

3.4 #41

$$\left(\frac{2c-3}{5}\right)^2 + 2\left(\frac{2c-3}{5}\right) = 8$$

is quadratic
in $u = \frac{2c-3}{5}$

$$\boxed{\text{Let } u = \frac{2c-3}{5}}. \text{ Then}$$

$$u^2 + 2u = 8$$

$$u^2 + 2u - 8 = 0$$

$$(u+4)(u-2) = 0$$

$$u = -4 \text{ OR } u = 2$$

$$AB = 0 \implies A = 0 \text{ OR } B = 0$$

$$\frac{2c-3}{5} = -4 \quad \frac{2c-3}{5} = 2$$

$$2c-3 = -20$$

$$2c-3 = 10$$

$$2c = -17$$

$$2c = 13$$

$$c = -\frac{17}{2} \text{ OR } c = \frac{13}{2}$$

$$c \in \left\{-\frac{17}{2}, \frac{13}{2}\right\}$$

3.4

$$\textcircled{7} \quad 3y^4 - 12y^2 = 0$$

$$3y^2(y^2 - 4) = 0$$

$$3y^2 = 0 \quad \text{OR} \quad y^2 - 4 = 0$$

$$y^2 = 0 \quad (y+2)(y-2) = 0$$

$$y = \pm 0 \quad y = -2 \quad \text{OR} \quad y = 2$$

$$y \in \{-2, 0, 2\}$$

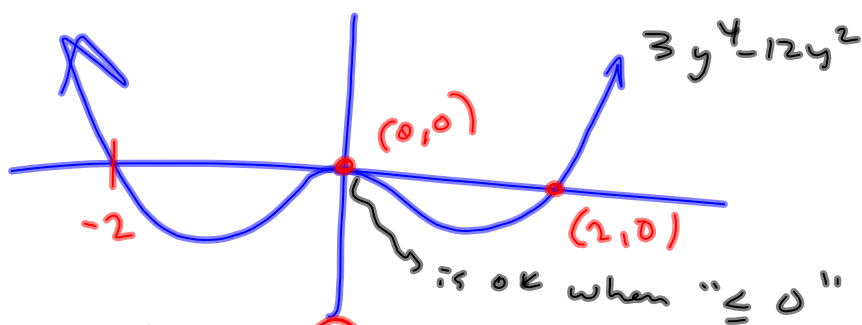
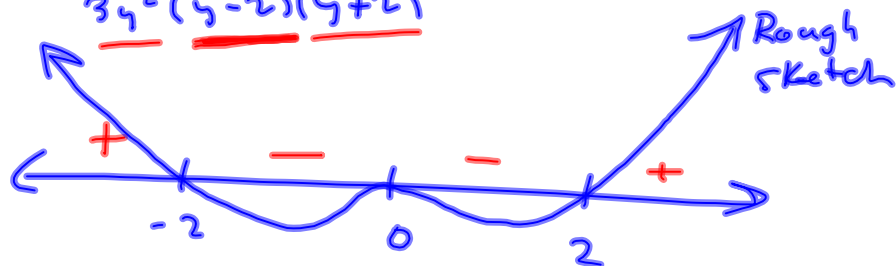
$y = 0, \pm 2$ are only 3 zeros
What up wit' dat?

$$3y^2(y^2 - 4) = 3y^2(y-2)(y+2)$$

$y = 0$ is a root of multiplicity 2

Tie-together w/ graphing

$$3y^2(y-2)(y+2)$$



Solve $3y^4 - 12y^2 < 0$

$$y \in [-2, 0) \cap (0, 2] = \emptyset \quad \text{No}$$

$$(-2, 0) \cup (0, 2) \quad \text{Yes}$$

$$3y^4 - 12y^2 \leq 0$$

$$[-2, 0] \cup [0, 2] = [-2, 2]$$

§ 3.4 #35

$x^4 - 12x^2 + 27 = 0$ is quadratic in $u = x^2$

Let $u = x^2$

$u^2 - 12u + 27 = 0$ etc.
 $x^2 = 3$ OR $x^2 = 9$

$x^{\frac{2}{3}} - 12x^{\frac{1}{3}} + 27 = 0$
 Let $u = x^{\frac{1}{3}}$

$u^2 - 12u + 27 = 0$

$u = 3$ OR $u = 9$

$x^{\frac{1}{3}} = 3$ OR $x^{\frac{1}{3}} = 9$

$(x^{\frac{1}{3}})^3 = 3^3$ $x = 9^3$

$x = 27$ $x = 729$

$\ln x = \log_e x$

$\frac{81}{729}$

$\ln(x^{\frac{1}{3}}) = \ln(3)$

$\frac{1}{3} \ln(x) = \ln(3)$

$\ln(x) = 3 \ln(3) = \ln(3^3)$

$e^{\ln(x)} = e^{\ln(3^3)}$

$x = 3^3$

$\log(xy) = \log x + \log y$

9.7 Computer

$\log(9 \cdot 7)$ turns products into sums
 $= \log 9 + \log 7$

$\log(x^y) = y \log x$

It adds.
 Then takes the inverse log.

(11)

$$\sqrt{x+1} = x-5$$

$$(x+1)^{\frac{1}{2}} = x-5$$

$$\begin{array}{r} x+1 \\ -x-1 \\ \hline \end{array} = \begin{array}{r} (x-5)^2 \\ = \\ -x-1 \end{array} = x^2 - 10x + 25$$

$$0 = x^2 - 11x + 24 = 0$$

$$(x-8)(x-3) = 0$$

$$x \in \{3, 8\}$$

$$\left(\left(\right)^{\frac{1}{2}}\right)^2$$

Fact: $A = B \Rightarrow$

$$A^2 = B^2$$

But

$$A^2 = B^2 \Rightarrow$$

$$A = B$$

$$(-3)^2 = 9 = 3^2$$

But

$$-3 \neq +3$$

Squaring both sides is like casting a net.

Sometimes we have to throw a fish back.

(11)

$$\sqrt{x+1} = x-5 \implies$$

$$(x+1)^{\frac{1}{2}} = x-5 \implies$$
~~$$x+1 = (x-5)^2 = x^2 - 10x + 25 \implies$$

$$-x-1 = -x-1$$~~

$$0 = x^2 - 11x + 24 = 0$$

$$(x-8)(x-3) = 0$$

$x \in \{3, 8\}$

{8} is extraneous root.
x=3 is extraneous root.

CHECK!

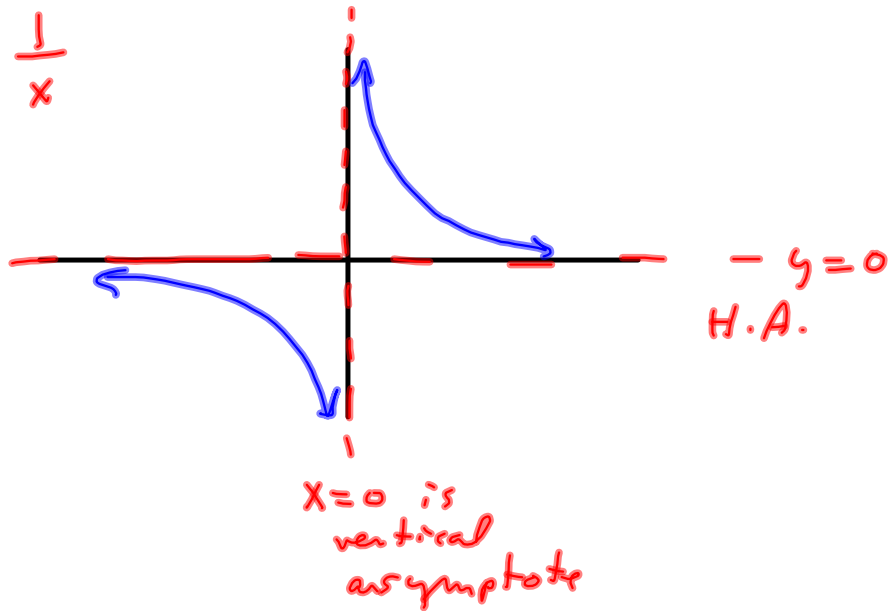
$$\sqrt{3+1} = 3-5$$

$$2 = \sqrt{4} = -2 \quad \text{New P}$$

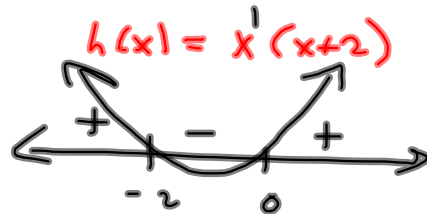
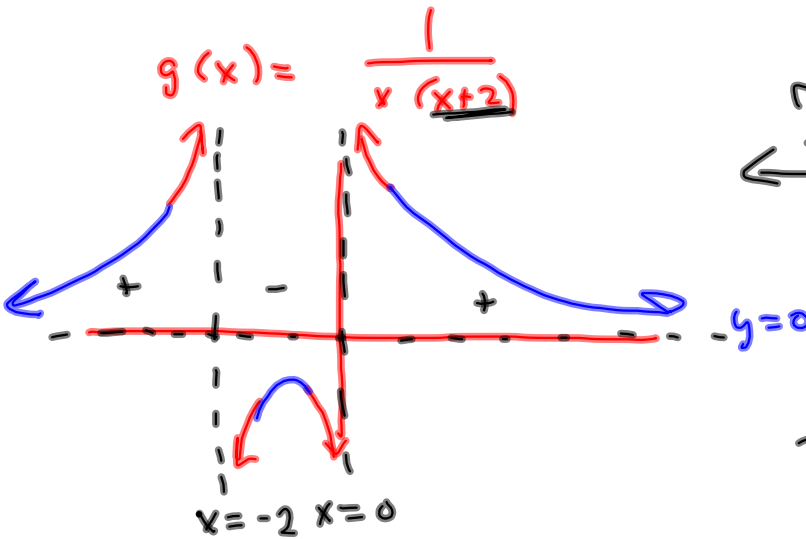
$$\sqrt{8+1} \stackrel{?}{=} 8-5$$

$$3 = 3 \quad \checkmark$$

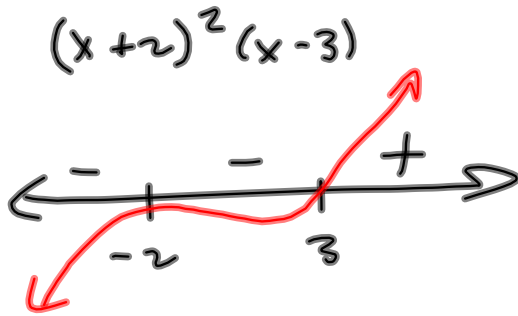
$f(x) = \frac{1}{x}$



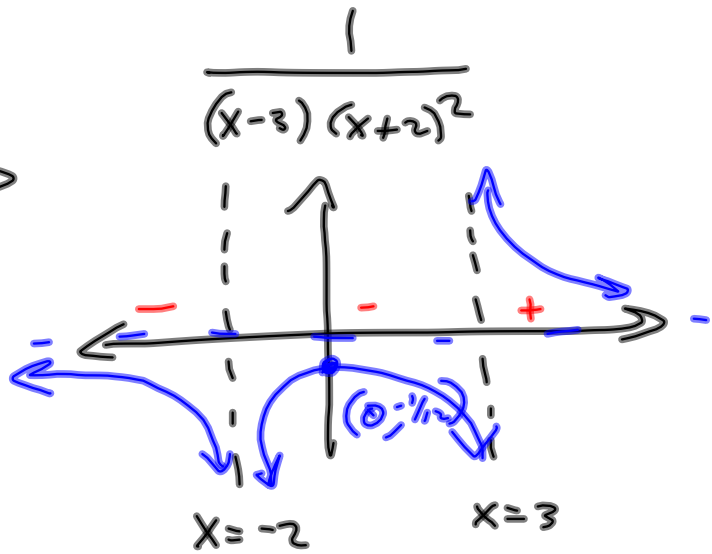
$g(x) = \frac{1}{x(x+2)}$



$\frac{1}{\dots\dots\dots\dots\dots\dots\dots}$ is
BIG



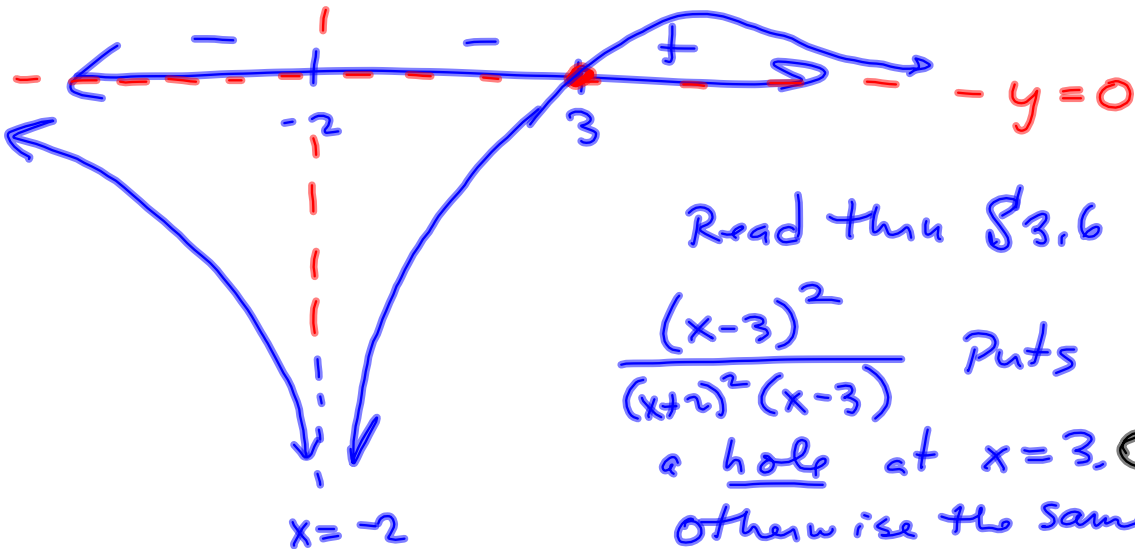
$y=0$



$$\frac{x-3}{(x+2)^2}$$

$= \frac{x}{x^2 + \text{smaller}}$

why is $y=0$ a Horizontal asymptote?
Because x^2 outstrips x



Read thru §3.6

$\frac{(x-3)^2}{(x+2)^2(x-3)}$ Puts
a hole at $x=3$. ○
otherwise the same.