

Homework --

Sentences! "Context"

Questions?

$$ax^2 + bx + c = 0$$

$$x^2 + \frac{b}{a}x = -\frac{c}{a}$$

$$x^2 + \frac{b}{a}x + \left(\frac{b}{2a}\right)^2 = -\frac{c}{a} + \frac{b^2}{4a^2} = \frac{b^2 - 4ac}{4a^2}$$

$$\frac{a/b}{2} = \frac{b}{a} \cdot \frac{1}{2} = \frac{b}{2a}$$

$$\left(x + \frac{b}{2a}\right)^2 = \frac{b^2 - 4ac}{4a^2}$$

$$\sqrt{\quad} = \sqrt{\quad}$$

$$\left|x + \frac{b}{2a}\right| = \sqrt{\frac{b^2 - 4ac}{4a^2}} = \frac{\sqrt{b^2 - 4ac}}{\sqrt{4a^2}} = \frac{\sqrt{b^2 - 4ac}}{2|a|}$$

$$x + \frac{b}{2a} = \pm \frac{\sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$-3x^2 + 5x - 3 = 0$$

$$3x^2 - 5x + 3 = 0$$

$$-\frac{c}{a} \cdot \frac{4a}{4a} + \frac{b^2}{4a^2} = \frac{b^2 - 4ac}{4a^2}$$

Derivation of  
Quadratic Formula  
in response to  
an innocent  
question.

Today: Some S1.6 examples

Some S1.5 probs on the board.

Last time  $A=B \implies A^2=B^2, A^3=B^3, \dots$

But  $A^2=B^2 \not\implies A=B$

$A^2=B^2 \implies A=\pm B$  Squaring both sides can inject extraneous solutions

$$x^{\frac{2}{3}} = 1$$

$$\left(x^{\frac{2}{3}}\right)^3 = 1^3$$

$$x^2 = 1$$

$$x = \pm 1$$

$$(x^a)^b = x^{ab}$$

check

S 1.6 #s 1, 6, 9, 12, 18, 19, 21, 22, 23, 27, 28  
31, 34, 35, 36, 37, 41, 43, 47, 53, 55, 59, 63,  
65, 67, 69, 73

Equations with rational (fractional) exponents.

.. Quadratic in Form I & II

.. with absolute value

.. ..  $\sqrt{\quad}$  & stuff.

$$(36) \quad x^4 + 10 = 7x^2$$

Let  $u = x^2$ . Then

$$u^2 + 10 = 7u$$

$$u^2 - 7u + 10 = 0$$

$$(u-5)(u-2) = 0$$

$$u-5=0 \text{ or } u-2=0$$

$$u=5 \quad u=2$$

$$x^2=5 \quad x^2=2$$

$$x = \pm\sqrt{5} \quad x = \pm\sqrt{2}$$

$$x \in \{ \pm\sqrt{5}, \pm\sqrt{2} \}$$

Quadratic in Form

Factor Theorem!

$$x^2 - 7x + 10 = 0$$

$$x^2 - 7x = -10$$

$$x^2 - 7x + \left(\frac{7}{2}\right)^2 = -10 + \frac{49}{4}$$

$$\frac{7}{2} \rightsquigarrow \left(\frac{7}{2}\right)^2$$

$$\left(x - \frac{7}{2}\right)^2 = \frac{-40 + 49}{4} = \frac{9}{4}$$

$$\sqrt{\quad} = \sqrt{\quad}$$

$$x - \frac{7}{2} = \pm \sqrt{\frac{9}{4}} = \pm \frac{\sqrt{9}}{\sqrt{4}}$$

$$x = \frac{7}{2} + \frac{3}{2} \rightarrow \frac{10}{2} = 5$$

$$x = \frac{7}{2} - \frac{3}{2} \rightarrow \frac{4}{2} = 2$$

$a^2 - b^2 = (a-b)(a+b)$  Difference of 2 squares

$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$  Difference of  
 $a^3 + b^3 = (a+b)(a^2 - ab + b^2)$  cubes

(40)  $x^4 - 625 = 0$

$x^2 + 25$   $(5i)^2 = -25$   
 $= x^2 - (-25)$   
 $x^2 - (5i)^2$

$(x^2 - 25)(x^2 + 25) = 0$

$(x-5)(x+5)(x-5i)(x+5i) = 0$

$x \in \{\pm 5, \pm 5i\}$

#18 You should check all answers, but

$u = x^2$

$u^2 - 625 = 0$

$\frac{9 \pm \sqrt{97}}{0} ! ?$

$(u - 25)(u + 25) = 0$

You really want me to plug that into

$u = 25$        $u = -25$

$x^2 = 25$        $x^2 = -25$

$\frac{1}{x} \sqrt{9x^2 + 1} = 0 ? !$

$x = \pm 5$        $x = \pm \sqrt{-25} = \pm i \sqrt{25} = \pm i5 = \pm 5i$

Same deal.  
 Your option on style.

<http://dlippman.imathas.com/graphcalc/graphcalc.html>

To check ugly ones, in  $\mathcal{S}^1$ , this is a good resource.

Has graphing capabilities:

Everything a TI-83 or 84  
Pocket CAS *max/min, intersection, zeros.*

Are CalcPro for iPhone/iPad

$$\left(\frac{x-5}{6}\right)^2 - \left(\frac{x-5}{6}\right) - 6 = 0$$

$$u^2 - u - 6 = 0 \quad u = \frac{x-5}{6}$$

$$(u-3)(u+2) = 0$$

$$u = 3$$

$$u = -2$$

& check.

$$\frac{x-5}{6} = 3$$

$$\frac{x-5}{6} = -2$$

$$x-5 = 18$$

$$x-5 = -12$$

$$x = 23$$

$$x = -7$$

$$\textcircled{46} \textcircled{42} (x^2+2x)^2 - 2(x^2+2x) - 3 = 0$$

$$u^2 - 2u - 3 = 0 \quad u = x^2 + 2x$$

$$(u-3)(u+1) = 0$$

$$u = 3 \quad u = -1$$

$$x^2 + 2x = 3 \quad x^2 + 2x = -1$$

$$x^2 + 2x - 3 = 0 \quad x^2 + 2x + 1 = 0$$

$$(x+3)(x-1) = 0 \quad (x+1)^2 = 0$$

$$x+1 = \pm 0 = 0$$

$$x = 1, -3 \quad x = -1$$

$$x \in \{-3, -1, 1\}$$



(48)

$$2x + 3\sqrt{x} - 20 = 0$$

Also quadratic  
in form.

$$u = \sqrt{x} !$$

$$(\sqrt{x})^2 = x$$

$$\sqrt{x^2} = |x|$$

$$2u^2 + 3u - 20 = 0$$

$$2u^2 + 8u - 5u - 20 = 0$$

$$2u(u+4) - 5(u+4) = 0$$

$$2u \text{ ☺ } - 5 \text{ ☺ } = 0$$

$$\text{☺ } (2u - 5) = 0$$

$$(u+4)(2u-5) = 0$$

$$u = -4 \text{ OR } u = \frac{5}{2}$$

$$\sqrt{x} = -4 \text{ OR } \sqrt{x} = \frac{5}{2}$$

Nabak!

$$x = \frac{25}{4}$$

$$(52) \quad x^{\frac{1}{2}} - 3x^{\frac{1}{4}} + 2 = 0$$

$$u = x^{\frac{1}{2}}$$

$$u^2 = x$$

$$u = x^{\frac{1}{4}}$$

$$u^2 = (x^{\frac{1}{4}})^2 = x^{\frac{1}{2}}$$

$$u - 3u^2 + 2 = 0$$

$$-3u^2 + u + 2 = 0$$

$$3u^2 - u - 2 = 0$$

$$3u^2 - 3u + 2u - 2 = 0$$

$$3u(u-1) + 2(u-1) = 0$$

$$(u-1)(3u+2) = 0$$

$$u = 1$$

$$u = -\frac{2}{3}$$

$$x^{\frac{1}{4}} = 1$$

$$x^{\frac{1}{4}} = -\frac{2}{3}$$

$$x = 1^4 = 1$$

$$x = 1$$

(54)

$$|x^2 - 1| = 1$$

$$x^2 - 1 = 1 \quad \text{or} \quad x^2 - 1 = -1$$

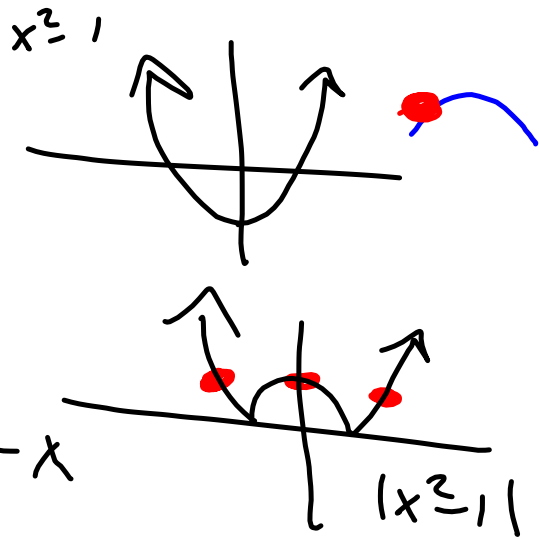
etc.

(60)

$$|3x - 4| = |x|$$

$$3x - 4 = x \quad \text{or} \quad 3x - 4 = -x$$

etc.



(6b) The toughest.

$$\sqrt{16x+1} - \sqrt{6x+13} = 1$$

$$\sqrt{16x+1} = \sqrt{6x+13} + 1$$

$$\begin{aligned} 16x+1 &= 6x+13 + (2\sqrt{6x+13})(1) + 1^2 \\ &= 6x+13 + 2\sqrt{6x+13} + 1 \\ &= 6x+14 + 2\sqrt{6x+13} = 16x+1 \end{aligned}$$

Square both sides!

$$\begin{aligned} 2\sqrt{6x+13} &= 10x-13 \\ 4(6x+13) &= 100x^2 - 260x + 169 \\ 24x+52 &= 100x^2 - 260x + 169 \end{aligned}$$

$$100x^2 - 284x + 117 = 0$$

etc.

$$(a+b)^2 = a^2 + 2ab + b^2$$