

1. (10 pts) Is the relation  $f = \{(3,-7), (4,-1), (2,5), (9,-1)\}$  a function? Explain in words.
  
2. (5 pts) What's the domain of  $f$ ?
  
3. (5 pts) What's the range of  $f$ ?
  
4. Let  $f(x) = \frac{x+7}{x-2}$  and  $g(x) = \sqrt{x+1}$ .
  - a. (5 pts) What is the domain of  $f$ ?
  
  - b. (5 pts) What is the domain of  $g$ ?
  
  - c. Determine the following functions. You don't need to simplify. In fact, I recommend you do not.
    - i) (5 pts)  $f + g$
  
    - ii) (5 pts)  $f \circ g$
  
  - d. (5 pts) What is the domain of  $f + g$ ? State your final answer in interval notation.
  
  - e. (5 pts) What is the domain of  $f \circ g$ ? State your final answer in interval notation.

5. (5 pts) Simplify the difference quotient,  $\frac{f(x+h) - f(x)}{h}$ , for  $f(x) = x^2 - 5x$ .



**Bonus** Pass to the limit, as  $h \rightarrow 0$ , on your answer to the above, so you can show me some calculus.

6. (5 pts) Explain to me why the equation  $x^2 + y^2 = 49$  does *not* define  $y$  as a function of  $x$ .

7. (5 pts) Draw me a picture showing what the difference quotient represents for the function  $f(x) = \sqrt{x}$ .



**Bonus** Simplify the difference quotient for  $f(x) = \sqrt{x}$ .

8. (10 pts) Answer one of the following:

- a. Show that  $f(x) = \frac{2}{3}x - 7$  is one-to-one, algebraically.
- b. If  $f(x) = x^2 - 6x + 7$ , for  $x \geq 3$ , what is  $f^{-1}(x)$ ?

9. (10 pts) Show that  $f(x) = \frac{x+3}{x-1}$  is its own inverse. In other words, show that in this example,  $f$  and  $f^{-1}$  are the same, exact function! There are two ways to accomplish this:

1. By finding  $f^{-1}$ , directly.
2. By the definition of  $f^{-1}$ .

10. (10 pts) Suppose  $y$  varies jointly with  $m_1$  and  $m_2$ , and inversely with the square of  $r$ . Write an equation describing this situation.