

Homework Notes

Fall 2012 Test 1 Practice

Practice Tests Link

AND

$$|3x+2| < 7 \Rightarrow$$

$$-7 < 3x+2 < 7$$

is OK

OR

$$|3x+2| > 7 \Rightarrow$$

$$-7 > 3x+2 > 7$$

is NOT OK.

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$\frac{2}{3}x$  is not OK      $\frac{2}{3}x$  NOT OK

$\frac{2}{3}x$  is OK.      $\frac{2x}{3}$  is OK      $(\frac{2}{3})x$  is OK

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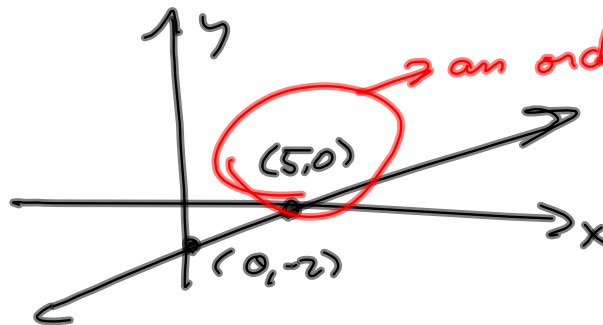
I might add a shared work problem.  
 otherwise, nothing different from  
 the CI Test you did.

## Homework Notes

I want ordered pair labels, not tickmarks

$$2x - 5y = 10$$

$$\begin{array}{r|l} x & y \\ \hline 0 & -2 \\ 5 & 0 \end{array}$$



→ an ordered (x, y)-pair.



Completing the square

$$x^2 + bx = x^2 + bx + \left(\frac{b}{2}\right)^2 - \frac{b^2}{4}$$

$$= \left(x + \frac{b}{2}\right)^2 - \frac{b^2}{4}$$

The cheat for getting  $f(x) = ax^2 + bx + c$   
in the form  $f(x) = a(x-h)^2 + k$

$$= a\left(x + \frac{b}{2a}\right)^2 + f\left(-\frac{b}{2a}\right)$$

$$f(x) = x^2 - 4x + 2$$

$$a=1, b=-4, c=2$$

$$-\frac{b}{2a} = -\frac{-4}{2(1)}$$

$$= 2 = h \text{ silly!}$$

$$f\left(-\frac{b}{2a}\right) = (-2)^2 - 4(-2) + 2 \text{ idiot!}$$

$$= 4 + 8 + 2 = 14 = k$$

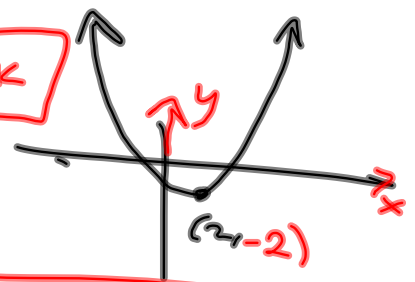
$$\text{So } f(x) = a(x-h)^2 + k$$

$$= 1(x - (-2))^2 - 2$$

$$= (x - 2)^2 - 2$$

$$(h, k) = (2, -2)$$

This is re-writing  
the expression  
for a quadratic  
function.



"Complete the square & write

$f(x)$  in the form  $a(x-h)^2 + k$ ."

Closely-related question:

Solve

$$x^2 - 4x + 2 = 0 \quad \text{by completing the square.}$$

$$x^2 - 4x = -2$$

$$x^2 - 4x + 2^2 = -2 + 4$$

$$(x-2)^2 = 2$$

$$x-2 = \pm\sqrt{2}$$

$$x = 2 \pm \sqrt{2} \Rightarrow x \in \{2 \pm \sqrt{2}\}$$

Using the cheat!

$$-\frac{b}{2a} = -\frac{-4}{2} = +2 = h$$

$$f\left(-\frac{b}{2a}\right) = 2^2 - 4(2) + 2$$

$$= 4 - 8 + 2$$

$$= -2 = k$$

So

$$x^2 - 4x + 2$$

$$= (x-2)^2 - 2$$

$$= (x-2)^2 - 2 \stackrel{\text{SET}}{=} 0$$

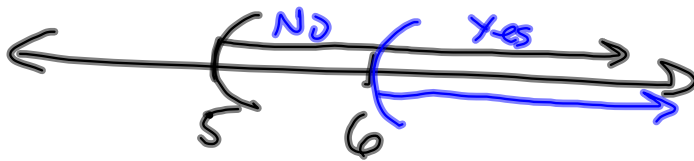
$$\rightarrow (x-2)^2 = 2, \text{ etc.}$$

Resources:

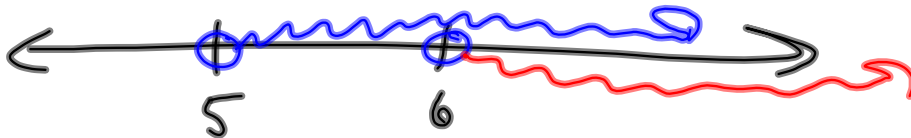
Practice Tests on Course Website  
Videos from Online

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$x > 5$  and  $x > 6$  means  $x > 6$

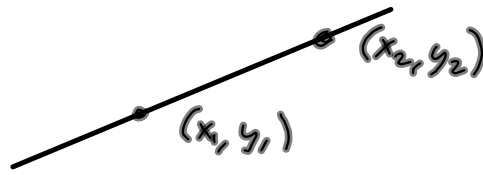


means  $x \in (6, \infty)$   
OR  $x \in \{x | x > 6\}$   
 $x = 6 \Rightarrow x \in \{6\}$ .



Lines

$$m = \frac{y_2 - y_1}{x_2 - x_1} = m$$



$$y_2 - y_1 = m(x_2 - x_1)$$

$$y - y_1 = m(x - x_1) \text{ is point-slope.}$$

$$y = m(x - x_1) + y_1$$

Line between  $(x_1, y_1) = (2, 3)$  &  $(x_2, y_2) = (-5, -2)$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-2 - 3}{-5 - 2} = \frac{-5}{-7} = \frac{5}{7}$$

$$y = m(x - x_1) + y_1$$

$$y = \frac{5}{7}(x - 2) + 3 \text{ STOP!}$$

$$\left(\frac{5}{7}\right)(-2) = \frac{5}{7} \cdot \frac{-2}{1} = \frac{-10}{7}$$

If I ask for AN equation.

The slope-intercept form:

$$y = \frac{5}{7}x - \frac{10}{7} + \frac{21}{7}$$

$$7 \left[ 3 = \frac{5}{7}(2) + b \right]$$

$$21 = 10 + 7b$$

$$11 = 7b$$

$$\frac{11}{7} = b$$

$$y = \frac{5}{7}x + \frac{11}{7}$$

$$y = \frac{5}{7}x + \frac{11}{7} \text{ is fine}$$



ANY Quadratic Equation, do the discriminant 1<sup>st</sup>.

Solve  $x^2 - 5x + 4 = 0$  by completing the square.

$$x^2 - 5x = -4 \quad a=1, b=-5, c=4$$

$$b^2 - 4ac = (-5)^2 - 4(1)(4) = 25 - 16 = 9 = 3^2 \Rightarrow \text{factors by AC.}$$

$$x^2 - 5x + \left(\frac{5}{2}\right)^2 = -4 + \frac{25}{4} = \frac{-16 + 25}{4} = \frac{9}{4}$$

$$\left(x - \frac{5}{2}\right)^2 = \frac{9}{4}$$

$$x - \frac{5}{2} = \pm \sqrt{\frac{9}{4}} = \pm \frac{\sqrt{9}}{\sqrt{4}} = \pm \frac{3}{2}$$

$$x = \frac{5}{2} \pm \frac{3}{2} \begin{matrix} \nearrow 4 \\ \searrow 1 \end{matrix} \Rightarrow x \in \{1, 4\}$$

Solve  $x^2 + 6x + 11 = 0$  by completing  
the square  
Solve... by quadratic formula.

Solve:

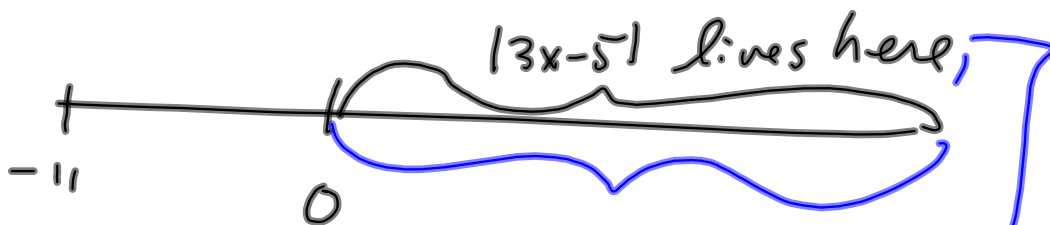
$$|3x-5| < 11 \quad |3x-5| > 11$$

$$|3x-5| \leq -11 \quad |3x-5| > -11$$

$\emptyset$

$$(-\infty, \infty)$$

$\mathbb{R}$



→ NO MATTER WHAT  $x$  IS!

$$x = -1000$$

$$|-3000-5| = |-3005| = 3005$$