

We've covered virtually every concept on Test 1,
 (1. Test 1: Monday

Today: Brief (review) §1.7 talk.

Then in-class work.

Recall: $|A| = B \left\{ \begin{array}{l} A = B \text{ or } A = -B \\ \Rightarrow A = \pm B \end{array} \right.$

only thing new is now $A = ax^2 + bx + c$ is sometimes quadratic.

$|x^2 - 5x + 5| = 1$ Spawns two equations.

$$x^2 - 5x + 5 = 1 \quad \text{or} \quad x^2 - 5x + 5 = -1 \quad *$$

$$x^2 - 5x + 4 = 0$$

$$(x-1)(x-4) = 0$$

$$x = 1, 4$$

$$x^2 - 5x + 6 = 0$$

$$(x-2)(x-3) = 0$$

$$x = 2, 3$$

$$x \in \{1, 2, 3, 4\}$$

$$-\frac{4}{1} \cdot \frac{4}{4} + \frac{25}{4} = \frac{9}{4}$$

$$\left(x - \frac{5}{2}\right)^2 = \frac{9}{4}$$

$$x - \frac{5}{2} = \pm \sqrt{\frac{9}{4}} = \pm \frac{3}{2}$$

$$x = \frac{5 \pm 3}{2} \dots$$

$$x^2 - 5x + 4 = 0$$

$$x^2 - 5x = -4$$

$$\frac{5}{2} \rightarrow \left(\frac{5}{2}\right)^2 = \frac{25}{4}$$

$$x^2 - 5x + \left(\frac{5}{2}\right)^2 = -4 + \frac{25}{4}$$

$$\left(x - \frac{5}{2}\right)^2 = \frac{9}{4}$$

$$\sqrt{\left(x - \frac{5}{2}\right)^2} = \sqrt{\frac{9}{4}}$$

$$\left|x - \frac{5}{2}\right| = \frac{3}{2}$$

$$x - \frac{5}{2} = \pm \frac{3}{2}$$

$$x = \frac{5 \pm 3}{2} \dots$$

$$x^2 - 5x + \left(\frac{5}{2}\right)^2 = -4 + \frac{25}{4}$$

$$\sqrt{\left(x - \frac{5}{2}\right)^2} = \sqrt{\frac{9}{4}}$$

$$x - \frac{5}{2} = \pm \frac{3}{2}$$

← cramming too much into one line/step.

Also, compound inequalities:
 Mind your and's & or's.
 Already worked with these on
 the 1st assignment (099 FINAL)

$$3 - 2x < 5$$

$$-2x < 2$$

$$x > \frac{2}{-2} = -1$$

$$x > -1$$

$$3 - 2x < 5$$

$$\frac{-2x < 2}{-2 \quad -2}$$

$$x > -1$$

Does not
follow
Does not
follow

$$\leftarrow \begin{array}{c} | \\ \longleftarrow \longrightarrow \\ | \end{array} \longrightarrow = (-1, \infty)$$

S 1, 7 #s 1-17, 19, 22, 23, 26, 27, 34, 35, 38, 39, 41, 45, 47, 50, 53,
 56, 60, 62, 63, 67, 74, 77, 79, 81, 84, 91, 93

Katie says, I did #30 instead of #31, and mis-copied #34.

$$\begin{aligned} \textcircled{34} \quad (x-2)^{-\frac{1}{2}} &= \frac{1}{3} \\ (x-2)^{\frac{1}{2}} &= \frac{3}{1} = 3 \\ \left((x-2)^{\frac{1}{2}}\right)^2 &= 3^2 \\ x-2 &= 9 \\ x &= 11 \\ x &\in \{11\} \end{aligned}$$

\pm

$$\begin{aligned} \sqrt{25} &= 5 \\ \sqrt{25} &\neq -5 \end{aligned}$$

$$\begin{aligned} A=B &\Rightarrow A^2=B^2 \\ A^2=B^2 &\not\Rightarrow A=B \\ A^2=B^2 &\Rightarrow A=\pm B \end{aligned}$$

\sqrt{A} is
Principle Square Root
and always positive
(or zero).

$$\sqrt{4} = 2 \neq -2$$

$$\sqrt{x^2} = |x|$$

$$\sqrt{(-3)^2} = 3 = \sqrt{3^2}$$

$\sqrt{\quad}$

§ 1.6 # 2

check $x = 5$ in $\sqrt{x-1} = x-7$

$$\sqrt{5-1} \stackrel{?}{=} 5-7$$
$$\sqrt{4} \stackrel{?}{=} -2$$
$$2 \stackrel{?}{=} -2$$

*Never!

§1.6 #1

$$\frac{-4x}{-4} = x \quad \frac{-12}{-4} = 3$$

$$\underline{x^3 + 3x^2 - 4x - 12 = 0}$$

$$x^2(x+3) - 4(x+3) = 0$$

$$(x+3)(x^2-4) = 0$$

$$(x+3)(x-2)(x+2) = 0$$

$$x \in \{\pm 2, -3\}$$

Check: Remainder Theorem!

$$f(x) = x^3 + 3x^2 - 4x - 12$$

Use synthetic division to find $f(-3)$:

Divide $f(x)$ by $x+3$ & look @ remainder.

$$\begin{array}{r|rrrr} -3 & 1 & 3 & -4 & -12 \\ & & -3 & 0 & 12 \\ \hline & 1 & 0 & -4 & 0 = f(-3) \end{array}$$

This work says:

$$\frac{x^3 + 3x^2 - 4x - 12}{x+3} = x^2 - 4 + 0$$

$$x^3 + 3x^2 - 4x - 12 = (x^2 - 4)(x+3) + 0$$

$$\frac{1}{p} - \frac{2}{\sqrt{9p+1}} = 0 \quad \text{LCD: } p\sqrt{9p+1}$$

$$\frac{1 \cdot \sqrt{9p+1}}{p \sqrt{9p+1}} - \frac{2}{\sqrt{9p+1}} \cdot \frac{p}{p} = 0 = \frac{0}{\text{LCD}}$$

$$\frac{\sqrt{9p+1} - 2p}{\text{LCD}} = \frac{0}{\text{LCD}}$$

$$\sqrt{9p+1} - 2p = 0 \quad \text{by hand}$$

checking this bear $\sqrt{\text{sucks}}$

⋮