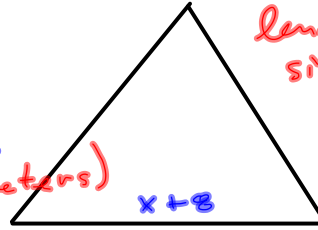


Two gardens are being fenced in. Both gardens will require the same amount of fencing (both gardens have the same perimeter in meters). One garden is in the shape of a square and the other is in the shape of an equilateral triangle. Each side of the triangle is 8 meters longer than each side of the square. Find the dimensions of the garden.



Let  $x$  = length of a side of the square. (in meters)



Find the length of the sides of each.

$$\begin{aligned}
 &\text{Perimeter} = \text{Perimeter} \\
 &4 \cdot \text{side length} = 3 \cdot \text{side length} \\
 &4x = 3(x+8) \quad \text{Distribute!} \\
 &4x = 3x + 24 \\
 &\underline{-3x = -3x} \\
 &x = 24
 \end{aligned}$$

Check it:

$$\begin{aligned}
 &4(24) = 3(24+8) = 3(32) \\
 &96 = 96 \quad \text{Nice.}
 \end{aligned}$$

Back-Track to §2.1 #47 (like #48)  
Pathologies

$$5(x-2) + 2x = 7(x+4) - 38$$

$$5x - 10 + 2x = 7x + 28 - 38$$

$$7x - 10 = 7x - 10 \text{ warning!}$$

$$\begin{array}{r} +10 \qquad +10 \\ \hline \end{array}$$

$$7x = 7x$$

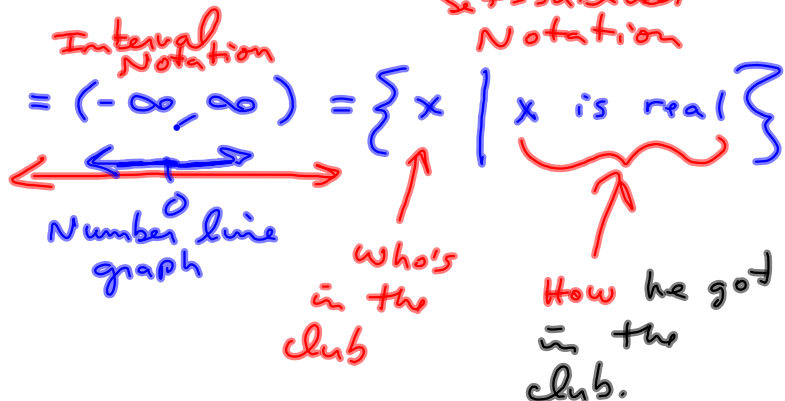
$$-7x = -7x$$

$$\underline{0 = 0}$$

statement is true, regardless of the value of  $x$ .

Solution Set:

All real numbers =  $(-\infty, \infty)$



$$5(x-2) + 2x = 7(x+4) - 37$$

$$5x - 10 + 2x = 7x + 28 - 37$$

$$7x - 10 = 7x - 9 \quad \text{Warning!}$$

$$\begin{array}{r} 7x - 10 = 7x - 9 \\ \hline +10 \qquad +10 \end{array}$$

$$7x = 7x + 1$$

$$\begin{array}{r} 7x = 7x + 1 \\ \hline -7x \qquad -7x \end{array}$$

$$0 = 1 \quad !?$$

No way

Absurd!

Premise is false

No Solution

RAA -  
Reductio ad  
Absurdum.  
Reduce to Absurdity

To solve any equation,  
all our reasoning is based  
on this assumption:

Revise: THERE IS A SOLUTION

When you reason from a  
faulty premise, you arrive  
at an absurdity.

$$\text{Sol'n Set} = \{ \} = \emptyset$$

The sum of the first and third of three consecutive even integers is 140. Find the three even integers.

Let  $n$  be an integer.

Find me an even integer in terms of  $n$ .

$$2n$$

$$\text{ODD Integer: } 2n+1$$

$$2n-1$$

3 consecutive even integers

$$2, 4, 6$$

$$8, 10, 12$$

Let  $x$  = the first (smallest) integer.

$$x, x+2, x+4$$

The sum of the 1<sup>st</sup> & 3<sup>rd</sup> is 140.

$$x + x + 4 = 140$$

$$2x + 4 = 140$$

$$-4 = -4$$

$$2x = 136$$

$$\frac{2x}{2} = \frac{136}{2}$$

$$x = 68$$

$$\frac{\quad}{2} \quad \frac{\quad}{2}$$

*Maybe come back.*

The following graph is called a circle graph or a pie chart. The circle represents a whole, or in this case, 100%. This particular graph shows the number of minutes per day that people use e-mail at work. Use this graph to answer what percent of e-mail users at work spend less than 15 minutes on e-mail per day?



## § 2.3 Formulas : 5 steps

STEP 1 : Clean Fractions

I prefer writing everything over one denominator  
THEN decide if you can throw the denominator  
 away (usually, we can).

STEP 2 : Get rid of parens.

STEP 3 : Combine like terms.

STEP 4 : Get "the" variable on one side

STEP 5 : Isolate the variable.

§ 2.3 #s 1, 4, 7, ..., 40

Solve  $L = a + (n-1)d$  for  $d$

$$\left. \begin{array}{l} L = a + nd - 1d \\ L = a + (n-1)d \end{array} \right\} \text{skip!}$$

$$a + (n-1)d = L$$

$$\begin{array}{r} -a \\ \hline \end{array} \quad \begin{array}{r} \\ \\ \\ \end{array} = -a$$

$$(n-1)d = L - a \quad \text{Need}$$

$$\frac{(n-1)d}{n-1} = \frac{L-a}{n-1}$$

$$\boxed{d = \frac{L-a}{n-1}} \quad \text{Need}$$

$$\frac{TI \ 30 \ \Pi}{x \ 5}$$

$$A = P \left(1 + \frac{r}{n}\right)^{nt}$$

$P =$  Principal

$r =$  Interest rate

$t =$  # of years

$n =$  # of compoundings per year.

~~principle~~

8% compounded annually:  $n = 1$

$$= 100 + (100)(.08)$$

$$= 100(1 + .08)$$

$$100 + 100(.08) + (100 + 100(.08))(.08)$$

$$= 100(1 + .08) + (100(1 + .08))(.08)$$

$$= 100(1 + .08) [1 + .08] = 100(1.08)^2$$

$$3 \quad 100(1.08)^3$$

⋮

(2006, 31.6)

$$31.6 \text{ mill} = x + 5.4\% \text{ of } x \text{ since 2001}$$

Let  $x = \text{pop. in 2001}$  (in millions of people)

$$31.6 = x + .054x = 1.054x \rightarrow$$

$$\frac{31.6}{1.054} = x \approx$$

Pop in 2006 is Pop in 2001 + New People

$$31.6 = x + .054x$$

Price + Tax is Price plus tax

$$\frac{\textcircled{?}}{31.60} = \frac{\$3 + (.08)(\$3)}{x + .08x}$$