

1. (10 pts) Form a polynomial in factored form with *real* coefficients with the given zeros and degree. Please do not expand the polynomial.

Zeros: -2, multiplicity 1; -5, multiplicity 2. Degree 3.

2. (10 pts) Expand $(x - 3 - 2i)(x - 3 + 2i)$

3. (10 pts) Use synthetic division to find $P(3)$ if $P(x) = 3x^5 - 2x^4 + 2x^2 - 7x + 5$.

4. (10 pts) Divide $f(x) = x^4 - 3x^3 + 2x + 5$ by $d(x) = x^2 + 3$. Then write the result in the form $Dividend = Divisor \cdot Quotient + Remainder$.

5. Solve the inequalities:

a. (10 pts) $3(x-2)^2(x+1)(x-1)^2 \geq 0$

b. (10 pts) $\frac{3(x-2)^2}{(x+1)(x-1)^2} \geq 0$ (A very different-looking function, but not so very different, when it comes to solving inequalities).

c. (10 pts) What is the domain of $f(x) = \log_2 \left(\frac{3(x-2)^2}{(x+1)(x-1)^2} \right)$?

6. (20 pts) Find the *real* zeros of $f(x) = x^5 - 4x^4 + 2x^3 + 14x^2 - 23x + 10$. Factor f over the set of real numbers.

7. (10 pts) Find the remaining (nonreal) zeros of f and factor f over the set of *complex* numbers.