

$$\frac{x^3 - 7x + 6}{x^2 - 5x + 4}$$

$$\frac{\cancel{(x-1)}(x-2)(x+3)}{\cancel{(x-1)}(x-4)}$$

$D = \mathbb{R} \setminus \{1, 4\}$
 v.A: $x=4$

$$\begin{array}{r} -3 \overline{) 1 \quad 0 \quad -7 \quad 6} \\ \underline{-3 \quad 9 \quad -6} \\ 1 \quad -3 \quad 2 \end{array}$$

$$x^2 - 3x + 2 = (x-1)(x-2)$$

hole @ $(1, \frac{4}{3})$

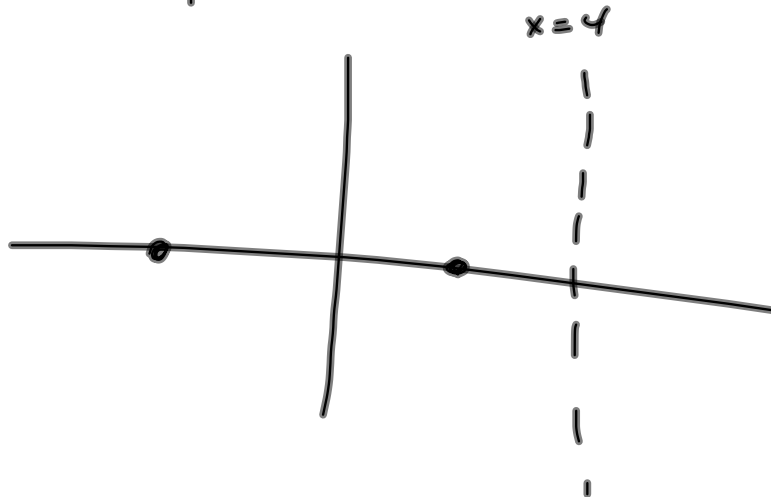
$$\frac{(1-2)(1+3)}{(1-4)} = \frac{(-1)(4)}{-3} = \frac{4}{3}$$

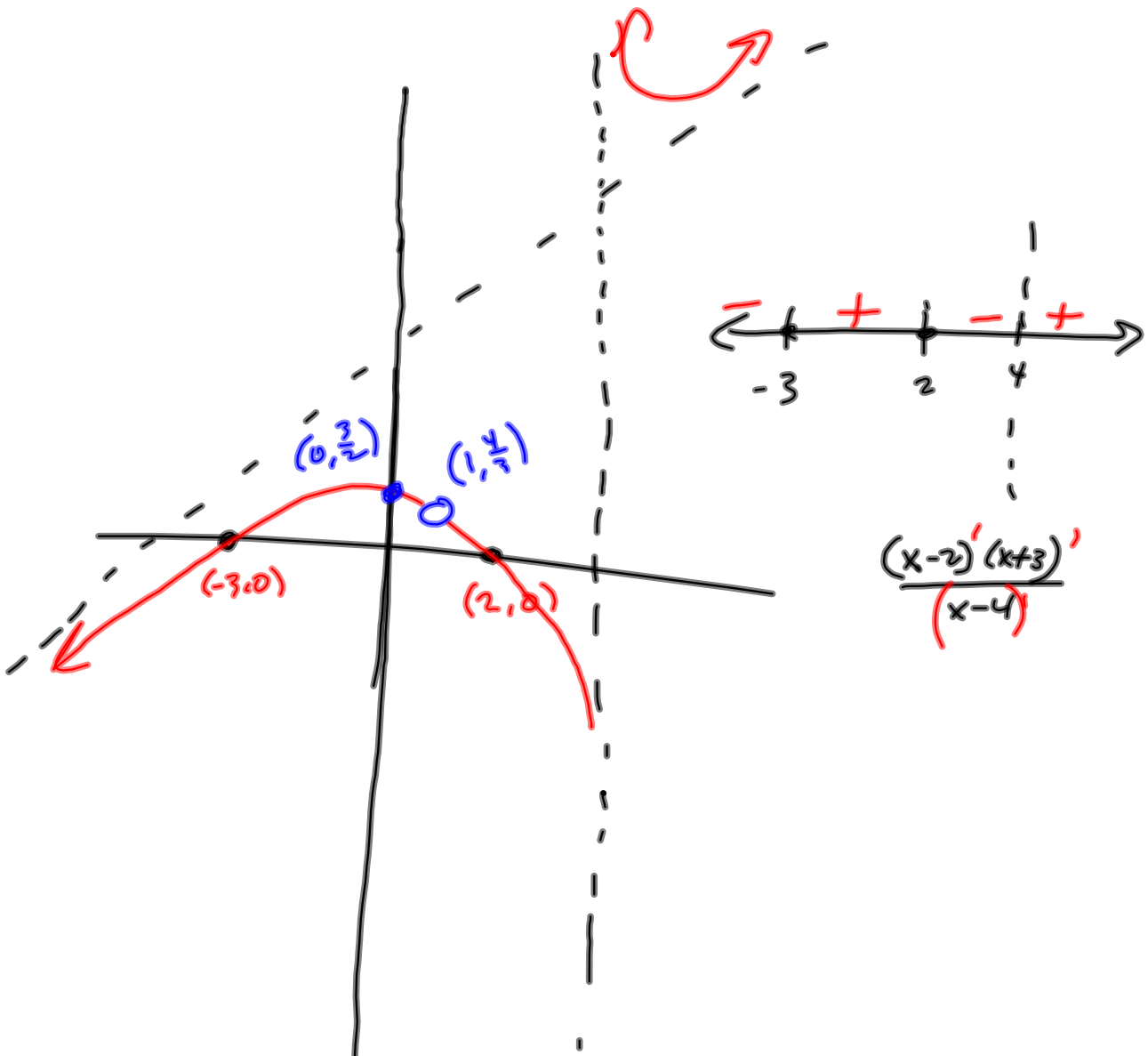
$$x-4 \overline{) x^2 + x - 6}$$

$y = x + 5$ O.A.

$$\begin{array}{r} 4 \overline{) 1 \quad 1 \quad -6} \\ \underline{4 \quad 20} \\ 1 \quad 5 \quad 14 \end{array}$$

x-axis: $(-3, 0), (2, 0)$





§4.1 Exponential Functions

D An exponential function with base a is a function of the form

$$f(x) = a^x$$

where $a, x \in \mathbb{R}$, $a > 0$, $a \neq 1$

$$f(x) = 3^x$$

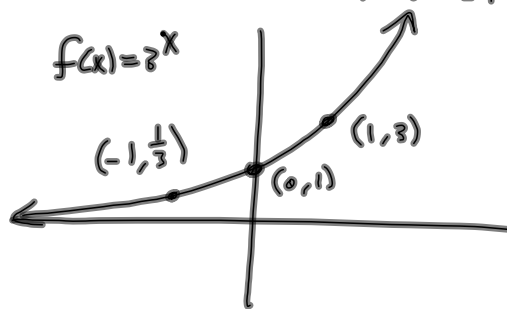
$$f(2) = 3^2 = 9$$

$$f(-2) = 3^{-2} = \frac{1}{3^2} = \frac{1}{9}$$

$$f(-1) = 3^{-1} = \frac{1}{3}$$

$$f(1) = 3^1 = 3$$

$$f(0) = 3^0 = 1$$



$$D = \mathbb{R}$$

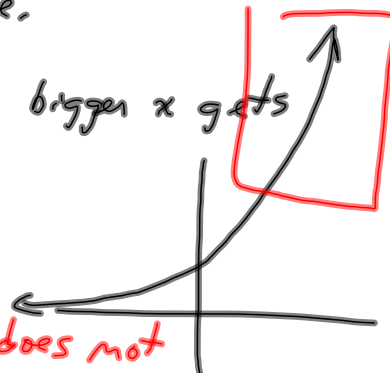
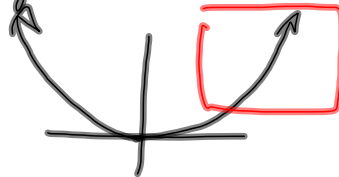
3^x is real
if x is real.

$$3^{100}$$

Exponential Growth:

Growth rate is proportional to population size.

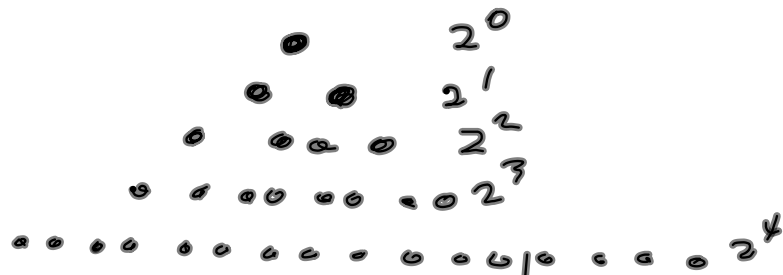
Now, x^2 grows faster the bigger x gets



But polynomial growth does not have this proportionality between size and growth rate.

Examples Pop., \$, aggregation,

$$2^x$$

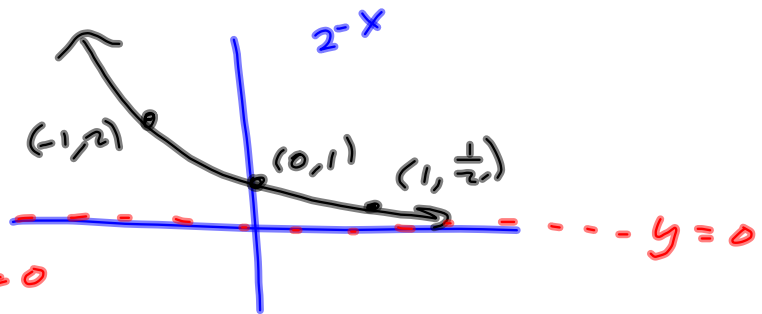
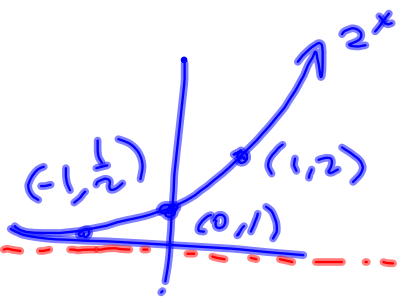


Exponential Decay

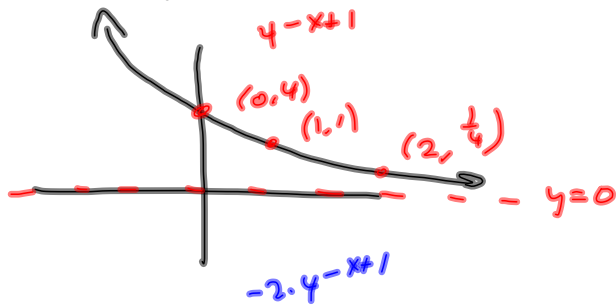
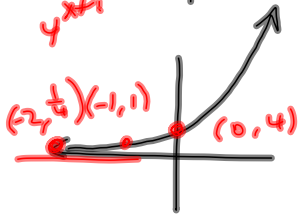
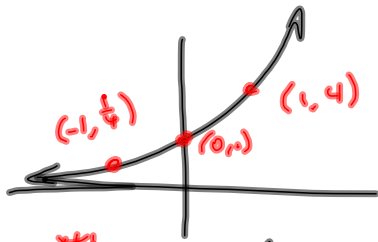
Pop.,

Radioactive Isotopes

$$f(x) = 2^{-x}$$



$$f(x) = 4^x$$



$$g(x) = -2 \cdot 4^{1-x} - 7$$

$$1-x = -x+1$$

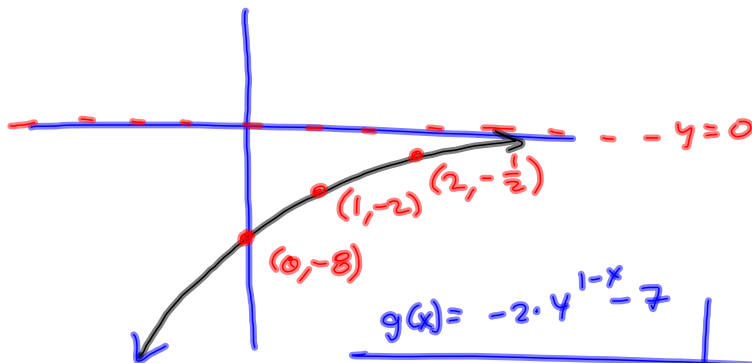
$$x+1, -x+1$$

$$4^x \rightarrow 4^{x+1} \rightarrow 4^{-x+1}$$

$$\rightarrow -2 \cdot 4^{-x+1}$$

$$\rightarrow -2 \cdot 4^{-x+1} - 7$$

- ① Hor Shift
- ② Hor stretch/ref.
- ③ Vert. stretch/ref.
- ④ Vert. shift.



$$g(x) = -2 \cdot 4^{1-x} - 7$$

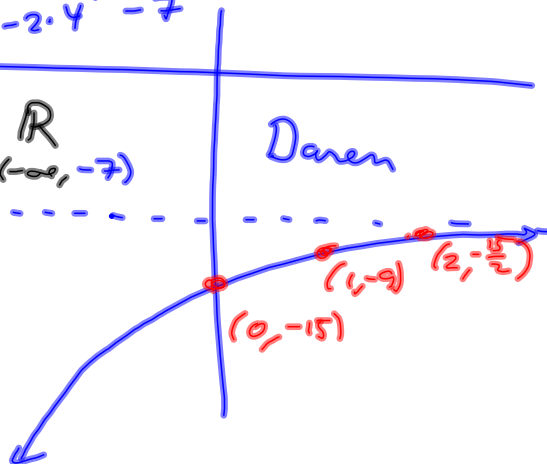
$$D = \mathbb{R}$$

$$R = (-\infty, -7)$$

Daren

$$y = -7$$

$$-\frac{1}{2} - \frac{4}{2} = -\frac{15}{2}$$



Compound Interest.

$$A = P \left(1 + \frac{r}{m} \right)^{mt}$$

$$\left. \begin{array}{l} n = mt \\ i = \frac{r}{m} \end{array} \right\}$$

$$A = P(1+i)^n$$

$r = \text{APR}$

$m = \text{periods/yr}$

$t = \text{\# of years}$

$P = \text{Principal}$

$A = \text{Future Value (accumulation)}$

$i = \text{interest rate/period.}$
 $n = \text{total \# of periods.}$

Future value of \$5,000 compounded daily
for 20 years @ 5%

$$\begin{aligned} A &= P \left(1 + \frac{r}{m} \right)^{mt} \\ &= 5000 \left(1 + \frac{.05}{365} \right)^{365 \cdot 20} \end{aligned}$$

```

Y3 (Ans)
5000(1+.05/365)^
365*20
105126.7496
5000(1+.05/365)^
(365*20)
13590.47834
    
```

Need parens around 365*20, since what this

does is

$$\left(5000 \left(1 + \frac{.05}{365} \right)^{365} \right) (20)$$

hierarchy of operations

Kristen wants to use an app:

It does work, but I suck @ apps.

TI 30 x ~~S~~ S

You want a calculator that displays entire expressions and has an edit feature.

```

N=
I/Y=0
PV=0
PMT=0
FV=0
P/Y=1
C/Y=1
PMT: [ ] [ ] BEGIN
    
```

$$5000 \left(1 + \frac{.05}{365}\right)^{365 \cdot 20}$$

```
(365*20)
13590.47834
5000(1+.05/360)^
(360*20)
13590.46542
500e^(.05*20)
1359.140914
```



} Continuous Compounding

missed a zero.

The number e: $e = \lim_{k \rightarrow \infty} \left(1 + \frac{1}{k}\right)^k$

limit, as $k \rightarrow \infty$
of ...

$$P \left(1 + \frac{r}{m}\right)^{mt}$$

$$= P \left(1 + \frac{1}{\frac{m}{r}}\right)^{\frac{m}{r} rt}$$

$\xrightarrow{\frac{m}{r} \rightarrow \infty} P e^{rt}$

#51-8 ALL, 9, 15, 19,
23, 25, 29, 33, 37,
39, 43, 47, 53, 57,
59, 61, 65, 71, 73,
75,
103, 105