

$$\begin{aligned} & \textcircled{29} \quad \frac{1}{x-5} - \frac{19-2x}{(x-5)(x+4)} \quad \text{LCD} = (x-5)(x+4) \\ & = \frac{1}{x-5} \cdot \frac{(x+4)}{x+4} - \frac{19-2x}{(x-5)(x+4)} = \frac{(x+4) - (19-2x)}{(x-5)(x+4)} \\ & = \frac{x+4-19+2x}{(x-5)(x+4)} = \frac{3x-15}{(x-5)(x+4)} = \frac{3(x-5)}{(x-5)(x+4)} = \boxed{\frac{3}{x+4}} \end{aligned}$$

§ 6.3 Due @ end of class, Monday.

### COMPLEX FRACTIONS

Invert & Multiply

$$\frac{\frac{a}{b}}{\frac{c}{d}} = \frac{a}{b} \cdot \frac{d}{c}$$

$$\frac{\frac{2}{3}}{\frac{4}{5}} = \frac{2}{3} \cdot \frac{5}{4} = \frac{\cancel{2}}{3} \cdot \frac{5}{\cancel{2} \cdot 2} = \frac{5}{6}$$

$$\frac{\frac{15}{2x}}{\frac{5}{6x}} = \frac{\cancel{3}^3}{\cancel{2}^2 x} \cdot \frac{6x}{\cancel{5}_5} = 9$$

$$\frac{1}{2} x \quad \text{BAD}$$

$$\frac{1}{2} x \quad \text{GOOD}$$

$$\frac{1}{2} x \quad \text{BAD}$$

$$\left(\frac{1}{2}\right) x \quad \text{GOOD}$$

$$\frac{\frac{x}{x+2}}{\frac{2}{x+2}} = \frac{x}{x+2} \cdot \frac{x+2}{2} = \frac{\cancel{x} \cancel{(x+2)}}{2 \cancel{(x+2)}} = \frac{x}{2} = \frac{1}{2} x$$

↑  
GOOD

The next level

$$\frac{\frac{x^2 - 4y^2}{xy}}{\frac{1}{y} - \frac{1}{x}} = \frac{\frac{x^2 - 4y^2}{xy}}{\frac{x-y}{xy}} = \frac{x^2 - 4y^2}{xy} \cdot \frac{xy}{x-y}$$

$\frac{1}{y} - \frac{1}{x}$  → Combine into one frac.  
 Do what we did before.

$$\frac{1}{y} \cdot \frac{x}{x} - \frac{1}{x} \cdot \frac{y}{y} = \frac{(x^2 - 4y^2)(\cancel{xy})}{(\cancel{xy})(x-y)} = \frac{x^2 - 4y^2}{x-y}$$

$LCD = xy$

$$= \frac{x-y}{xy}$$

$$\frac{\frac{x^2 - 4y^2}{xy}}{\frac{1}{y} - \frac{1}{x}}$$

LCD = xy } LCD = xy  
 LCD = xy

$$\frac{\frac{x^2 - 4y^2}{\cancel{xy}} \cdot \frac{\cancel{xy}}{1}}{\frac{1}{\cancel{y}} \cdot \frac{\cancel{xy}}{1} - \frac{1}{\cancel{x}} \cdot \frac{\cancel{xy}}{1}} = \frac{x^2 - 4y^2}{x - y}$$

*(x-2y)(x+2y)*  
 leads nowhere  
 in terms of  
 cancellation



$$\frac{\frac{3}{x-4} - \frac{2}{x-4}}{\frac{2}{x-4} - \frac{2}{x}}$$

$LCD = x(x-4)$

$$\frac{\frac{3}{\cancel{x-4}} \cdot \frac{\cancel{x(x-4)}}{1} - \frac{2}{\cancel{x-4}} \cdot \frac{\cancel{x(x-4)}}{1}}{\frac{2}{\cancel{x-4}} \cdot \frac{\cancel{x(x-4)}}{1} - \frac{2}{\cancel{x}} \cdot \frac{\cancel{x(x-4)}}{1}} = \frac{3x - 2x}{2x - 2(x-4)}$$

$= \frac{x}{2x - 2x + 8} = \frac{x}{8}$

LCD is  $x$

$$\frac{\frac{3}{x-4} - \frac{2}{x-4}}{\frac{2}{x-4} - \frac{2}{x}} = \frac{\frac{1}{x-4}}{\frac{2}{x-4} \cdot \frac{x}{x} - \frac{2}{x} \cdot \frac{x-4}{x-4}}$$

$$= \frac{\frac{1}{x-4}}{\frac{2x - 2(x-4)}{x(x-4)}} = \frac{\frac{1}{x-4}}{\frac{8}{x(x-4)}}$$

$$\frac{1}{\cancel{x-4}} \cdot \frac{\cancel{x(x-4)}}{8} = \frac{x}{8}$$

$$\frac{a^{-1} - 4}{4 + a^{-2}} = \frac{\frac{1}{a} - 4}{4 + \frac{1}{a^2}}$$

Method 1

LCD =  $a^2$ 

$$\frac{\frac{1}{a} \cdot \frac{a^2}{1} - 4a^2}{4a^2 + \frac{1}{a^2} \cdot \frac{a^2}{1}}$$

$$= \frac{a - 4a^2}{4a^2 + 1}$$

$$= \frac{a(1-4a)}{4a^2+1}$$

$$\frac{a - 4a^2}{4a^2 + 1}$$

Method 2

$$\frac{\frac{1}{a} - \frac{4a}{a}}{\frac{4a^2}{a^2} + \frac{1}{a^2}}$$

$$= \frac{\frac{1-4a}{a}}{\frac{4a^2+1}{a^2}}$$

$$= \frac{1-4a}{a} \cdot \frac{a^2}{4a^2+1} = \frac{(1-4a)a}{4a^2+1}$$

$$\frac{5}{7} = \frac{\cancel{2}+3}{\cancel{2}+5} = \frac{3}{5}$$

! ? No!

$$\text{Quotient} = \frac{\text{numerator}}{\text{denominator}} = \frac{\text{Dividend}}{\text{Divisor}}$$

§ 6.4 Division of Polynomials.  
we've already sorts done this.

Factor out the GCF

$$\begin{aligned} & 6x^5 - 8x^4 + 2x^3 \\ = & 2x^3 \left( \frac{6x^5}{2x^3} - \frac{8x^4}{2x^3} + \frac{2x^3}{2x^3} \right) \\ = & 2x^3 (3x^2 - 4x + 1) \end{aligned}$$

Division by the monomial  $2x^3$  is term-by-term.



$$\frac{296}{7}$$

$$\begin{array}{r} 42 \text{ r } 2 \\ 7 \overline{) 296} \\ \underline{-(28)} \\ 16 \\ \underline{-(14)} \\ 2 \end{array}$$

This says

$$\frac{296}{7} = 42 + \frac{2}{7}$$

= Quotient +  $\frac{\text{Remainder}}{\text{Divisor}}$

OR

$$296 = (7)(42) + 2$$

Dividend = Divisor · Quotient + Remainder

$$\frac{x^3 - 7x^2 + 2x + 5}{x - 3} = ?$$

$$\begin{array}{r} x^2 - 4x - 10 \text{ r } -25 \\ x-3 \overline{) x^3 - 7x^2 + 2x + 5} \\ \underline{-(x^3 + 3x^2)} \\ -4x^2 + 2x + 5 \\ \underline{+(4x^2 + 12x)} \\ -10x + 5 \\ \underline{+(10x + 30)} \\ -25 \end{array}$$

Subtract →

$$\begin{aligned} \frac{x^3}{x} &= x^2 \\ x^2(x-3) &= x^3 - 3x^2 \\ \frac{-4x^2}{x} &= -4x \\ -4x(x-3) &= -4x^2 + 12x \\ \frac{-10x}{x} &= -10 \end{aligned}$$

$$\frac{x^3 - 7x^2 + 2x + 5}{x - 3} = x^2 - 4x - 10 - \frac{25}{x - 3}$$

$$x^3 - 7x^2 + 2x + 5 = (x - 3)(x^2 - 4x - 10) - 25$$