

$$i^{58} = i^{2 \cdot 29} = (i^2)^{29} = (-1)^{29} = -1$$

$$2^5 \cdot 3^2 \cdot 7 \cdot 11^3 = ?$$

Factored into the product of powers of primes.

$$2,683,296$$

Handwritten prime factorization tree for 2,683,296:

- 2683296 ÷ 2 = 1341648
- 1341648 ÷ 2 = 670824
- 670824 ÷ 2 = 335412
- 335412 ÷ 2 = 167706
- 167706 ÷ 3 = 55902
- 55902 ÷ 3 = 18634
- 18634 ÷ 7 = 2662
- 2662 ÷ 11 = 242
- 242 ÷ 11 = 22
- 22 ÷ 11 = 2

- 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41

$$2^5 \cdot 3^2 \cdot 7 \cdot 11^3$$

$$\sqrt{2683296}$$

$$= \sqrt{2^5 \cdot 3^2 \cdot 7 \cdot 11^3}$$

$$= \sqrt{2^4 \cdot 2^1 \cdot 3^2 \cdot 7^1 \cdot 11^2 \cdot 11^1}$$

$$= 2^{\frac{4}{2}} \cdot 3^{\frac{2}{2}} \cdot 11^{\frac{2}{2}} \sqrt{2 \cdot 7 \cdot 11}$$

$$= 2^2 \cdot 3 \cdot 11 \sqrt{154}$$

$$= 132 \sqrt{154}$$

$$\frac{133}{13} = 10 \frac{3}{13}$$

$$\sqrt[3]{2683296}$$

$$= \sqrt[3]{2^5 \cdot 3^2 \cdot 7 \cdot 11^3}$$

$$= \sqrt[3]{2^3 \cdot 2^2 \cdot 7 \cdot 11^3}$$

$$= 2^{\frac{3}{3}} \cdot 11^{\frac{3}{3}} \sqrt[3]{2^2 \cdot 7 \cdot 3^2}$$

$$= 2 \cdot 11 \sqrt[3]{28 \cdot 3^2} = 22 \sqrt[3]{252}$$

$$\sqrt{x^4} = x^2$$

$$\sqrt{x^6} = |x^3| \quad \text{if } x \text{ is real.}$$

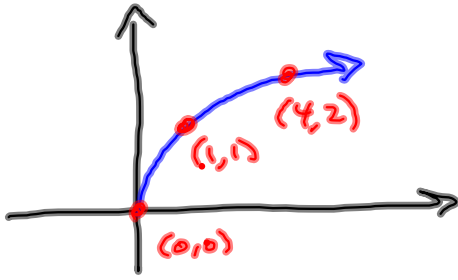
If x is positive, then

$$\sqrt{x^6} = x^3$$

$$\begin{aligned} \sqrt{x^{11}} &= \sqrt{x^{10+1}} \\ &= \sqrt{x^{10} x^1} = x^{\frac{10}{2}} \sqrt{x^1} \\ &= x^5 \sqrt{x} \end{aligned}$$

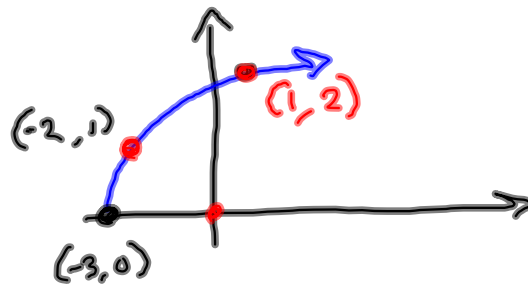
$$\begin{array}{r} 7 \overline{) 28} \\ \underline{25} \\ 25 \\ \underline{25} \\ 2 \end{array}$$

$$f(x) = \sqrt{x}$$



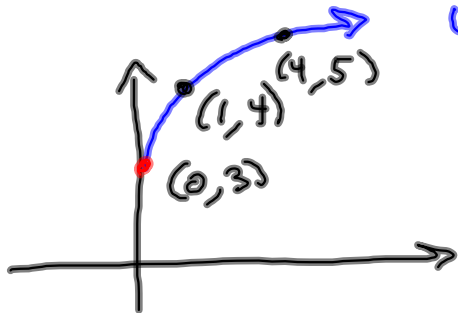
$$f(x+3) = \sqrt{x+3}$$

Left + 3



$$f(x) + 3 = \sqrt{x} + 3$$

Up 3



All working
off the
basic graph of
 $f(x)$.

$$\sqrt{x-3}$$

RIGHT 3

$$\sqrt{x} - 3$$

Down 3

Rationalize the
Denominator

$$\left(\frac{2+3\sqrt{2}}{5-2\sqrt{2}} \right) \left(\frac{5+2\sqrt{2}}{5+2\sqrt{2}} \right)$$

$$= \frac{10 + 4\sqrt{2} + 15\sqrt{2} + 6 \cdot 2}{25 - 8}$$

$$= \frac{22 + 19\sqrt{2}}{17}$$

Divide

$$\left(\frac{2+3i}{5-2i} \right) \left(\frac{5+2i}{5+2i} \right)$$

$$= \frac{10 + 4i + 15i + 6i^2}{5^2 + 2^2}$$

$$= \frac{4 + 19i}{29} = \frac{4}{29} + \frac{19}{29}i$$