

Solve $3.2x^2 - 7.1x - 2.5 = 0$

$a = 3.2, b = -7.1, c = -2.5$

Discriminant $b^2 - 4ac = (-7.1)^2 + 4(3.2)(+2.5)$
 $=$

Write
much
Think
little.

$7.1^2 + 4 * 3.2 * 2.5 = 82.41$

$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(-7.1) \pm \sqrt{82.41}}{2(3.2)}$

$= \frac{7.1 \pm \sqrt{82.41}}{6.4} =$

$\frac{7.1 + \sqrt{82.41}}{6.4}$ $\frac{7.1 - \sqrt{82.41}}{6.4}$

Get a TI30II

etc.

2.5278117770982956292137714253857

$(7.1 + \sqrt{(82.41)}) / 6.4$

$$|2x-3| > -5$$

 \mathbb{R}

$$|2x-3| > 5$$

$$2x-3 > 5 \text{ OR } 2x-3 < -5$$

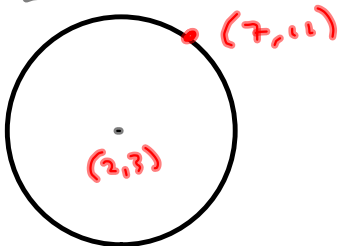
$$|2x-3| < -5$$

 \emptyset

$$|2x-3| < 5$$

$$2x-3 < 5 \text{ AND } 2x-3 > -5$$

Equation of the circle with center $(2, 3) = (2, 3)$ and point $(7, 11)$.
 Standard Form $(x-h)^2 + (y-k)^2 = r^2$



$$\begin{aligned} r &= \sqrt{(7-2)^2 + (11-3)^2} \\ &= \sqrt{5^2 + 8^2} \\ &= \sqrt{25 + 64} \\ &= \sqrt{89} \end{aligned}$$

$$(x-2)^2 + (y-3)^2 = 89$$

Solve by completing the square.

$$3x^2 + 2x - 7 = 0$$

Bonus.

$$x^2 + \frac{2}{3}x = \frac{7}{3}$$

$$\left(\frac{1}{3}\right)^2 = \frac{1^2}{3^2} = \frac{1}{9}$$

$$x^2 + \frac{2}{3}x + \left(\frac{1}{3}\right)^2 = \frac{7}{3} + \frac{1}{9} = \frac{21+1}{9} = \frac{22}{9}$$

$$\sqrt{\left(x + \frac{1}{3}\right)^2} = \sqrt{\frac{22}{9}}$$

$$x + \frac{1}{3} = \pm \sqrt{\frac{22}{9}} = \pm \frac{\sqrt{22}}{\sqrt{9}} = \pm \frac{\sqrt{22}}{3}$$

$$x = -\frac{1}{3} \pm \frac{\sqrt{22}}{3} \quad \left\{ -\frac{1}{3} \pm \frac{\sqrt{22}}{3} \right\}$$

$$x^2 + 5x = 11$$

$$x^2 + 5x + \left(\frac{5}{2}\right)^2 = 11 + \frac{25}{4}$$

$$\left(x + \frac{5}{2}\right)^2 = \frac{69}{4}$$

Line thru $(2, 3)$ & $(7, 11)$
 (x_1, y_1) (x_2, y_2)

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{11 - 3}{7 - 2} = \frac{8}{5}$$

$$y - y_1 = m(x - x_1)$$

$$\left(\frac{8}{5}\right)\left(\frac{7}{1}\right) = \frac{16}{5}$$

$$y = m(x - x_1) + y_1 \quad \text{My version of point + slope}$$

$$y = \frac{8}{5}(x - 2) + 3$$

Point-Slope

$$y = m(x - x_1) + y_1$$

$$= \frac{8}{5}x - \frac{16}{5} + 3 \cdot \frac{5}{5}$$

$$= \frac{8}{5}x - \frac{16}{5} + \frac{15}{5}$$

$$y = \frac{8}{5}x - \frac{1}{5}$$

Slope-Intercept

$$y = mx + b$$

$$5y = 8x - 1$$

$$-8x + 5y = -1$$

General Form.
 $Ax + By = C$

For the litigators

Nate sez
 this $\rightarrow 8x - 5y = 1$
 It's in the fine print.

$$x^2 - 6x - 40 = 0$$

- ① Solve by factoring:
 ② quadratic formula:
 ③ completing the square

①

$$\begin{aligned} -(x+4)(x-10) &= 0 \\ x+4 &= 0 \text{ OR } x-10 = 0 \\ x &= -4 \text{ OR } x = 10 \end{aligned}$$

②

$$\begin{aligned} a &= 1, b = -6, c = -40 \\ b^2 - 4ac &= (-6)^2 - 4(1)(-40) \\ &= 36 + 160 \\ &= 196 = 14^2 \Rightarrow \text{I+ factors} \end{aligned}$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{6 \pm \sqrt{196}}{2(1)} = \frac{6 \pm 14}{2}$$

$$x = -4, 10 \Rightarrow$$

$$-(x+4)(x-10) = x^2 - 6x - 40$$

Factor Theorem. Chapter 3.

we cheated:

use quadratic formula to find roots.
use roots to find factors.

③ $x^2 - 6x - 40 = 0$

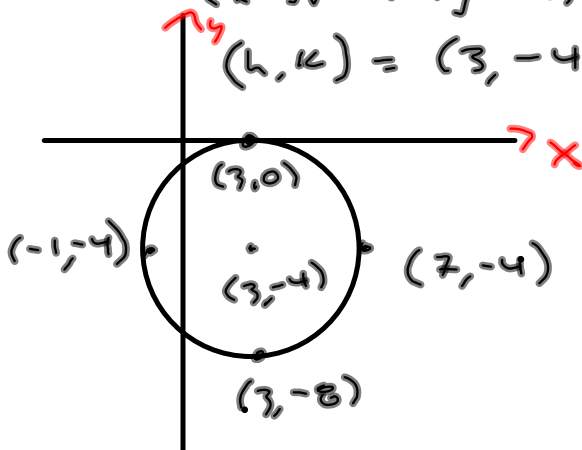
Graph the circle

$$x^2 + y^2 - 6x + 8y = -9$$

$$x^2 - 6x + 3^2 + y^2 + 8y + 4^2 = -9 + 9 + 16$$

$$(x-3)^2 + (y+4)^2 = 16$$

$$(h, k) = (3, -4), r = 4$$



$$\frac{4}{x-1} - \frac{9}{x+1} = \frac{3}{x^2-1} \quad \text{LCD} = (x-1)(x+1)$$

$$(x-1)(x+1)$$

Method 1

$$(x-1)(x+1) \cdot \frac{4}{x-1} - (x-1)(x+1) \cdot \frac{9}{x+1} = (x-1)(x+1) \cdot \frac{3}{(x-1)(x+1)}$$

$$4(x+1) - 9(x-1) = 3 \quad *$$

$$4x + 4 - 9x + 9 = 3$$

$$-5x + 13 = 3$$

$$-5x = -10$$

$$x = 2$$

Method 2

Slower but more versatile.

$$\frac{4}{x-1} - \frac{9}{x+1} = \frac{3}{x^2-1} \quad \text{LCD} = (x-1)(x+1)$$

$$(x-1)(x+1)$$

$$\left(\frac{4}{x-1}\right) \frac{(x+1)}{(x+1)} - \left(\frac{9}{x+1}\right) \frac{(x-1)}{(x-1)} = \frac{3}{(x-1)(x+1)}$$

$$\frac{4x+4}{\text{LCD}} - \frac{9(x-1)}{\text{LCD}} = \frac{3}{\text{LCD}} \quad \text{All over LCD.}$$

$$4x + 4 - 9x + 9 = 3$$

Ditch LCD.