



Today C7,8 Worksheet Posted.
Problems for practice
listed in Friday's Lecture.

I'm asking for a minimal cross-section.
If you can't work a problem on the worksheet,
work a bunch that are like it. Look for
examples in the book. Just getting the
worksheet right doesn't mean you can work
them without help on a test. You need
to know the difference between under-
standing and **not** understanding.

Today & Tomorrow

$$\textcircled{1} \sqrt{x^2} = |x|$$

your book lets you FORGET this with instructions like "Assume all variables represent positive numbers."

When this is the case,

$$\sqrt{x^2} = |x| = x$$

$$3 \overline{)39} \\ \underline{13}$$

$$\textcircled{2} \sqrt{-1} = i, \quad i^2 = -1$$

$$\sqrt{-39} = i\sqrt{39}$$

$\textcircled{3}$ Solving Quadratics by square root property.

$\textcircled{4}$ Completing the square.

$$\begin{aligned}\sqrt{-16} &= i\sqrt{16} \\ &= i\sqrt{2 \cdot 2 \cdot 2 \cdot 2} \\ &= i \cdot 2 \cdot 2 \sqrt{1 \cdot 1} \\ &= i \cdot 4 = 4i\end{aligned}$$

$$\begin{array}{r} 2 \overline{)16} \\ 2 \overline{)8} \\ 2 \overline{)4} \\ 2 \end{array}$$

FACT: If $a \geq 0, b \geq 0$, then $\sqrt{a}\sqrt{b} = \sqrt{ab}$

$$\begin{array}{r} 2 \overline{)12} \\ 2 \overline{)6} \\ 3 \end{array}$$

$$\sqrt{6}\sqrt{2} = \sqrt{12} = \sqrt{2 \cdot 2 \cdot 3} = 2\sqrt{3}$$

$$\sqrt{-6}\sqrt{-2} = i\sqrt{6}i\sqrt{2} = \underline{i^2\sqrt{6}\sqrt{2}}$$

$$= i^2\sqrt{12} = i^2 \cdot 2\sqrt{3}$$

$$= 2i^2\sqrt{3}$$

$$= -2\sqrt{3}$$

why not just $\sqrt{-6}\sqrt{-2} = \sqrt{(-6)(-2)} = \sqrt{12} = 2\sqrt{3}$

↳ -6 & -2 are NOT ≥ 0 .

Rule says $a \geq 0, b \geq 0$ make

$$\sqrt{a}\sqrt{b} = \sqrt{ab}$$

Product of
the radicals

Radical
of
the product.

$$x^2 - 57 = 0$$

No "x" term in the middle

$$x^2 = 57$$

$$\sqrt{x^2} = \sqrt{57}$$

$$|x| = \sqrt{57}$$

$$x = \sqrt{57} \text{ or } x = -\sqrt{57}$$

$$x = \pm\sqrt{57}$$

Show these steps
on your 1st 20
tries.

$$(2x-7)^2 - 15 = 0$$

$$(\text{something})^2 - \text{constant} = 0$$

$$(2x-7)^2 = 15$$

$$\sqrt{(2x-7)^2} = \sqrt{15}$$

$$|2x-7| = \sqrt{15}$$

$$2x-7 = \sqrt{15} \text{ or } 2x-7 = -\sqrt{15}$$

$$2x = 7 + \sqrt{15} \text{ or } 2x = 7 - \sqrt{15}$$

$$x = \frac{7 + \sqrt{15}}{2} \text{ or } x = \frac{7 - \sqrt{15}}{2}$$

After 20:

$$(2x-7)^2 = 15$$

$$2x-7 = \pm\sqrt{15}$$

$$2x = 7 \pm \sqrt{15}$$

$$x = \frac{7 \pm \sqrt{15}}{2}$$

$$(2x-7)^2 + 15 = 0$$

$$(2x-7)^2 = -15$$

$$\sqrt{(2x-7)^2} = \sqrt{-15}$$

$$|2x-7| = i\sqrt{15}$$

$$2x-7 = i\sqrt{15} \quad \text{OR} \quad 2x-7 = -i\sqrt{15}$$

$$2x = 7 + i\sqrt{15} \quad \text{OR} \quad 2x = 7 - i\sqrt{15}$$

$$x = \frac{7 + i\sqrt{15}}{2} \quad \text{OR} \quad x = \frac{7 - i\sqrt{15}}{2}$$

Simplify

$$\frac{6 + \sqrt{54}}{3} =$$

 $\sqrt{x^2}$

$$\begin{array}{r} 2 \overline{)54} \\ 3 \overline{)27} \\ 3 \overline{)9} \\ 3 \end{array}$$

~~$2, 3, 5, 7, 11, 13, 17$~~

$$\frac{3\sqrt{6}}{3} = \sqrt{6}$$

$$\sqrt{54} = \sqrt{2 \cdot \underline{3 \cdot 3} \cdot 3}$$

$$= 3\sqrt{6}$$

$$\frac{6 + 3\sqrt{6}}{3} = \frac{\cancel{3}(2 + \sqrt{6})}{\cancel{3}}$$

$$= 2 + \sqrt{6}$$

Coming Soon

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$(x+b)^2 = x^2 + 2bx + b^2$$