

Homework 7 due 4/11 (Next Wednesday)

$$\sqrt{ab} = \sqrt{a}\sqrt{b}$$

when $a \geq 0$ & $b \geq 0$

if not, then you
need to manage
imaginary.

$$\sqrt{-2} \sqrt{-6} =$$

$$(i\sqrt{2})(i\sqrt{6}) =$$

$$i^2 \sqrt{2} \sqrt{6} =$$

$$-1 \sqrt{2} \sqrt{6} =$$

$$-1 \sqrt{2 \cdot 6} =$$

$$-\sqrt{12} =$$

$$-\sqrt{2 \cdot 2 \cdot 3} =$$

$$\boxed{-2\sqrt{3}}$$

$$\begin{array}{r} 2 \overline{)12} \\ 2 \overline{)6} \\ 3 \end{array}$$

$$\sqrt{\text{☺}^2} = |\text{☺}|$$

$$(y-3)^2 = 4$$

$$\sqrt{(y-3)^2} = \sqrt{4}$$

$$|y-3| = \sqrt{4} = 2$$

$$y-3=2 \text{ OR } y-3=-2$$

$$y=5 \text{ OR } y=1$$

I asked for absolute value management, specifically.

is OK
 $(y-3 = \pm 2)$

$$y = 3 \pm 2$$

$$y = 5 \text{ OR } y = 1$$

82

$$\begin{array}{r} 2 \overline{) 72} \\ \underline{2} \\ 2 \\ \underline{2} \\ 3 \\ \underline{3} \\ 3 \\ \underline{3} \\ 0 \end{array}$$

$$(x+5)^2 = 72$$

$$x+5 = \pm \sqrt{72}$$

$$x+5 = \pm 2 \cdot 3\sqrt{2}$$

$$x+5 = \pm 6\sqrt{2}$$

$$x = -5 \pm 6\sqrt{2}$$

shortest legal way.

$$(x+5)^2 = 72$$

$$x+5 = \pm \sqrt{72} = \pm 6\sqrt{2}$$

$$x = -5 \pm 6\sqrt{2}$$

$$\frac{4 - \sqrt{48}}{2} = \frac{4 - 4\sqrt{3}}{2}$$

$$= \frac{\overset{2}{\cancel{4}}(1 - \sqrt{3})}{\underset{1}{\cancel{2}}} = \frac{2(1 - \sqrt{3})}{1}$$

$$= \boxed{2 - 2\sqrt{3}}$$

$$\begin{array}{r} 2 \overline{)48} \\ \underline{2} \\ 2 \\ \underline{2} \\ 0 \\ 2 \overline{)12} \\ \underline{2} \\ 0 \\ 2 \overline{)6} \\ \underline{2} \\ 0 \end{array}$$

$$\sqrt{2 \cdot 2 \cdot 2 \cdot 2 \cdot 3}$$

$$= 2 \cdot 2\sqrt{3}$$

$$= 4\sqrt{3}$$

Shorter

$$\frac{\overset{2}{\cancel{4}} - \overset{2}{\cancel{4}}\sqrt{3}}{\underset{1}{\cancel{2}}} = 2 - 2\sqrt{3}$$

$$2 - 2x = -x \rightarrow \text{No way}$$

we treat 2 & $2\sqrt{3}$ like "unlike terms"

is OK, but beginners tend to forget to cancel with every term in the numerator.

$$\frac{4 - \sqrt{48}}{2} = \frac{4 - 4\sqrt{3}}{2}$$

$$4i\sqrt{3} \quad \text{---}$$

$$= i4\sqrt{3}$$

$$= 4\sqrt{3}i$$

$$\frac{4 - \sqrt{-48}}{2} = \frac{4 - i\sqrt{48}}{2} = \frac{4 - 4i\sqrt{3}}{2}$$

$$= \frac{4(1 - i\sqrt{3})}{2} = \frac{2(1 - i\sqrt{3})}{1} = \boxed{2 - 2i\sqrt{3}}$$

Alternate
(After you
have done
50 of 'em.)

$$= \frac{\overset{2}{4} - \overset{2}{4}i\sqrt{3}}{\overset{2}{2}} = 2 - 2i\sqrt{3}$$

Quadratic Formula

$$ax^2 + bx + c = 0 \implies$$

$$\text{Discriminant} = b^2 - 4ac$$

Compute 1st



Why?

- ① Positive: 2 different real solutions.
- ② Zero: one real solution
(and $ax^2 + bx + c$ is a perfect square trinomial)
- ③ Negative: 2 different non-real solutions
- ④ It cleans up your work handling the $b^2 - 4ac$ separately.

$$3x^2 - 7x - 11 = 0$$

$$a = 3, b = -7, c = -11$$

$$b^2 - 4ac = (-7)^2 - 4(3)(-11)$$

$$= 49 + 132$$

$$= 181$$

$\sqrt{181}$ is simplified

$$\text{So } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(-7) \pm \sqrt{181}}{2(3)} = \frac{7 \pm \sqrt{181}}{6} = x$$

$$x = \frac{-(-7) \pm \sqrt{(-7)^2 - 4(3)(-11)}}{2(3)} = \frac{7 \pm \sqrt{181}}{6}$$

is messier
for most folks,
in practice.

$$\begin{array}{l} 2, 3, 5, 7, 11, 13, 17 \\ 4, 9, 25, 49, 121, 169, 289 \end{array}$$

$$\begin{array}{l} \cancel{2}, \cancel{3}, \cancel{5}, \cancel{7}, \cancel{11}, \cancel{13}, 17 \\ 4, 9, 25, 49, 121, 169, 289 \end{array}$$

Solve it

$$(x-2)(x+3) = 7$$

$$x^2 + 3x - 2x - 6 = 7$$

$$x^2 + x - 6 = 7$$

$$x^2 + x - 13 = 0$$

$$a=1, b=1, c=-13$$

$$b^2 - 4ac = 1^2 - 4(1)(-13)$$

$$= 1 + 52$$

$$= 53 \text{ Doesn't factor.}$$

$\sqrt{53}$ is simplified

Factored left side
is NO HELP, unless
the right side is
zero!

$$x = \frac{-1 \pm \sqrt{53}}{2}$$

$$25x^2 + 30x + 9 = 0$$

$$a=25, b=30, c=9$$

$$b^2 - 4ac = (30)^2 - 4(25)(9)$$

$$= 900 - 900$$

$= 0$ means we have a perfect square trinomial

$$x = \frac{-30 \pm \sqrt{0}}{2(25)} = \frac{-30}{50} = -\frac{3}{5}$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\begin{aligned} & 25x^2 + 30x + 9 \\ \rightarrow & (5x)^2 + 2(5x)(3) + 3^2 = 0 \\ & (5x + 3)^2 = 0 \end{aligned}$$

$$|5x + 3| = \sqrt{0} = 0$$

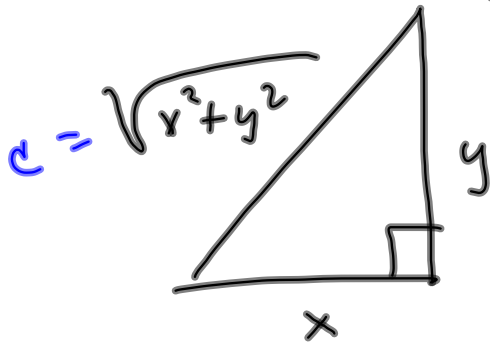
$$|5x + 3| = 0$$

$$5x + 3 = 0 \quad \text{or} \quad \cancel{5x + 3 = -0}$$

$$5x = -3$$

$$x = -\frac{3}{5}$$

Pythagoras Says



$$x^2 + y^2 = c^2$$

$$|c| = \sqrt{x^2 + y^2}$$

$$c = \pm \sqrt{x^2 + y^2} \quad \&$$

we always take
the positive.