

Two numbers, A & B . And all I know is that $AB = 0$.

Any possibilities?

$$A = 2, B = 0 \Rightarrow AB = 2 \cdot 0 = 0$$

$$A = 32\pi, B = 0 \Rightarrow 32\pi \cdot 0 = 0$$

$$\approx 32 \cdot 3.14$$

Basically, anything for one and

$$A = 2, B = \frac{1}{2} \quad AB = 1 \neq 0$$

Principle of zero products:

$$AB = 0 \Rightarrow$$

$$A = 0 \quad \text{OR} \quad B = 0$$

This is WHY we factor.

$$x^2 - 9 = 0$$

$$x^2 - 3^2 = 0$$

$$(x-3)(x+3) = 0$$

$$\underbrace{\quad} \cdot \underbrace{\quad} = 0 \Rightarrow$$

$$A = 0 \quad \text{OR} \quad B = 0$$

$$x - 3 = 0 \quad \text{OR} \quad x + 3 = 0$$

$$\boxed{x = 3 \quad \text{OR} \quad x = -3}$$

Factoring turns a HARD quadratic equation into

a pair of EASY linear equations.

Quadratic Equation

2nd-degree polynomial equation

Has an x^2 in it

Two Linear equations

Has x^1 as highest power!

Down the road, we'll only factor things we're good at factoring (the easy ones) and we'll clobber 'em with the quadratic formula when we're NOT good at factoring.

we won't waste much time on factoring the toughies, like yesterday's example.

This was hard.

$$10x^2 - 9x - 91 = [2x-7][5x+13] \text{ is now factored!}$$

$$-9x = \underline{-10x + 1x} \quad (10)(1) = -10 \neq -910 =$$

$$-9x = \underline{-35x + 26x} \quad (-35)(26) = -910! \text{ magic number!}$$

$$\begin{array}{l} \downarrow \\ 10x^2 - 9x - 91 \\ = 10x^2 - 35x + 26x - 91 \quad \& \text{ factor by grouping.} \\ = 5x[2x-7] + 13[2x-7] \\ = [2x-7][5x+13] \end{array}$$

If you KNOW

$10x^2 - 9x - 91 = [2x-7][5x+13]$, then you

can solve $10x^2 - 9x - 91 = 0$

$$(2x-7)(5x+13) = 0$$

$$2x-7=0 \quad \text{OR} \quad 5x+13=0$$

$$\frac{+7}{+7} = \frac{+7}{+7}$$

$$2x = 7$$

$$5x = -13$$

$$\frac{2x}{2} = \frac{7}{2}$$

$$x = \frac{7}{2} \quad \text{OR} \quad x = -\frac{13}{5}$$

Check: $10x^2 - 9x - 91 = 0$

$$10\left(\frac{7}{2}\right)^2 - 9\left(\frac{7}{2}\right) - 91 = 0 ?$$

$$10\left(\frac{7^2}{2^2}\right) - \left(\frac{9}{1}\right)\left(\frac{7}{2}\right) - 91 = 0 ?$$

$$\left(\frac{10}{1}\right)\left(\frac{49}{4}\right) - \frac{63}{2} - 91 = 0 ?$$

$$\frac{490}{4} - \frac{63}{2} - 91 = 0 ?$$

$$\frac{245}{2} - \frac{63}{2} - 91 = 0 ?$$

$$\frac{182}{2} - 91 = 0 ?$$

$$91 - 91 = 0 ! \quad \text{Sweet!}$$

So what sorts of factoring do I want?

$$S'5.7 \left\{ \begin{array}{l} a^2 - b^2 \\ a^2 - 2ab + b^2 \\ a^2 + 2ab + b^2 \end{array} \right.$$

$$\left. \begin{array}{l} a^3 - b^3 \\ a^3 + b^3 \end{array} \right\} \text{ Bonus.}$$

S'5.6 "Easy ones" #5 1-8, 35-42

$$|x^2 + 9x + 20 = 0$$

$$x^2 + 5x + 4x + 20 = 0$$

$$x(x+5) + 4(x+5) = 0$$

$$(x+5)(x+4) = 0$$

$$\rightarrow x = -5 \text{ OR } x = -4$$

#5 1-8 S'5.6 are like this.

u-substitution
 $x^2 + bx + c = 0$

Magic #: 20

Sum is 9, product is 20

<u>8+1</u>	8
<u>7+2</u>	14
<u>6+3</u>	18
5+4	<u>20 Sweet!</u>

Another method.

$$x^2 + 9x + 20 = 0$$

$$(x+1)(x+20) = x^2 + 21x + 20 \text{ No}$$

$$(x+2)(x+10) = x^2 + 12x + 20 \text{ No}$$

$$(x+4)(x+5) = x^2 + 9x + 20 \text{ Sweet!}$$

#5 35-42 are u-substitution problems.

Recognizing when an equation is
"quadratic in form"

$$\textcircled{36} \quad x^4 - x^2 - 20$$

$$\text{Let } u = x^2$$

$$x^4 = x^{2 \cdot 2} = (x^2)^2$$

$$x^4 - x^2 - 20$$

$$= (x^2)^2 - x^2 - 20$$

$$= u^2 - u - 20$$

$$= u^2 - 5u + 4u - 20$$

$$= u(u-5) + 4(u-5)$$

$$= (u-5)(u+4)$$

Twisted! $= (x^2-5)(x^2+4)$ is Done, for now.

$$= (x^2 - (\sqrt{5})^2)(x^2+4)$$

$$= (x+\sqrt{5})(x-\sqrt{5})(x^2+4)$$

Goal down the road
is solving
 $x^4 - x^2 - 20 = 0$

Magic:	-20	product
sum		
-2 + 1		-2
-3 + 2		-6
-4 + 3		-12
-5 + 4		-20!
		Sweet!

$$(\sqrt{5})^2 = (\sqrt{5})(\sqrt{5})$$

$$= 5$$

$$a^2 - b^2 =$$

$$(a+b)(a-b)$$

$$\textcircled{38} \quad (3x-1)^2 + 5(3x-1) + 6 = 0$$

Let $u = 3x-1$. Then

$u^2 + 5u + 6$ is what we have.

$$= u^2 + 2u + 3u + 6 = 0$$

$$= u(u+2) + 3(u+2) = 0$$

$$= (u+2)(u+3) = 0 \quad u \text{ has served its purpose.}$$

$$= ((3x-1)+2)((3x-1)+3) = 0$$

$$= (3x-1+2)(3x-1+3) = 0$$

$$= (3x+1)(3x+2) = 0$$

Test
Wednesday

$$x = -\frac{1}{3}, -\frac{2}{3}$$

So, #s 1-8, 35-42 in § 5.6 is
the extent of § 5.6

Skip 5.7, 5.8

#s 1-8: Treat like EQUATIONS
and SOLVE those equations.
Put an "= 0" after every one.

#s 37, 38 treat like equations, also.