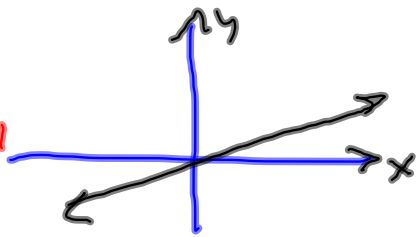


S6.7

Direct Variation

 $y$  varies directly with  $x$ 

$$y = kx$$

for some constant  $k$ .  
→ proportional to.

§  $y = 4$  when  $x = 20$

Find  $k$  & the variation equation.

$$y = kx$$

$$4 = 20k$$

$$y = \frac{1}{5}x$$

$$k = \frac{1}{5} = \frac{4}{20} = k$$

§  $y$  is directly proportional to the square of  $x$ .

$$y = kx^2$$

Falling bodies,  
constant acceleration.

§  $y = 7$  when  $x = 3$ . Find  $y$  when  $x = 5$ .

$$y = kx^2$$

$$7 = (3^2)k$$

$$7 = 9k$$

$$\frac{7}{9} = k$$

$$y = \frac{7}{9}x^2$$

when  $x = 5$ ,

$$y = \frac{7}{9}(5)^2$$

$$= \frac{(7)(25)}{9}$$

$$= \frac{175}{9} = y$$

Find

$$\left(\frac{7}{9}\right)(25)$$

$$= \left(\frac{7}{9}\right)\left(\frac{25}{1}\right)$$

$$= \frac{(7)(25)}{9}$$

## Joint Variation

$y$  varies jointly with  $x$  and  $z$ .

$$y = kxz$$

$y = 7$ , when  $x = 9$ ,  $z = 2$   
 what's  $y$  when  $x = 3$ ,  $z = 8$ ?

Find  $k$   
 use  $k$

$$7 = (9)(2)k$$

$$\frac{7}{18} = k$$

$$y = \frac{7}{18}xz$$

$$y = \frac{7}{18}(3)(8) = \frac{\cancel{24}^{\cancel{12}}(7)}{\cancel{18}_9} = \frac{84}{9} = y$$

## Inverse Variation

$y$  varies inversely with  $x$ .

$$y = \frac{k}{x}$$

$y$  is proportional to the reciprocal of  $x$

$$y = k\left(\frac{1}{x}\right) = \frac{k}{x}$$

Surface area of a ball is proportional to the square of its radius.

Suppose the surface area is  $36\pi$  in<sup>2</sup> when the radius is 3 inches.  
 What's the surface area when radius is 5 inches?

Let  $S$  = surface area (in in<sup>2</sup>)  
 $r$  = radius (in inches)

$$S = kr^2$$

$$36\pi = (3)^2k = 9k$$

$$k = 4\pi = \frac{36\pi}{9} = k =$$

$$S = 4\pi r^2$$

when  $r = 5$

$$S = (4\pi)(5^2) = \boxed{100\pi \text{ square inches}}$$

Perfect

The force of attraction (gravitational) between two bodies varies jointly with the mass of the two bodies and inversely with the square of the distance between them.

$$F = \frac{K m_1 m_2}{r^2}$$

$F$  = force

$m_1$  = mass of 1<sup>st</sup> body

$m_2$  = " " 2<sup>nd</sup> "

$r$  = distance between them

Solve:

$$\frac{4x^2 - 24x}{3x^2 - x - 2} + \frac{3}{3x+2} = \frac{-4}{x-1}$$

$$(3x+2)(x-1) = 3x^2 - 3x + 2x - 2 \\ = 3x^2 - x - 2 \quad \text{cool}$$

$$\text{LCD} = (3x+2)(x-1)$$

$$D = \left\{ x \mid x \neq 1 \text{ and } x \neq -\frac{2}{3} \right\}$$

$$\frac{4x^2 - 24x}{(3x+2)(x-1)} + \left( \frac{3}{3x+2} \right) \left( \frac{x-1}{x-1} \right) = \left( \frac{-4}{x-1} \right) \left( \frac{3x+2}{3x+2} \right)$$

$$4x^2 - 24x + 3(x-1) = -4(3x+2)$$

$$4x^2 - 24x + 3x - 3 = -12x - 8$$

$$+12x + 8 = +12x + 8$$

$$4x^2 - 24x + 15x + 5 = 0$$

$$4x^2 - 9x + 5 = 0$$

Find #s whose product is  
 $(4)(5) = 20$  & which add  
 up to  $-9$

} Forgot to  
 collect  
 like terms.

← Collected l.k. terms.

$$-4-5 = -9$$

$$(-4)(-5) = +20$$

$$4x^2 - 5x - 4x + 5$$

$$x(4x-5) - 1(4x-5)$$

$$(4x-5) \left( \frac{x \cancel{(4x-5)}}{\cancel{(4x-5)}} - \frac{1 \cancel{(4x-5)}}{\cancel{(4x-5)}} \right)$$

$$(4x-5)(x-1) = 0$$

$$4x-5 = 0 \quad \text{OR} \quad x-1 = 0$$

$$4x = 5$$

$$x = \frac{5}{4}$$

$$x = 1$$

$\rightarrow \notin D$

Final Answer:

$$\left\{ \frac{5}{4} \right\}$$