

Section 3.1 #s 1-9, 11-19 odds, 75-90

Section 3.1 #s 9-19 odds:

Show vertex and intercepts

Complete the square to write in the form $f(x) = a(x-h)^2 + k$

Check vertex with $-\frac{b}{2a}$ + h.i.n.g

State intervals of increase and decrease.

Section 3.1 #s 75-90:

Answers in interval form

Work all like #s 79-90 (I want #s 75-78 lumped in with #s 79-90)

Show SIGN PATTERN

Show graph that shows only x-intercepts

Special: #s 75-78, 87, 88 are not typical. (Kiss the x-axis or don't cross it at all!).

Before Wednesday: One Theorem per page. All theorems from Sections 3.2, 3.3 in your notes.

This is a key activity for students who want to go on and graduate from college.

$$(h, k) = \text{vertex}$$

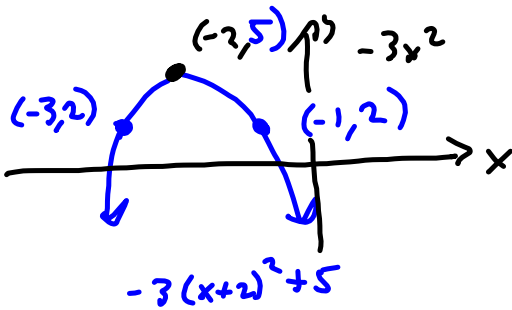
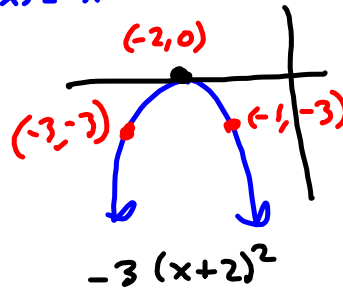
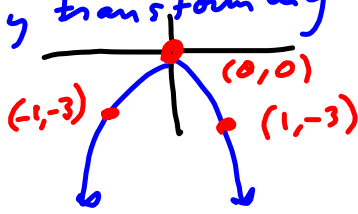
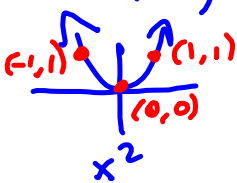
$$(h, k) = \left(-\frac{b}{2a}, f\left(-\frac{b}{2a}\right)\right)$$

Recall graphing, say

$$g(x) = -3(x+2)^2 + 5$$

$$f(x) = x^2, -3x^2, -3(x+2)^2, -3(x+2)^2 + 5$$

Graphing by transforming



Follow-up:
Find x- and y-intercepts

$$g(x) = -3(x+2)^2 + 5$$

-3 in front

vertex: (-2, 5)

x-int:

$$-3(x+2)^2 + 5 = 0$$

$$-3(x+2)^2 = -5$$

Need $(x+2)^2 = \frac{-5}{-3} = \frac{5}{3}$

y-int: $g(0)$

$$= -3(0+2)^2 + 5$$

$$= -3(2)^2 + 5$$

$$= -12 + 5$$

$$= -7 \rightarrow (0, -7)$$

$$\sqrt{(x+2)^2} = \sqrt{\frac{5}{3}} = \frac{\sqrt{5}}{\sqrt{3}} = \frac{\sqrt{5} \cdot \sqrt{3}}{\sqrt{3} \cdot \sqrt{3}} = \frac{\sqrt{15}}{3}$$

optional steps → scratch work

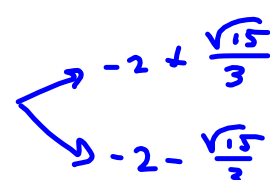
$$|x+2| = \frac{\sqrt{15}}{3}$$

$$x+2 = \frac{\sqrt{15}}{3} \quad \text{OR} \quad x+2 = -\frac{\sqrt{15}}{3}$$

Need

$$x+2 = \pm \frac{\sqrt{15}}{3}$$

$$x = -2 \pm \frac{\sqrt{15}}{3}$$



$$\left(-2 + \frac{\sqrt{15}}{3}, 0\right)$$

$$\left(-2 - \frac{\sqrt{15}}{3}, 0\right)$$

$$g(x) = -3(x+2)^2 + 5$$

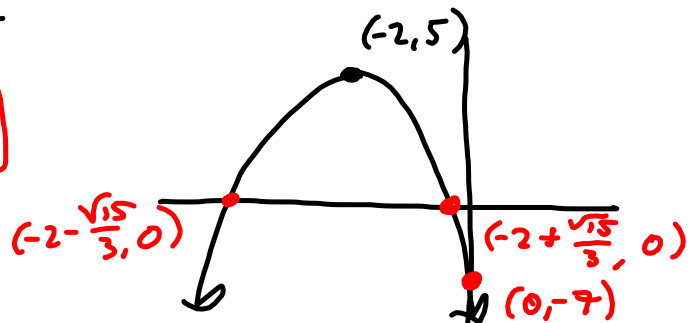
-3 in front

vertex: $(-2, 5)$

$$\left(-2 + \frac{\sqrt{15}}{3}, 0\right)$$

$$\left(-2 - \frac{\sqrt{15}}{3}, 0\right)$$

$$(0, -7)$$



want to locate about
where $-2 \pm \frac{\sqrt{15}}{3}$ are

$$-2 + \frac{\sqrt{15}}{3} \approx -0.709$$

$$-2 - \frac{\sqrt{15}}{3} \approx -3.3$$

$$g(x) = 5(x-7)^2 - 11$$

$$(h, k) = (7, -11)$$

opens up

y-int:

$$\begin{aligned} & 5(49) - 11 \\ & = 245 - 11 \\ & = 234 \rightarrow (0, 234) \end{aligned}$$

x-int

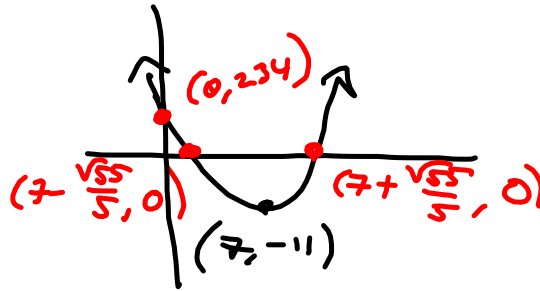
$$5(x-7)^2 - 11 = 0$$

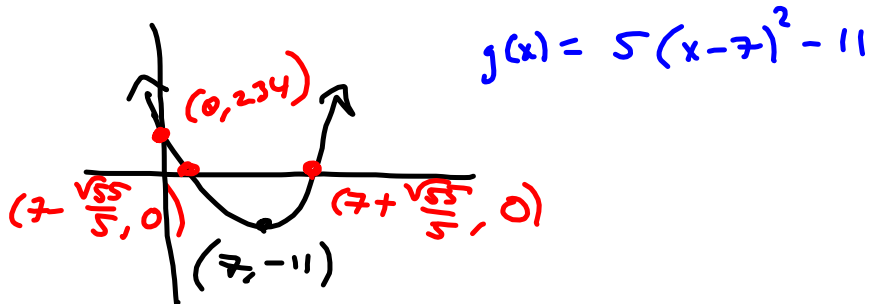
$$5(x-7)^2 = 11$$

$$(x-7)^2 = \frac{11}{5}$$

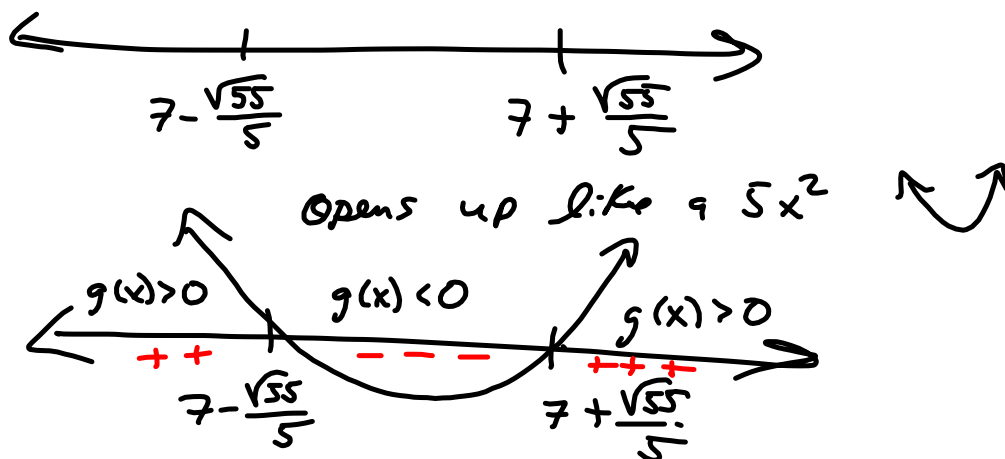
$$x-7 = \pm \sqrt{\frac{11}{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} = \pm \frac{\sqrt{55}}{5}$$

$$x = 7 \pm \frac{\sqrt{55}}{5} \quad 5.516760303 \approx 7 - \frac{\sqrt{55}}{5}$$





Solve $g(x) > 0$ for the inequality
at the end of the assignment, all we
need is



Sign Pattern:

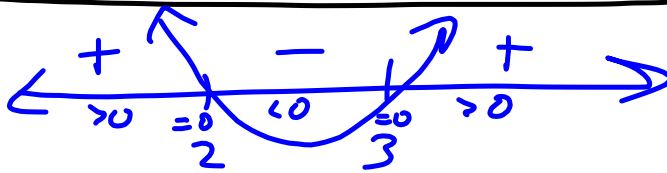


> 0 says take the " $+$ "

$$x^2 - 5x + 6 \leq 0$$
$$(x-2)(x-3) \leq 0$$

x^2 ↗ ↗

$x-2 \leq 0$ OR $x-3 \leq 0$
most common error



want
 ≤ 0

$$x \in [2, 3]$$

$$\text{Solve } 9x^2 - 12x + 1 \geq 0$$

$$a = 9, b = -12, c = 1$$

$$b^2 - 4ac = (-12)^2 - 4(9)(1)$$

$$= 144 - 36$$

$$= 108$$

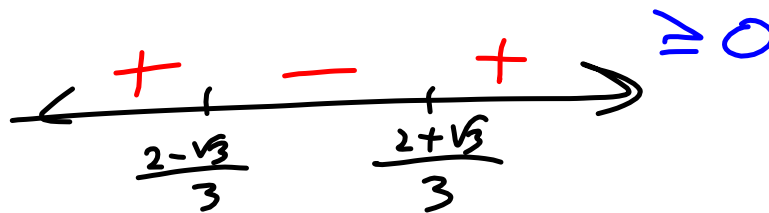
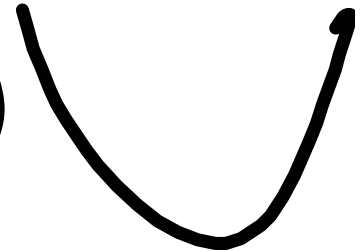
$$x = \frac{12 \pm 6\sqrt{3}}{2(9)}$$

$$= \frac{12 \pm 6\sqrt{3}}{18} = \frac{6(2 \pm \sqrt{3})}{18}$$

$$= \frac{2 \pm \sqrt{3}}{3}$$

$$\sqrt{108} = 6\sqrt{3}$$

$$\begin{array}{r} 2 \overline{)108} \\ 2 \overline{)54} \\ 3 \overline{)27} \\ 3 \overline{)9} \\ 3 \end{array}$$



$$\left(-\infty, \frac{2-\sqrt{3}}{3}\right] \cup \left[\frac{2+\sqrt{3}}{3}, \infty\right)$$