

§ 5.4 #75

$$\begin{aligned}
 & (x+y)(2x-1)(x+1) \\
 = & (x+y)(2x^2+2x-x-1) \\
 = & (x+y)(2x^2+x-1) \\
 = & 2x^3+x^2-x+2x^2y+xy-y
 \end{aligned}$$

$$\begin{aligned}
 (a+b)(a+b) &= \\
 \underline{a^2+ab+ab+b^2} &= \\
 (a+b)^2 &= \\
 \underline{a^2+2ab+b^2} &
 \end{aligned}$$

$$\textcircled{35} \quad (3+(4b+1))^2$$

$$= 3^2 + \underline{2(3)(4b+1)} + (4b+1)^2$$

$$= 9 + 6(4b+1) + (4b)^2 + 2(4b)(1) + 1^2$$

$$= \underline{9} + \underline{24b} + \underline{6} + 16b^2 + \underline{8b} + \underline{1}$$

$$= 16b^2 + 32b + 16$$

$$\begin{aligned}
 (a+b)^2 &= \\
 a^2+2ab+b^2 &
 \end{aligned}$$

$$(5x^{257} - 133)^2$$

$$= (5x^{257})^2 - 2(5x^{257})(133) + 133^2$$

Factoring by Grouping

$$\begin{aligned} & \underline{2b+3a} + \underline{2b+6} \\ = & 2(b+3) + 2(b+3) \\ = & (b+3) \left(\frac{\cancel{2(b+3)}}{\cancel{(b+3)}} + \frac{\cancel{2(b+3)}}{\cancel{(b+3)}} \right) \\ = & (b+3)(2+2) \end{aligned}$$

$$(5x+6)(3x-2) = 15x^2 - 10x + 18x - 12$$

$(-10)(18) = -180$
 $(15)(-12) = -180$

$$(6x+7)(3x+11)$$

$$= 18x^2 + 66x + 21x + 77$$

$(66)(21) = 1386$
 1386

Magic!

Factor $15x^2 + 8x - 12$

$(15)(-12) = -180$

$$8 = 9 - 1 \quad (9)(-1) = -9$$

$$8 = 10 - 2 \quad (10)(-2) = -20$$

$$= 15 - 7 \quad (15)(-7) = -105$$

$$= 20 - 12 \quad (20)(-12) = -240$$

$$= 18 - 10 \quad (18)(-10) = -180$$

Sweet!

Find numbers that
 SUBTRACT to
 give 8 AND
 Multiply together
 to give -180.
 Subtract because
 -180 is negative.

$$15x^2 + 18x - 10x - 12$$

$$= 3x(5x+6) - 2(5x+6)$$

$$= (5x+6)(3x-2)$$

$$42x^2 + 95x + 50 \quad (42)(50) = \underline{2100}$$

Find #s that sum to 95, 850 higher and multiply to 1500 higher give 2100
1950 Higher
2100 Sweet!

$$95 = 94 + 1$$

$$= 85 + 10$$

$$= 75 + 20$$

$$= 65 + 30$$

$$= 60 + 35$$

$$42x^2 + 60x + 35x + 50$$

$$= 6x(\underline{7x + 10}) + 5(\underline{7x + 10})$$

$$= (7x + 10)(6x + 5)$$

$$\begin{array}{r} 2 \overline{)42} \\ 3 \overline{)21} \\ 7 \end{array}$$

$$\begin{array}{r} 2 \overline{)60} \\ 2 \overline{)30} \\ 3 \overline{)15} \\ 5 \end{array}$$

$$\begin{aligned} & -x^2 + 5x - 6 \\ = & -(\underline{x^2 - 5x + 6}) \\ & \text{Factor } x^2 - 5x + 6 \quad (x-3)(x-2) \\ & \text{Negate the result} \quad - (x-3)(x-2) \end{aligned}$$

$$72x^2 - 54x - 35$$

↑

$$(72)(35) = -2520$$

$$(-84)(30) = -2520$$

$$72x^2 - 84x + 30x - 35$$

$$12x(6x - 7) + 5(6x - 7)$$

$$(6x - 7)(12x + 5)$$

Shawn
Hon. Mention:
Nicholas.

$$\begin{array}{r}
 2 \overline{) 2520} \\
 \underline{2} \\
 2 \overline{) 1260} \\
 \underline{2} \\
 2 \overline{) 630} \\
 \underline{2} \\
 3 \overline{) 315} \\
 \underline{3} \\
 3 \overline{) 105} \\
 \underline{3} \\
 5 \overline{) 35} \\
 \underline{5} \\
 7
 \end{array}$$

2 · 2 · 2 · 3 · 3 · 5 · 7