

121 $\sum 3, 3 \# 5, 15, 17, 19, 23, 31, 33, 39$

#5 15-22 Find the product $\underline{\underline{i^2 = -1}}$

$$\textcircled{15} (x-3i)(x+3i) = x^2 - (3i)^2 = x^2 - 3^2 i^2$$
$$\underline{(a-b)(a+b) = a^2 - b^2} \quad \boxed{x^2 + 9}$$

$$\textcircled{17} (x - (1 + \sqrt{2}i))(x - (1 - \sqrt{2}i))$$
$$= x^2 - (1 - \sqrt{2}i)x - (1 + \sqrt{2}i)x + (1 + \sqrt{2}i)(1 - \sqrt{2}i)$$
$$= x^2 - x + \sqrt{2}ix - x - \sqrt{2}ix + 1^2 - (\sqrt{2})^2$$
$$= x^2 - 2x + 1 - 2 = \boxed{x^2 - 2x - 1}$$

$$\textcircled{19} (x - (3 + 2i))(x - (3 - 2i))$$
$$\boxed{M1} = x^2 - (3 - 2i)x - (3 + 2i)x + (3 + 2i)(3 - 2i)$$
$$= x^2 - 3x + 2ix - 3x - 2ix + 3^2 - (2i)^2$$
$$= x^2 - 6x + 9 - 4i^2$$
$$= x^2 - 6x + 9 + 4$$
$$= \boxed{x^2 - 6x + 13}$$

$$\boxed{M2} (x - 3 - 2i)(x - 3 + 2i)$$
$$= x^2 - 3x + 2ix - 3x + 9 - 6i - 2ix + 6i - 4i^2$$
$$= x^2 - 6x + 9 + 4$$
$$= \boxed{x^2 - 6x + 13}$$

(121) § 3.3 # 823, 31, 33, 39

#523-42 Find polynomial eq'n with real coefficients that has the given roots

(23) $-3, 5 \Rightarrow (x+3)(x-5) = 0$

(31) $0, i\sqrt{3} \Rightarrow \underbrace{x(x-i\sqrt{3})(x-(-i\sqrt{3})) = 0}_{\text{CAT}}$

(33) $3, 1-i \Rightarrow (x-3)(x-(1-i))(x-(1+i)) = 0$

(39) $\frac{1}{2}, \frac{1}{3}, \frac{1}{4} \Rightarrow (x-\frac{1}{2})(x-\frac{1}{3})(x-\frac{1}{4}) = 0$

Further Probs.

543, 47, 51, 61, 65, 67, 69*, 70*

* Quadratic in Form