

099 Practice Final Solutions

① $\sqrt{94500}$

$$= \sqrt{2^2 \cdot 3^3 \cdot 5^3 \cdot 7}$$

$$= \sqrt{2^2 \cdot 3^{2+1} \cdot 5^{2+1} \cdot 7}$$

$$= \sqrt{2^2 \cdot 3^2 \cdot 3 \cdot 5^2 \cdot 5 \cdot 7}$$

$$= 2^{\frac{2}{2}} \cdot 3^{\frac{2}{2}} \cdot 5^{\frac{2}{2}} \sqrt{3 \cdot 5 \cdot 7}$$

$$= 2 \cdot 3 \cdot 5 \sqrt{105} = \boxed{30\sqrt{105}}$$

$$\begin{array}{r} 2 \overline{) 94500} \\ \underline{2 \overline{) 47250}} \\ 3 \overline{) 23625} \\ \underline{3 \overline{) 7875}} \\ 3 \overline{) 2625} \\ \underline{5 \overline{) 875}} \\ 5 \overline{) 175} \\ \underline{5 \overline{) 35}} \\ 7 \end{array}$$

$$\begin{array}{r} 2 \overline{) 108} \\ \underline{2 \overline{) 54}} \\ 3 \overline{) 27} \\ \underline{3 \overline{) 9}} \\ 3 \end{array}$$

② $\sqrt{\frac{108x^2y^{-3}}{x^5z^{-5}}}$

when we see odd powers under the square root, we must assume the variables are nonnegative.

when $x \geq 0$, then $|x| = x$, so we don't sweat the absolute values, here.

Scratch: $108 = 2^2 \cdot 3^3$

$$= 2^2 \cdot 3^2 \cdot 3$$

$$x^{2-5} y^{-3} z^5 = x^{-3} y^{-3} z^5$$

$$= \frac{z^5}{x^3 y^3} = \frac{z^4 \cdot z}{x^2 \cdot x \cdot y^2 \cdot y}$$

$$= \sqrt{\frac{2^2 \cdot 3^2 \cdot 3 \cdot z^4 \cdot z}{x^2 \cdot y^2 \cdot x \cdot y}} = \frac{2 \cdot 3 \cdot z^2}{xy} \sqrt{\frac{3z}{xy}}$$

$$= \boxed{\frac{6z^2}{xy} \sqrt{\frac{3z}{xy}}}$$

$$\begin{array}{r} 3 \overline{) 81} \\ \underline{3 \overline{) 27}} \\ 3 \overline{) 9} \\ 3 \end{array}$$

③ $\sqrt{x^2} = |x|$, ④ $\sqrt{(x-5)^2} = |x-5|$

⑤ $(81)^{\frac{1}{4}}$
 $= (3^4)^{\frac{1}{4}}$
 $= 3^{(4 \times \frac{1}{4})} = \boxed{3}$

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(6) $x^2 - 2x - 35 = 0$ in 3 methods

(a) $(x-7)(x+5) = 0 \Rightarrow \boxed{x=7 \text{ OR } x=-5}$

(b) $x^2 - 2x = 35$

$$x^2 - 2x + 1^2 = 35 + 1^2$$

$$(x-1)^2 = 36$$

$$|x-1| = \sqrt{36} = 6$$

$$x-1 = 6 \text{ OR } x-1 = -6$$

$$\boxed{x=7 \text{ OR } x=-5}$$

(c) $a=1, b=-2, c=-35$

$$b^2 - 4ac = (-2)^2 - 4(1)(-35)$$

$$= 4 + 140 = 144$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-(-2) \pm \sqrt{144}}{2(1)}$$

$$= \frac{2 \pm 12}{2} = \frac{2(1 \pm 6)}{2}$$

$$= 1 \pm 6 \rightarrow \boxed{x=7 \text{ OR } x=-5}$$

(7) The discriminant of

$$x^2 - 2x - 35 = 0 \text{ is}$$

$$b^2 - 4ac = (-2)^2 - 4(1)(-35)$$

$$= \boxed{144}$$

$$(a=1, b=-2, c=-35)$$

(8) $x^2 - 5x + 7 = 0$

$$x^2 - 5x = -7$$

$$x^2 - 5x + \left(\frac{5}{2}\right)^2 = -7 + \left(\frac{5}{2}\right)^2$$

$$\left(x - \frac{5}{2}\right)^2 = -\frac{3}{4}$$

$$x - \frac{5}{2} = \pm \sqrt{-\frac{3}{4}} = \pm i \sqrt{\frac{3}{4}} = \pm i \frac{\sqrt{3}}{\sqrt{4}} = \pm \frac{i\sqrt{3}}{2}$$

$$x = \frac{5}{2} \pm \frac{i\sqrt{3}}{2} = \frac{5 \pm i\sqrt{3}}{2} \rightarrow \boxed{x = \frac{5 + i\sqrt{3}}{2} \text{ OR } \frac{5 - i\sqrt{3}}{2}}$$

SCRATCH:

$$-7 + \left(\frac{5}{2}\right)^2 = -7 + \frac{5^2}{2^2}$$

$$= -7 + \frac{25}{4}$$

$$= -\frac{7}{1} \cdot \frac{4}{4} + \frac{25}{4}$$

$$= \frac{-28 + 25}{4} = -\frac{3}{4}$$

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⑧ Done with quadratic formula

$$x^2 - 5x + 7 = 0$$

$$a = 1, b = -5, c = 7$$

$$\begin{aligned} b^2 - 4ac &= (-5)^2 - 4(1)(7) \\ &= 25 - 28 = -3 \end{aligned}$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{5 \pm \sqrt{-3}}{2} = \frac{5 \pm i\sqrt{3}}{2}$$

$$\boxed{x = \frac{5 + i\sqrt{3}}{2} \text{ OR } x = \frac{5 - i\sqrt{3}}{2}}$$

#s 9 - 18 SEE TEST 5

#s 19 - 22 SEE TEST 4

ALL THE REST, just back track thru the other test keys I posted on the website.