

$$(x+2)(x+2) = x^2 + 4x + 4 = x^2 + 4x + 2^2$$

$$(x+3)(x+3) = x^2 + 6x + 9 = x^2 + 6x + 3^2$$

$$(x-7)(x-7) = x^2 - 14x + 49 = x^2 - 14x + 7^2$$

$$(x-11)(x+11) = x^2 - 121 =$$

$$(x-11)(x-11) = x^2 - 22x + 121 = x^2 - 22x + 11^2$$

Complete the square

$$y = x^2 - 8x + \underline{0}$$

$$\frac{8}{2} = 4 \rightsquigarrow 4^2$$

$$y = x^2 - 8x + 4^2 - 16$$

$$y = (x-4)^2 - 16$$

$$\text{Vertex } x = (h, k) = (4, -16)$$

$$\text{Axis of symmetry: } x=4$$

$$\text{Increasing: } x \in [4, \infty)$$

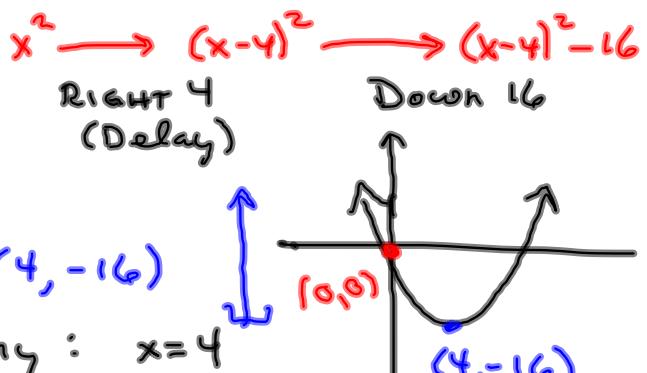
$$\text{Decreasing: } x \in (-\infty, 4]$$

$$\mathcal{D} = (-\infty, \infty)$$

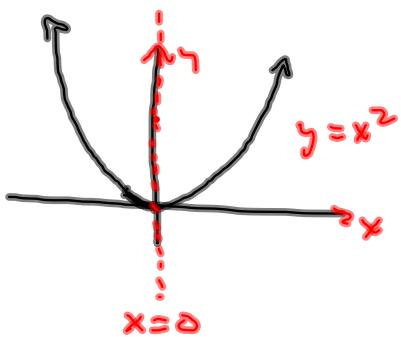
$$\mathcal{R} = \{y \mid y = f(x) \text{ for some } x \in \mathcal{D}\}$$

$$= [-16, \infty)$$

Min value is  $y = -16$  @  $x = 4$



$\left. \begin{array}{l} \text{x-values for} \\ \text{which the desired} \\ \text{trait is manifest,} \end{array} \right\}$



Ax's  
of  
Symmetry:  $x=0$   
 $D = \mathbb{R}$   
 $R = [0, \infty)$   
Inc:  $[0, \infty)$   
Dec:  $(-\infty, 0]$   
 $(h, k) = (0, 0)$

(14)

$$2(x-h)^2 + 1 <$$

$$y = \underline{3x^2 - 12x + 1} \rightarrow (0, 1)$$

$$y = 3(x^2 - 4x) + 1$$

$$y = 3(x^2 - 4x + 2^2 - 4) + 1$$

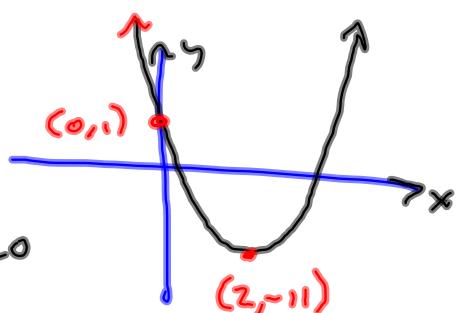
$$= 3(x^2 - 4x + 2^2) + 3(-4) + 1$$

$$= 3(x-2)^2 - 12 + 1$$

$$= 3(x-2)^2 - 11$$

Good enough for #s 9-20

Roughed it in.



#s 21-24  
Find the vertex

(22)  $f(x) = -2x^2 - 8x + 9$

$$a = -2, b = -8, c = 9$$

$$-\frac{b}{2a} = -\frac{-8}{2(-2)} = -2$$

$$\begin{aligned} f\left(-\frac{b}{2a}\right) &= -2(-2)^2 - 8(-2) + 9 \\ &= -8 + 16 + 9 \\ &= 17 \end{aligned}$$

My Way:

$$f(x) = -2x^2 - 8x + 9$$

$$= -2(x^2 + 4x + 2^2 - 4) + 9$$

$$= -2(x+2)^2 + \underbrace{8+9}_{17}$$

Using  $-\frac{b}{2a}$  to obtain

$$\begin{aligned} &-2(x+2)^2 + 17 \\ &a(x-h)^2 + k \end{aligned}$$

-2	-2	-8	9
		4	8
-2	-4	<u>17</u>	

$f(-2)$

$$(h, k) = (-2, 17)$$

#5 41-52 is really about a complete graph. All intercepts, etc.

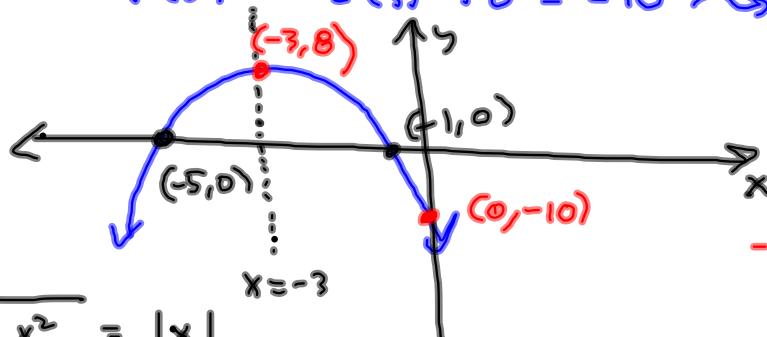
3 (50)

$$y = -2(x+3)^2 + 8 = f(x)$$

$$(h, k) = (-3, 8)$$

opens down

$$f(0) = -2(3)^2 + 8 = -10 \rightarrow (0, -10)$$



$$\sqrt{x^2} = |x|$$

$$(\sqrt{x})^2 = x,$$

and the assumption going in is that  $x \geq 0$ , lest  $\sqrt{x}$  be nonreal.

$$\sqrt{(x+3)^2} = \sqrt{4}$$

$$|x+3| = 2$$

$$x+3 = \pm 2$$

$$\begin{aligned} x+3 &= 2 \\ -2(x+3)^2 + 8 &= 0 \end{aligned}$$

$$-2(x+3)^2 = -8$$

$$(x+3)^2 = 4$$

$$x+3 = \pm 2$$

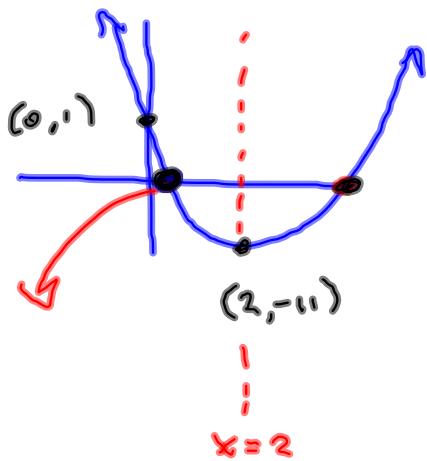
$$x = -3 \pm 2$$

$$x = -1 \text{ or } x = -5$$

$$(-1, 0), (-5, 0)$$

Let's do the same thing for an uglier one.

$$\begin{aligned}
 y &= 3x^2 - 12x + 1 \\
 &= 3(x^2 - 4x + 2^2 - 4) + 1 \\
 &= 3(x-2)^2 - 11
 \end{aligned}$$



because

$$\begin{aligned}
 x-\text{int}: \\
 3(x-2)^2 - 11 &= 0 \\
 3(x-2)^2 &= 11 \\
 (x-2)^2 &= \frac{11}{3} \\
 x-2 &= \pm \sqrt{\frac{11}{3}} \\
 x &= 2 \pm \sqrt{\frac{11}{3}} \\
 &= 2 \pm \frac{\sqrt{33}}{3}
 \end{aligned}$$