

1. (10 pts) $f = \{(2,-1), (3,-2), (4,2), (3,4)\}$

a. Function? (Yes/no) *NO*

b. If not, why not? *x=3 is paired with y = -2 & y = 4*

c. If it is a function, is it 1-to-1? (Yes/no) *X*

d. If it is not 1-to-1, why not? *X Not Func 1*

e. Domain? *{2, 3, 4}*

f. Range? *{-1, -2, 2, 4}*

2. (5 pts) $g = \{(2,-2), (4,6), (3,2), (11,5)\}$

a. Function? (Yes/no) *Yes*

b. If not, why not? *X*

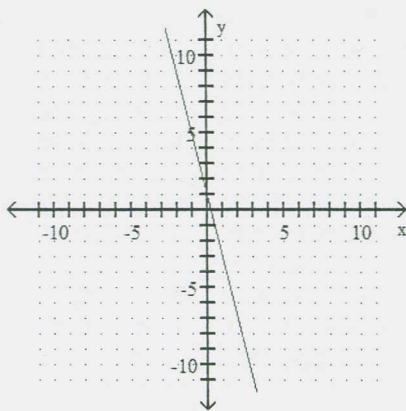
c. If it is a function, is it 1-to-1? (Yes/no) *Yes*

d. If it is not 1-to-1, why not? *X*

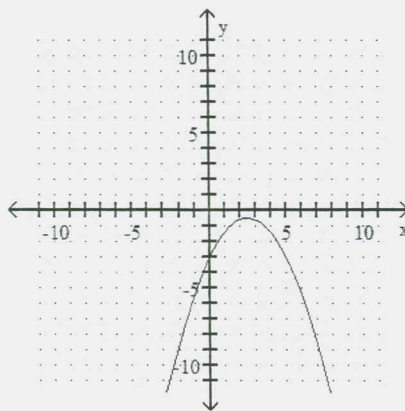
e. Domain? *{2, 4, 3, 11}*

f. Range? *{-2, 6, 2, 5}*

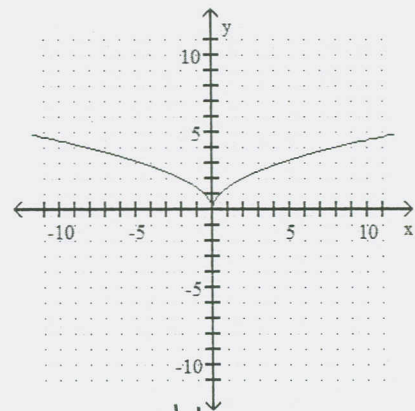
3. (5 pts) Use the horizontal line test to determine if the following functions are 1-to-1 (Yes/No for each graph).



Yes



No



No

4. (5 pts) Determine whether or not $|y-2|+x=7$ defines y as a function of x . If it does not, show/explain why not.

$$|y-2| = -x+7$$

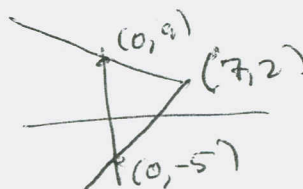
$$y-2 = -x+7 \quad \text{OR} \quad y-2 = x-7$$

$$y = -x+9 \quad \text{OR} \quad y = x-5$$

This gives 2 y -values for each x -value.

Eg $x=1 \rightsquigarrow (1,8), (1,-4)$

$$x = 7 - |y-2|$$



5. (10 pts) Let $f(x) = x^2 - 5$. Simplify the difference quotient $\frac{f(x+h) - f(x)}{h}$.

$$\frac{f(x+h) - f(x)}{h} = \frac{(x+h)^2 - 5 - (x^2 - 5)}{h}$$

$$= \frac{x^2 + 2xh + h^2 - 5 - x^2 + 5}{h}$$

$$= \frac{2xh + h^2}{h} = \frac{h(2x+h)}{h} = \boxed{2x+h}$$

6. Let $f(x) = 3x - 5$ and $g(x) = \sqrt{x+7}$.

a. (5 pts) What is the domain of f ? (Use Interval Notation.)

$$(-\infty, \infty)$$

b. (5 pts) What is the domain of g ? (Use Interval Notation.)

Need $x+7 \geq 0 \implies x \geq -7 \implies \mathcal{D} = [-7, \infty)$

c. Determine each of the following functions and state the domain of each in interval notation.

i. (5 pts) $(f+g)(x)$

$$= 3x - 5 + \sqrt{x+7}$$

$$\mathcal{D} = [-7, \infty)$$

ii. (5 pts) $\left(\frac{g}{f}\right)(x)$

$$= \frac{\sqrt{x+7}}{3x-5}$$

Need $x \geq -7$ and $3x-5 \neq 0$
 $x \neq \frac{5}{3}$

$$\mathcal{D} = [-7, \frac{5}{3}) \cup (\frac{5}{3}, \infty)$$



iii. (5 pts) $(f \circ g)(x)$

$$= f(g(x))$$

$$= f(\sqrt{x+7})$$

$$= 3\sqrt{x+7} - 5$$

$$\mathcal{D} = \{x \mid \underbrace{x \in \mathcal{D}(g)}_{[-7, \infty)} \cap \underbrace{g(x) \in \mathcal{D}(f)}_{(-\infty, \infty)}\}$$

$$= [-7, \infty)$$

iv. (5 pts) $(g \circ f)(x)$

$$= g(f(x))$$

$$= g(3x-5) = \sqrt{3x-5+7}$$

$$= \sqrt{3x+2}$$

Need $3x+2 \geq 0$
 $\implies 3x \geq -2$
 $x \geq -\frac{2}{3}$

$$[-\frac{2}{3}, \infty)$$

7. (5 pts) Show that $f(x) = \frac{x+1}{x-3}$ is 1-to-1.

$$\S f(x_1) = f(x_2)$$

$$\frac{x_1+1}{x_1-3} = \frac{x_2+1}{x_2-3}$$

$$(x_1+1)(x_2-3) = (x_2+1)(x_1-3)$$

$$\underline{-3 + x_1} \quad \underline{x_2 - 3x_1 + x_2} = \underline{x_1 x_2 - 3x_2 + x_1} \quad \underline{-3}$$

$$-3x_1 + x_2 = -3x_2 + x_1$$

$$-4x_1 = -4x_2$$

$$x_1 = x_2 \quad \square$$

8. (5 pts) Let $f(x) = \frac{x+1}{x-3}$. Find $f^{-1}(x)$.

$$x = \frac{y+1}{y-3} \quad f$$

$$x(y-3) = y+1$$

$$xy - 3x = y + 1$$

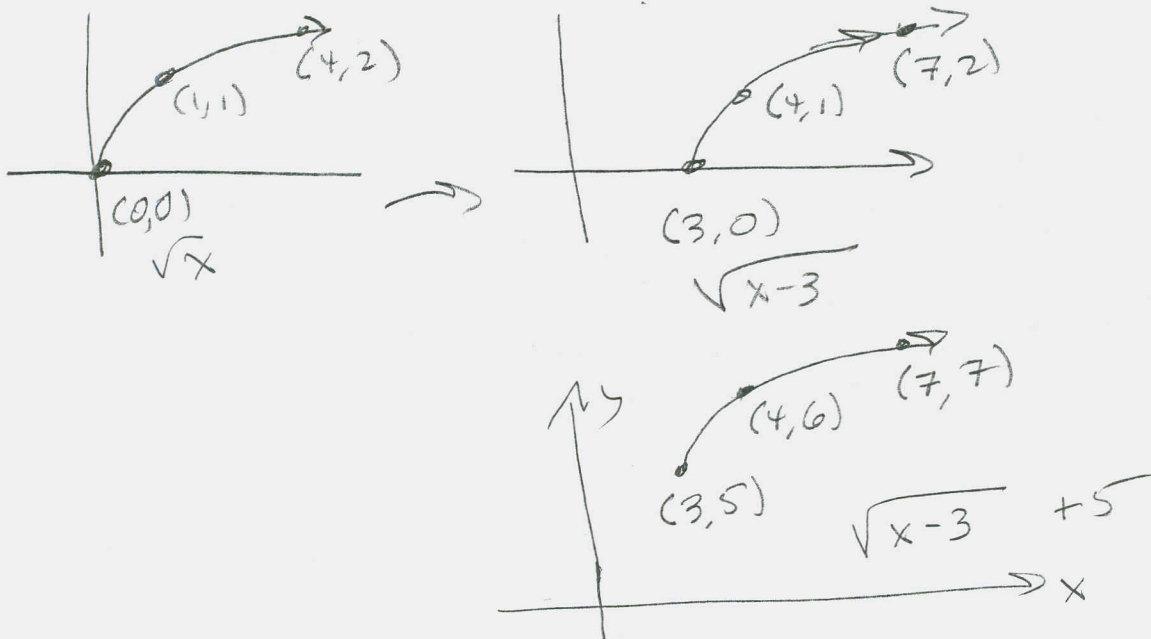
$$xy - y = 3x + 1$$

$$y(x-1) = 3x+1$$

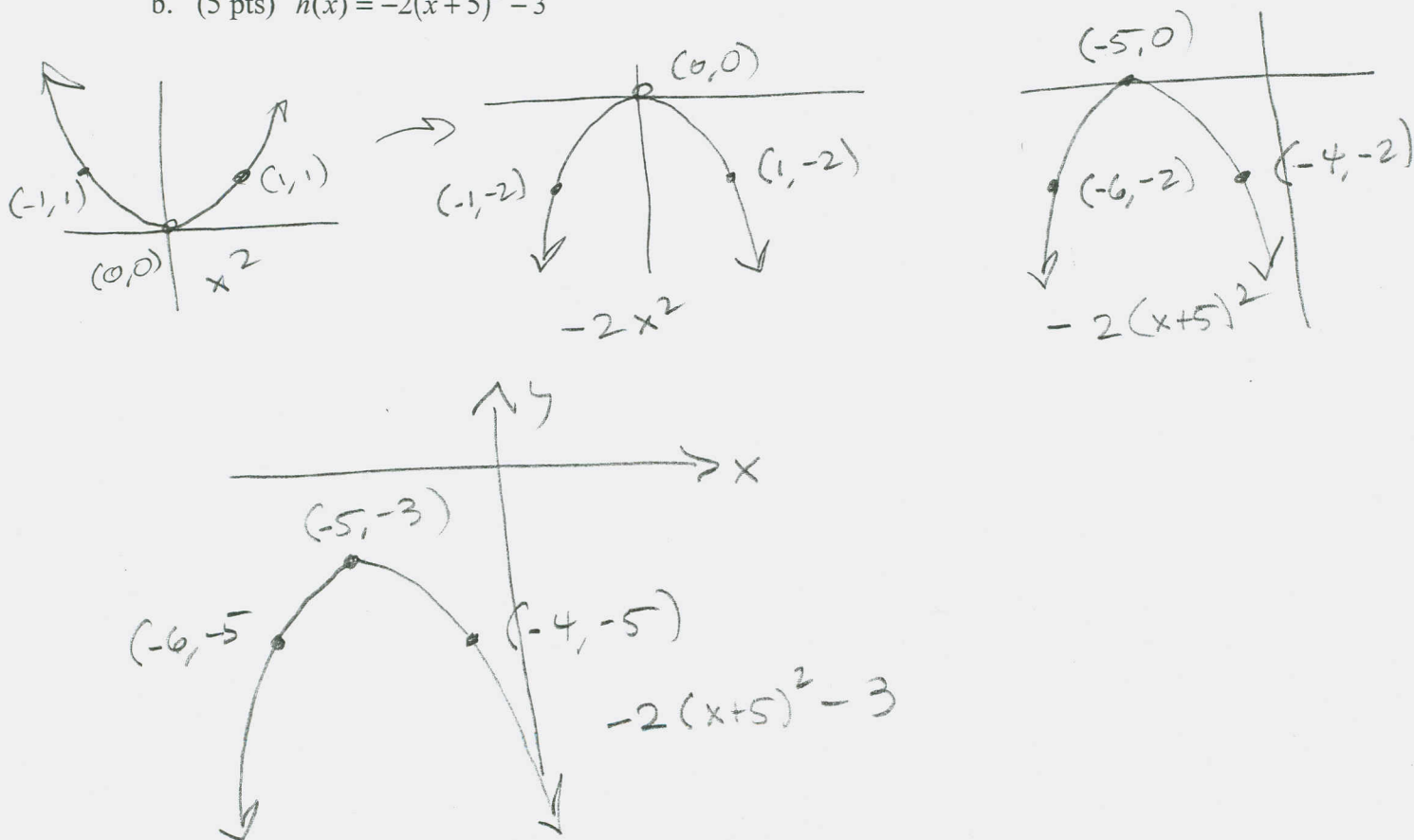
$$\boxed{f^{-1}(x) = \frac{3x+1}{x-1}}$$

9. Graph each of the following functions using techniques of shifting, compressing, stretching, and/or reflecting. Start with the graph of the basic function and show all stages in separate sketches. Track 3 key points through the transformations.

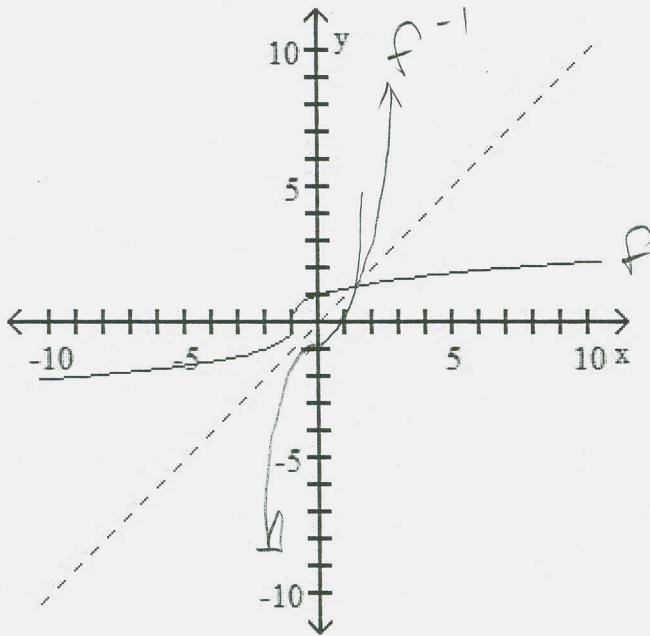
a. (5 pts) $g(x) = \sqrt{x-3} + 5$



b. (5 pts) $h(x) = -2(x+5)^2 - 3$



10. (5 pts) The graph of f is given. Sketch the graph of f^{-1} .



11. (5 pts) If f varies jointly as q^2 and h , and $f = -36$ when $q = 3$ and $h = 2$, find f when $q = 4$ and $h = 2$.

$$\begin{aligned}
 f &= kq^2h \\
 -36 &= k \cdot 3^2 \cdot 2 \\
 -36 &= 18k \\
 -\frac{36}{18} &= k = -2
 \end{aligned}$$

$$f = -2q^2h$$

$$f = -2(4^2)(2)$$

$$= -(4)(16)$$

$$= -64 = f$$

$$f = -64$$

12. (5 pts) Find the inverse of $f(x) = 3x - 7$

$$x = 3y - 7 = x$$

$$3y = x + 7$$

$$y = \frac{x+7}{3}$$

$$y = f^{-1}(x) = \frac{1}{3}x + \frac{7}{3}$$