

Solve in 3 ways

- ① Factoring
  - ② Completing the Square
  - ③ Quadratic Formula
- $$x^2 - 6x + 8 = 0$$

Use synthetic division to find  $P(3)$  if  $P(x) = x^2 + 6x - 8$   
 $(a-b)^2 = a^2 - 2ab + b^2$

① Factors +8 whose sum is -6

$$x^2 - 4x - 2x + 8 =$$

$$x(x-4) - 2(x-4) =$$

$$(x-4)(x-2) = 0$$

$$x \in \{2, 4\}$$

②  $x^2 - 6x = -8$

$$\frac{-6}{2} = -3 \rightarrow (-3)^2 = +9$$

$$x^2 - 6x + 3^2 = -8 + 9$$

$$(x-3)^2 = 1$$

$$x-3 = \pm\sqrt{1} = \pm 1$$

$$x = 3 \pm 1$$

$$3+1=4 \qquad 3-1=2$$

$$x \in \{2, 4\}$$

$$(x-3)^2 = x^2 - 6x + 9$$

$$(x+5)^2 = x^2 + 10x + 25$$

$$(x-7)^2 = x^2 - 14x + 49$$

$\downarrow$   
 $2 \cdot 7 \cdot x$

$$x^2 - 6x + 8 = 0$$

$$a = 1, b = -6, c = 8$$

$$b^2 - 4ac = (-6)^2 - 4(1)(8)$$

$$= 36 - 32 = 4$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\frac{-(-6) \pm \sqrt{4}}{2(1)}$$

$$= \frac{6 \pm 2}{2}$$

$$\frac{6+2}{2} = \frac{8}{2} = 4$$

$$\frac{6-2}{2} = \frac{4}{2} = 2$$

$$x \in \{2, 4\}$$

Test 1

$$|3x-7| = -5$$

Never

$$|3x-7| = +5$$

$$3x-7 = 5 \quad \text{OR} \quad 3x-7 = -5$$

:

$$|3x-7| < 5$$

$$3x-7 < 5 \quad \text{AND} \quad 3x-7 > -5$$

$-5 < 3x-7 < 5$  is permitted

$$|3x-7| > 5$$

$$3x-7 > 5 \quad \text{OR} \quad 3x-7 < -5$$

$-5 > 3x-7 > 5$  will get you shot.

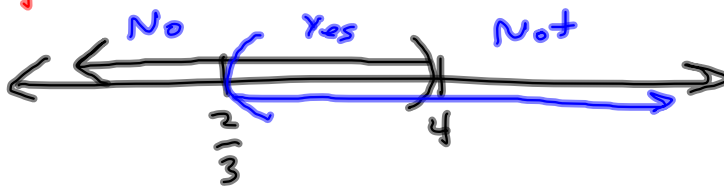
$$|3x-7| < 5$$

$$3x-7 < 5 \quad \text{AND} \quad 3x-7 > -5$$

$$3x < 12$$

$$3x > 2$$

$$\left\{ x \mid x < 4 \quad \text{AND} \quad x > \frac{2}{3} \right\} \text{ set-builder}$$



$$\left\{ x \mid x < 4 \text{ and } x > \frac{2}{3} \right\}$$

$$= \left( \frac{2}{3}, 4 \right) \text{ Interval answer.}$$

$$|3x-7| > 5$$

$$3x-7 > 5 \quad \text{OR} \quad 3x-7 < -5$$

$$3x > 12$$

$$x > 4$$

$$3x-7 < -5$$

$$3x-7 > -5$$

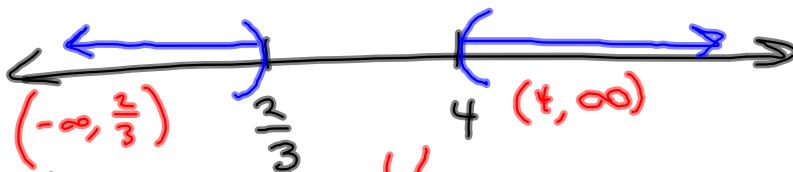
$$3x-7 < -5$$

$$3x < 2$$

$$x < \frac{2}{3}$$

$$\left\{ x \mid x > 4 \quad \text{OR} \quad x < \frac{2}{3} \right\}$$

Most common screwup.  
Gahbridge  
 $\left(\frac{2}{3}, -\infty\right)$



Strict inequality.  $\left(-\infty, \frac{2}{3}\right) \cup (4, \infty)$

$$|5x-7| \geq 5 \Rightarrow x \in \left(-\infty, \frac{2}{3}\right] \cup [4, \infty)$$

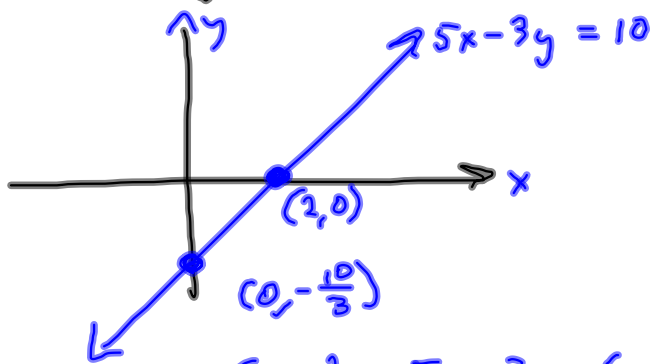
$5x - 3y = 10$  Graph

x	y
0	$-\frac{10}{3}$
2	0

$5(0) - 3y = 10 \Rightarrow y = -\frac{10}{3}$

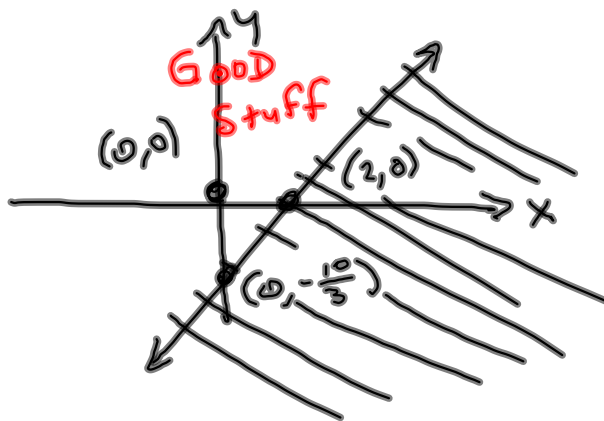
$5x - 3(0) = 10 \Rightarrow x = \frac{10}{5} = 2$

$(0, -\frac{10}{3})$  y-int ( $x=0$ )  
 $(2, 0)$  x-int ( $y=0$ )



$\{ \frac{2}{3}, 4 \}$

Graph  $5x - 3y \leq 10$



Test  $(0,0)$ :  
 $5(0) - 3(0) \leq 10$ ?  
 $0 \leq 10$ ?  
 Yes.  $(0,0)$  good  
 Scratch out bad stuff