

Left over from last time:

④ Completing the square.

$$\left. \begin{aligned} (a-b)^2 &= a^2 - 2ab + b^2 \\ (a+b)^2 &= a^2 + 2ab + b^2 \end{aligned} \right\} \text{The square of} \\ & \text{a binomial}$$

$$\sqrt[4]{81} = \sqrt[4]{3^4} = 3$$

$$\begin{array}{r} 3 \overline{)81} \\ \underline{3} \\ 3 \overline{)27} \\ \underline{3} \\ 3 \overline{)9} \\ \underline{3} \\ 3 \end{array}$$

$$\sqrt[4]{81x^4} = 3|x|$$

$$\sqrt[3]{81x^4} = \sqrt[3]{3^4 x^4} = \sqrt[3]{3^3 3^1 x^3 x^1}$$

$$= 3x \sqrt[3]{3x}$$

No absolute value concerns for odd-indexed roots

$$\sqrt[4]{162x^6} = \sqrt[4]{2 \cdot 3^4 \cdot x^4 x^2} = 3|x| \sqrt[4]{2x^2}$$

$$\begin{array}{r} 2 \overline{)162} \\ \underline{2} \\ 3 \overline{)81} \\ \underline{3} \\ 3 \overline{)27} \\ \underline{3} \\ 3 \overline{)9} \\ \underline{3} \\ 3 \end{array}$$

Now. If you assume $x \geq 0$, then

it's $3x \sqrt[4]{2x^2}$

Since $|x| = x$ when $x \geq 0$

RECALL $|x| = \begin{cases} x & \text{if } x \geq 0 \\ -x & \text{if } x < 0 \end{cases}$

$$\begin{aligned} (x-2)^2 &= x^2 - 2(x)(2) + (-2)^2 \\ (a-b)^2 &= a^2 - 2ab + b^2 \\ (a+b)^2 &= a^2 + 2ab + b^2 \end{aligned} \left. \vphantom{\begin{aligned} (x-2)^2 &= x^2 - 2(x)(2) + (-2)^2 \\ (a-b)^2 &= a^2 - 2ab + b^2 \\ (a+b)^2 &= a^2 + 2ab + b^2 \end{aligned}} \right\} \text{MEMORIZE}$$

$$(x-2)^2 = x^2 - 4x + 4$$

$$\begin{aligned} (x+3)^2 &= x^2 + 2(x)(3) + 3^2 \\ &= x^2 + 6x + 9 \end{aligned}$$

$$(x+7)^2 = x^2 + 14x + 49$$

In §8.1, we want to go from

$$x^2 + 14x + 49$$

to $(x+7)^2$ Binomial Squared

Complete the square:

$$x^2 + 14x + \underline{49}$$



$$\frac{14}{2} = 7 \rightsquigarrow 7^2 = 49$$

$$x^2 + \underline{8x} + \underline{16} \quad \text{Now factors into } (x+4)^2$$

\downarrow
 $\frac{8}{2} = 4 \rightsquigarrow 4^2 = 16$

$$x^2 - \underline{3x} + \underline{\left(\frac{3}{2}\right)^2} = \left(x - \frac{3}{2}\right)^2$$

\downarrow
 $\frac{3}{2} \rightarrow \left(\frac{3}{2}\right)^2 = \frac{3^2}{2^2} = \frac{9}{4}$

check

$$\left(x - \frac{3}{2}\right)^2 = x^2 - \underline{2(x)\left(\frac{3}{2}\right)} + \underline{\left(\frac{3}{2}\right)^2} = x^2 - 3x + \frac{9}{4}$$

$$(a-b)^2 = a^2 - 2ab + b^2$$

$$\left. \begin{aligned} (x+2)^2 &= 11 \\ \sqrt{(x+2)^2} &= \sqrt{11} \\ |x+2| &= \sqrt{11} \\ x+2 &= \pm\sqrt{11} \end{aligned} \right\} \text{Today is about getting to this point}$$

$$x = -2 \pm \sqrt{11}$$

Solve, by completing the square.

$$x^2 + 4x - 7 = 0$$

$$\begin{aligned} x^2 + 4x &= 7 \\ \sqrt{\quad} & \\ \frac{4}{2} = 2 &\rightarrow 2^2 = 4 \end{aligned}$$

$$x^2 + 4x + 4 = 7 + 4$$

$$(x+2)^2 = 11$$

$$x+2 = \pm\sqrt{11}$$

$$x = -2 \pm \sqrt{11}$$

WE ONLY KNOW HOW TO COMPLETE THE SQUARE WHEN THE COEFFICIENT OF x^2 IS "1"

short version for the rest

We did these last two steps in about 5 steps, but once you're practiced it's just 2 steps to the finish.

Solve $x^2 - 6x - 7 = 0$ by completing
the square. (Factors: $(x-7)(x+1)$)

$$x^2 - 6x + 3^2 = 7 + 9$$

\downarrow
 $\frac{6}{2} = 3 \rightsquigarrow 3^2 = 9$

$$(x-3)^2 = 16$$

$$x-3 = \pm \sqrt{16} = \pm 4$$

$$x = 3 \pm 4 \begin{cases} \rightarrow 3+4 = 7 = x \\ \rightarrow 3-4 = -1 = x \end{cases}$$

Ex. 1 #535-42 are good for this skill

Solve by completing the square

① Get $x^2 + bx$ by itself on Left

② $\frac{b}{2} \rightarrow \left(\frac{b}{2}\right)^2$ Add to both sides

③ write $\left(x + \frac{b}{2}\right)^2 = K$

Solve by square root property.

$$x^2 + 6x - 4 = 0$$

① $x^2 + 6x = 4$

② $x^2 + 6x + 3^2 = 4 + 9$

$(x+3)^2 = 13$

③ $x+3 = \pm\sqrt{13}$
 $x = -3 \pm\sqrt{13}$