrow x = 6, y = 5$, so $(6, 5, 0)$ is a particular solution.

Solution set, here, is a line

$$\begin{array}{rcl}
 2x & -y & + z = 7 \\
 & y & + z = 5 \\
 & & 3y + 3z = 17
 \end{array}
 \qquad
 \begin{array}{r}
 -3E2 + E3! \\
 -3E2 \quad -3y - 3z = -15 \\
 E3 \quad 3y + 3z = 17 \\
 \hline
 0 = 2 \quad !?
 \end{array}$$

This falsehood contradicts the assumption that the system has a solution.

No Sol'n

DEPENDENT,
INCONSISTENT

§ 5.3 Pre-prob:

$$5x - y = 6$$

$$y = x^2$$

$$5x - y = 6$$

$$5x - x^2 = 6$$

$$-x^2 + 5x - 6 = 0$$

$$x^2 - 5x + 6 = 0$$

$$(x-3)(x-2) = 0$$

$$x \in \{2, 3\}$$

