

S8.2

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

See pp 489-90

Assume $a > 0$

$$ax^2 + bx + c = 0$$

$$x^2 + \frac{b}{a}x + \frac{c}{a} = 0$$

$$x^2 + \frac{b}{a}x + \left(\frac{b}{2a}\right)^2 = -\frac{c}{a} + \frac{b^2}{4a^2}$$

$$\frac{\frac{b}{a}}{2} = \frac{b}{a} \cdot \frac{1}{2} = \frac{b}{2a} \rightarrow \left(\frac{b}{2a}\right)^2 = \frac{b^2}{(2a)^2} = \frac{b^2}{2^2 a^2} = \frac{b^2}{4a^2}$$

$$\left(x + \frac{b}{2a}\right)^2 = \frac{b^2 - 4ac}{4a^2}$$

LCD = $2 \cdot 2 \cdot a^2$

$$-\frac{c}{a} + \frac{b^2}{4a^2} =$$

$$-\frac{c}{a} \cdot \frac{4a}{4a} + \frac{b^2}{4a^2} = \frac{-4ac}{4a^2} + \frac{b^2}{4a^2} = \frac{b^2 - 4ac}{4a^2}$$

$$\left(x + \frac{b}{2a}\right)^2 = \frac{b^2 - 4ac}{4a^2}$$

$$x + \frac{b}{2a} = \pm \sqrt{\frac{b^2 - 4ac}{4a^2}}$$

$$x = -\frac{b}{2a} \pm \frac{\sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\sqrt{4a^2} =$$

$$\sqrt{4} \sqrt{a^2} =$$

$$2a$$

$$\frac{\sqrt{b^2 - 4ac}}{\sqrt{4a^2}} = \frac{\sqrt{b^2 - 4ac}}{2a}$$

Assume $a > 0$.

$$2x^2 + 9x + 10 = 0$$

$$a = 2, b = 9, c = 10$$

$$b^2 - 4ac = 9^2 - 4(2)(10)$$

$$= 81 - 80 = 1$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-9 \pm \sqrt{1}}{2(2)} = \frac{-9 \pm 1}{4}$$

$$2x^2 + 5x + 4x + 10 = 0$$

$$x(2x+5) + 2(2x+5) = 0$$

$$(2x+5)(x+2) = 0$$

$$x \in \left\{ -\frac{5}{2}, -2 \right\}$$

$$\frac{-9+1}{4} = \frac{-8}{4} = -2$$

$$\frac{-9-1}{4} = \frac{-10}{4} = -\frac{5}{2}$$

$$2x^2 + 7x + 5 = 0$$

Factoring:

$$2x^2 + 5x + 2x + 5 = 0$$

$$x(2x+5) + 1(2x+5) = 0$$

$$(2x+5)(x+1) = 0$$

$$\left\{ -\frac{5}{2}, -1 \right\}$$

Completing Square:

$$x^2 + \frac{7}{2}x + \frac{5}{2} = 0$$

$$x^2 + \frac{7}{2}x + \left(\frac{7}{4}\right)^2 = -\frac{5}{2} + \frac{49}{16}$$

$$\frac{7}{2} \cdot \frac{1}{2} = \frac{7}{4} \rightarrow \left(\frac{7}{4}\right)^2 = \frac{49}{16}$$

$$-\frac{5}{2} \cdot \frac{8}{8} + \frac{49}{16} = \frac{-40 + 49}{16} = \frac{9}{16}$$

$$\left(x + \frac{7}{4}\right)^2 = \frac{9}{16}$$

$$x + \frac{7}{4} = \pm \sqrt{\frac{9}{16}} = \pm \frac{3}{4}$$

$$x = -\frac{7}{4} \pm \frac{3}{4}$$

$$= \frac{-7 \pm 3}{4}$$

$$\frac{-7+3}{4} = -1$$

$$\frac{-7-3}{4} = -\frac{10}{4}$$

Ladsey

$$2x^2 + 7x + 5 = 0$$

$$a = 2, b = 7, c = 5$$

$$b^2 - 4ac = 7^2 - 4(2)(5)$$

$$= 49 - 40$$

$$= 9$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-7 \pm \sqrt{9}}{2(2)} = \frac{-7 \pm 3}{4}$$

$$x \in \left\{ -\frac{5}{2}, -1 \right\}, \text{ as before.} \quad \text{every.}$$

$$\begin{aligned} (x - (-\frac{5}{2}))(x - (-1)) &= (x + \frac{5}{2})(x + 1) \\ &= x^2 + x + \frac{5}{2}x + \frac{5}{2} \\ &= x^2 + \frac{7}{2}x + \frac{5}{2} \end{aligned}$$

Missing the factor of 2

$$2(x + \frac{5}{2})(x + 1) = (2x + 5)(x + 1)$$

Using the quadratic formula to factor.
 $x^2 + 5x + 6 = 0$ A little work tells you
 $x = -2$ & $x = -3$. This means

$$(x+2)(x+3)$$

$$(x - (-2))(x - (-3))$$

From Factor
Theorem, Chapters
5 & 6.

$$x^2 - x - 6 = 0$$

$$a = 1, b = -1, c = -6$$

$$b^2 - 4ac = (-1)^2 - 4(1)(-6)$$

$$= 1 + 24$$

$$= 25$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(-1) \pm \sqrt{25}}{2(1)} = \frac{1 \pm 5}{2}$$

Factors into:

$$(x-3)(x - (-2))$$

$$= (x-3)(x+2)$$

$$\frac{1+5}{2} = 3$$

$$\frac{1-5}{2} = \frac{-4}{2} = -2$$

FACTOR :

$$40x^2 - 34x - 63$$

$$a = 40, b = -34, c = -63$$

$$b^2 - 4ac = (-34)^2 - 4(40)(-63)$$

$$= 11236$$

$$\sqrt{11236} = 106$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(-34) \pm 106}{2(40)} = \frac{34 \pm 106}{80}$$

$$\frac{34 + 106}{80} = \frac{140}{80} = \frac{14}{8} = \frac{7}{4}$$

$$\frac{34 - 106}{80} = -\frac{72}{80} = -\frac{9}{10}$$

$$40 \left(x - \frac{7}{4} \right) \left(x + \frac{9}{10} \right) =$$

$$4 \cdot 10 \left(x - \frac{7}{4} \right) \left(x + \frac{9}{10} \right) =$$

$$4 \left(x - \frac{7}{4} \right) 10 \left(x + \frac{9}{10} \right) =$$

$$(4x - 7)(10x + 9)$$

Trick
Steve

$$\frac{-2 \pm \sqrt{-7}}{5}$$

2 nonreal solutions
 $b^2 - 4ac < 0$

$$\frac{-2 \pm \sqrt{7}}{5}$$

2 real solutions
 $b^2 - 4ac > 0$

$$\frac{-2 \pm \sqrt{0}}{5}$$

1 real
 $b^2 - 4ac = 0$

Discriminant = $b^2 - 4ac$

Find an equation with solutions

$$\frac{-5 \pm \sqrt{37}}{2}$$

$$\left(x - \left(\frac{-5 + \sqrt{37}}{2}\right)\right) \left(x - \left(\frac{-5 - \sqrt{37}}{2}\right)\right) = 0$$

$$x^2 - \left(\frac{-5 - \sqrt{37}}{2}\right)x - \left(\frac{-5 + \sqrt{37}}{2}\right)x + \left(\frac{-5 + \sqrt{37}}{2}\right)\left(\frac{-5 - \sqrt{37}}{2}\right)$$

$$= x^2 - \left(-\frac{5}{2}x\right) - \left(-\frac{5}{2}\right)x + \frac{(5^2) - 37}{4}$$

$$= x^2 + \frac{5}{2}x + \frac{5}{2}x + \frac{25 - 37}{4}$$

$$= x^2 + 5x - \frac{12}{4}$$

$$= x^2 + 5x - 3$$

$\int_{8,2}^{5} \begin{matrix} 4^{\text{th}} \\ 1-21 \end{matrix} 23,$
 25, 27, 29, 33, 35, 51

Tuesday

$$x^2 + 5x - 3 = 0$$