

201 § 4.3 #5 1-10 ALL, 17, 45, 47, 49, 51, 53, 61,  
71, 75, 79, 81, 98  $\log(xy) = \log(x) + \log(y)$

- ① Log of the product is sum of the logs
- ② Log of the quotient is the difference of the logs  
 $\log(x/y) = \log(x) - \log(y)$
- ③ log of the power is that power times the log  
 $\log(a^x) = x \log(a) = \log(a) \times$
- ④ Change-of-base formula says  $\log_b x = \frac{\log_a x}{\log_a b}$

#s 5-10 Simplify

⑤  $e^{\ln(\sqrt{y})} = \boxed{\sqrt{y}}$

⑥  $10^{\log(3x+1)} = \boxed{3x+1}$

⑦  $\log(10^{y+1}) = \boxed{y+1}$

⑧  $\ln(e^{2k}) = \boxed{2k}$

⑨  $7^{\log_7(999)} = \boxed{999}$

⑩  $\log_4(2^{300}) = \log_4(2^{2 \cdot 150}) = \log_4(2^2)^{150}$   
 $= \log_4(4^{150}) = \boxed{150}$

121 § 4.3 #s 17, 45, 47, 49, 51, 53, 61, 71, 75, 79, 81, 98

#s 11-18 Write as a single log.

$$\textcircled{17} \ln(x^8) - \ln(x^3) = \ln\left(\frac{x^8}{x^3}\right) = \boxed{\ln(x^5)}$$

#s 19-26 Rewrite as sum/diff of logs

$$\text{---} \rightarrow 20 \log_3(xy) = \log_3(x) + \log_3(y)$$

#s 41-52 Rewrite as sum/diff of multiples of logs

$$\textcircled{45} \log(3\sqrt{x}) = \log(3x^{\frac{1}{2}}) = \log(3) + \log(x^{\frac{1}{2}}) \\ = \boxed{\log(3) + \frac{1}{2}\log(x)}$$

$$\textcircled{47} \log(3 \cdot 2^{x-1}) = \log(3) + \log(2^{x-1}) \\ = \boxed{\log(3) + (x-1)\log(2)}$$

$$\textcircled{49} \ln\left(\frac{\sqrt[3]{xy}}{t^{4/3}}\right) = \ln\left(\frac{(xy)^{\frac{1}{3}}}{t^{\frac{4}{3}}}\right) = \ln\left(\frac{x^{\frac{1}{3}}y^{\frac{1}{3}}}{t^{\frac{4}{3}}}\right)$$

$$= \ln(x^{1/3}) + \ln(y^{1/3}) - \ln(t^{4/3})$$

$$= \boxed{\frac{1}{3}\ln(x) + \frac{1}{3}\ln(y) - \frac{4}{3}\ln(t)}$$

121 54.3 #5 51, 53, 61, 71, 72, 73, 74, 75

$$\textcircled{51} \ln\left(\frac{6\sqrt{x-1}}{5x^3}\right) = \ln\left(\frac{6(x-1)^{\frac{1}{2}}}{5x^3}\right)$$

$$= \ln 6 + \ln(x-1)^{\frac{1}{2}} - \ln(5) - \ln(x^3)$$

$$= \ln(6) + \frac{1}{2} \ln(x-1) - \ln(5) - 3 \ln(x)$$

#553-62 Re-write as a single log.

$$\textcircled{53} \log_2(5) + 3 \log_2(x)$$

$$= \log_2(5) + \log_2(x^3)$$

$$= \log_2(5x^3)$$

$$\textcircled{61} 3 \log_4(x^2) - 4 \log_4(x^{-3}) + 2 \log_4(x)$$

$$= \log_4((x^2)^3) - \log_4((x^{-3})^4) + \log_4(x^2)$$

$$= \log_4(x^6) - \log_4(x^{-12}) + \log_4(x^2)$$

$$= \log_4\left(\frac{x^6 x^2}{x^{-12}}\right) = \log_4(x^8 x^{12}) = \log_4(x^{20})$$

12) #4, 8 #5 71, 75, 79, 81, 98

#5 71-76 Find each log to 4 decimal places

$$(71) \log_4(9) = \frac{\ln(9)}{\ln(4)} \approx 1.584962501 \approx \boxed{1.5850}$$

RECALL we had a  $\frac{\ln(3)}{\ln(2)}$  earlier  $\rightarrow$   $\uparrow$

Why the same #?

$$\frac{\ln(9)}{\ln(4)} = \frac{\ln(3^2)}{\ln(2^2)} = \frac{2\ln(3)}{2\ln(2)} = \frac{\ln(3)}{\ln(2)}$$

$$(75) \log_{1/2}(12) = \frac{\ln(12)}{\ln(1/2)} \approx -3.584962501$$
$$\approx \boxed{-3.5850}$$

#5 77-84 Solve round to 4 decimal places.

$$(79) (1.0001)^{365t} = 3.5$$

$$\ln((1.0001)^{365t}) = \ln(3.5)$$

$$\ln(1.0001)(365)t = \ln(3.5)$$

$$t = \frac{\ln(3.5)}{365\ln(1.0001)} \approx 34.32398919$$

$$\approx \boxed{34.3240}$$

121 § 4.3 #5 81, 98

(81)  $(1+r)^3 = 2.3$

$$\sqrt[3]{(1+r)^3} = \sqrt[3]{2.3}$$

$$1+r = \sqrt[3]{2.3}$$

$$r = \sqrt[3]{2.3} - 1$$

$$\approx 1.320006122$$

$$\approx \boxed{1.3200}$$

$$(1+r)^3 = 2.3$$

$$((1+r)^3)^{\frac{1}{3}} = 2.3^{\frac{1}{3}}$$

$$1+r = (2.3)^{\frac{1}{3}}$$

$$r = (2.3)^{\frac{1}{3}} - 1$$

(98) 1960 → \$.49  
2009 → \$4.59

Find annual growth rate.

Madison said compound annually.

I said compound continuously.

Book likes Madison more.

Let  $t = \#$  of years after 1960.

Then  $P(1 + \frac{r}{m})^{mt} = .49(1+r)^t$   $m=1$   
Madison

Now  $2009 - 1960 = 49 = t \rightarrow$

$$.49(1+r)^{49} = 4.59$$

$$(1+r)^{49} = \frac{4.59}{.49}$$

$$\sqrt[49]{(1+r)^{49}} = \sqrt[49]{\frac{4.59}{.49}}$$

solve for  $r$

$$1+r = \sqrt[49]{\frac{4.59}{.49}}$$

$$r = \sqrt[49]{\frac{4.59}{.49}} - 1$$

$$\approx .0467161145$$
  
$$\approx .0467 \text{ or } \boxed{4.67\%}$$

121 S<sup>4.4</sup> # 98

(98) Compounded continuously version

$$Pe^{rt} = .49e^{rt}$$

$$.49e^{49r} = 5.49$$

$$e^{49r} = \frac{5.49}{.49}$$

$$\ln(e^{49r}) = \ln\left(\frac{5.49}{.49}\right)$$

$$49r = \ln\left(\frac{5.49}{.49}\right)$$

$$r = \frac{\ln\left(\frac{5.49}{.49}\right)}{49} \approx .0493117988$$

$$\approx .0493$$

Note it takes  
HIGHER rate compounded  
continuously?!

OR  
4.93%

Something must be wrong, Continuous  
compounding grows faster with same  $r$ .

So why does it need a BIGGER  $r$ ?

Can somebody help with this?

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