

7.4

Evaluate $2x + 3x$ when $x = \sqrt{7}$

$$2\sqrt{7} + 3\sqrt{7} = 5\sqrt{7}$$

$$2x + 3x = 5x$$

$$x = \sqrt{7} \Rightarrow$$

$$5\sqrt{7}$$

$$5\sqrt{15} + 2\sqrt{15} = 7\sqrt{15}$$

$$6\sqrt{10} - 3\sqrt[3]{10} = 6\sqrt{10} - 3\sqrt[3]{10}$$

Need same index, same radicand.
Apples & Oranges.

$$\begin{aligned} & \sqrt{50} + \sqrt{18} \\ &= \sqrt{25 \cdot 2} + \sqrt{9 \cdot 2} \\ &= \sqrt{25} \sqrt{2} + \sqrt{9} \sqrt{2} \\ &= 5\sqrt{2} + 3\sqrt{2} = 8\sqrt{2} \end{aligned}$$

$$\begin{array}{r} 2 \overline{)50} \\ \underline{5 \overline{)25}} \\ 5 \end{array} \qquad \begin{array}{r} 2 \overline{)18} \\ \underline{3 \overline{)9}} \\ 3 \end{array}$$

$$\begin{aligned} & \sqrt{5^2 \cdot 2} + \sqrt{3^2 \cdot 2} \\ &= 5\sqrt{2} + 3\sqrt{2} \end{aligned}$$

$$\sqrt{27} = \sqrt[2]{3^3} = \sqrt{3^{2+1}} = \sqrt{3^2 \cdot 3^1}$$

when powers aren't perfect.

$$= \sqrt{3^2} \sqrt{3} = 3\sqrt{3}$$

$$\begin{aligned} & \sqrt[3]{24} - 4\sqrt[3]{192} \\ & \sqrt[3]{8 \cdot 3} - 4\sqrt[3]{2^6 \cdot 3} \\ & \sqrt[3]{8} \sqrt[3]{3} - 4 \cdot 2^2 \sqrt[3]{3} \\ & 2\sqrt[3]{3} - 16\sqrt[3]{3} = -14\sqrt[3]{3} \end{aligned}$$

$2^3 \sqrt[3]{3}$ NOT

$$\begin{array}{r} 2 \overline{)192} \\ \underline{2 \overline{)96}} \\ 2 \overline{)48} \\ \underline{2 \overline{)24}} \\ 2 \overline{)12} \\ \underline{2 \overline{)6}} \\ 3 \\ 2^6 \cdot 3 \end{array}$$

$$\begin{aligned} & \sqrt[3]{2^6} = \\ & (2^6)^{\frac{1}{3}} = 2^{\frac{6}{3}} \\ & = 2^2 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{20x} - 6\sqrt{16x} + \sqrt{45x} \\
 = & \sqrt{4 \cdot 5x} - 6 \cdot 4\sqrt{x} + \sqrt{9 \cdot 5x} \\
 = & \sqrt{4}\sqrt{5x} - 24\sqrt{x} + \sqrt{9}\sqrt{5x} \\
 = & 2\sqrt{5x} - 24\sqrt{x} + 3\sqrt{5x} \\
 = & 5\sqrt{5x} - 24\sqrt{x}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt[3]{8y^5} + \sqrt[3]{27y^5} \\
 & 2\sqrt[3]{y^5} + 3\sqrt[3]{y^5} \\
 = & 2y\sqrt[3]{y^2} + 3y\sqrt[3]{y^2} \\
 = & 5y\sqrt[3]{y^2}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt[3]{\frac{512}{y}} \\
 = & \sqrt[3]{\frac{510+2}{y}} \\
 = & \sqrt[3]{\frac{510}{y}} \sqrt[3]{\frac{2}{y}} \\
 & y^{170} \sqrt[3]{y^2}
 \end{aligned}$$

$$\begin{aligned}
 \frac{5}{3} &= 1 + \frac{2}{3} \\
 y^5 &= y^{3+2} = y^3 y^2 \\
 \sqrt[3]{y^3 \cdot y^2} \\
 = \sqrt[3]{y^3} \sqrt[3]{y^2} \\
 = y \sqrt[3]{y^2}
 \end{aligned}$$

$$\begin{aligned}
 \frac{512}{3} &= 170 + \frac{2}{3} \\
 \frac{512}{3} &= 170.\bar{6} \\
 (170)(3) &= 510 \\
 512 - 510 &= 2
 \end{aligned}$$

$$\begin{aligned}
 \frac{512}{3} &= 170\text{-stuff} \\
 (170)(3) &= 510 \\
 512 - 510 &= 2 \\
 & \frac{2}{3}
 \end{aligned}$$

$$\begin{aligned}\sqrt[4]{y^{17}} &= \sqrt[4]{y^{16+1}} = \sqrt[4]{y^{16}y^1} \\ &= y^4 \sqrt[4]{y}\end{aligned}$$

$$\begin{aligned}\sqrt[5]{x^{377}} &= \sqrt[5]{x^{375+2}} = x^{\frac{375}{5}} \sqrt[5]{x^2} \\ &= x^{75} \sqrt[5]{x^2}\end{aligned}$$

$$\begin{aligned} & \sqrt{2} (6 + \sqrt{10}) \\ & 6\sqrt{2} + \sqrt{2}\sqrt{10} \\ & = 6\sqrt{2} + \sqrt{20} \\ & = \boxed{6\sqrt{2} + 2\sqrt{5}} \end{aligned}$$

$$\frac{\sqrt{5 \cdot 4} = \sqrt{20}}{2\sqrt{5}}$$

$$(\sqrt{3} - \sqrt{5})(\sqrt{2} + 7)$$

$$\begin{aligned} & \sqrt{3}\sqrt{2} + 7\sqrt{3} - \sqrt{5}\sqrt{2} - 7\sqrt{5} \\ & \sqrt{6} + 7\sqrt{3} - \sqrt{10} - 7\sqrt{5} \end{aligned}$$

Sideban

$$\sqrt{3}\sqrt{2} + \sqrt{5}\sqrt{2} = (\sqrt{3} + \sqrt{5})\sqrt{2},$$

but nothing gained, unless there's a reason for it.

$$(\sqrt{5} + \sqrt{2})(\sqrt{5} - \sqrt{2}) = 3$$

$$(a+b)(a-b) = a^2 - b^2$$

$$\sqrt{5}\sqrt{5} - \sqrt{5}\sqrt{2} + \sqrt{2}\sqrt{5} + \sqrt{2}\sqrt{2}$$

$$= \sqrt{5^2} - \sqrt{2^2} = 5 - 2 = 3 !$$

$$(\sqrt{3} + \sqrt{7})(\sqrt{3} - \sqrt{7}) = \sqrt{3}^2 - \sqrt{7}^2 = 3 - 7 = -4$$

$$(\sqrt{5} + \sqrt{2})^2 = 5 + 2\sqrt{5}\sqrt{2} + 2 = 7 + 2\sqrt{10}$$

$$(a+b)^2 = a^2 + 2ab + b^2$$

$$(\sqrt{5} + \sqrt{2})(\sqrt{5} + \sqrt{2}) = \sqrt{5}^2 + \sqrt{5}\sqrt{2} + \sqrt{2}\sqrt{5} + \sqrt{2}^2$$

$$\Rightarrow 5 + 2\sqrt{10} + 2$$

$$= 7 + 2\sqrt{10}$$

$$(\sqrt{5})^2 = 5$$

7.4

#s 1-76, every 4th one:

1, 5, 9, ..., stop right b4 #76
Monday.

$$\sqrt[3]{\frac{5x}{27}} + 4\sqrt[3]{5x}$$

$$= \frac{\sqrt[3]{5x}}{\sqrt[3]{27}} + 4\sqrt[3]{5x}$$

$$= \frac{\sqrt[3]{5x}}{3} + \frac{4\sqrt[3]{5x}}{1} \cdot \frac{3}{3}$$

$$= \frac{\sqrt[3]{5x} + 12\sqrt[3]{5x}}{3} = \frac{13\sqrt[3]{5x}}{3}$$

Carlie's great.
~~best~~
time.